

Algebra 1

Chapter 3 Resource Masters



New York, New York Columbus, Ohio Chicago, Illinois Peoria, Illinois Woodland Hills, California

Consumable Workbooks

Many of the worksheets contained in the Chapter Resource Masters booklets are available as consumable workbooks in both English and Spanish.

Study Guide and Intervention Workbook	0-07-827753-1
Study Guide and Intervention Workbook (Spanish)	0-07-827754-X
Skills Practice Workbook	0-07-827747-7
Skills Practice Workbook (Spanish)	0-07-827749-3
Practice Workbook	0-07-827748-5
Practice Workbook (Spanish)	0-07-827750-7

ANSWERS FOR WORKBOOKS The answers for Chapter 3 of these workbooks can be found in the back of this Chapter Resource Masters booklet.





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Algebra 1 Chapter 3 Resource Masters

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Teacher's Guide to Using the Chapter 3 Resource Masters

The *Fast File* Chapter Resource system allows you to conveniently file the resources you use most often. The *Chapter 3 Resource Masters* includes the core materials needed for Chapter 3. These materials include worksheets, extensions, and assessment options. The answers for these pages appear at the back of this booklet.

All of the materials found in this booklet are included for viewing and printing in the *Algebra 1 TeacherWorks* CD-ROM.

Vocabulary Builder Pages vii—viii include a student study tool that presents up to twenty of the key vocabulary terms from the chapter. Students are to record definitions and/or examples for each term. You may suggest that students highlight or star the terms with which they are not familiar.

WHEN TO USE Give these pages to students before beginning Lesson 3-1. Encourage them to add these pages to their Algebra Study Notebook. Remind them to add definitions and examples as they complete each lesson.

Study Guide and Intervention

Each lesson in *Algebra 1* addresses two objectives. There is one Study Guide and Intervention master for each objective.

WHEN TO USE Use these masters as reteaching activities for students who need additional reinforcement. These pages can also be used in conjunction with the Student Edition as an instructional tool for students who have been absent.

Skills Practice There is one master for each lesson. These provide computational practice at a basic level.

WHEN TO USE These masters can be used with students who have weaker mathematics backgrounds or need additional reinforcement.

Practice There is one master for each lesson. These problems more closely follow the structure of the Practice and Apply section of the Student Edition exercises. These exercises are of average difficulty.

WHEN TO USE These provide additional practice options or may be used as homework for second day teaching of the lesson.

Reading to Learn Mathematics

One master is included for each lesson. The first section of each master asks questions about the opening paragraph of the lesson in the Student Edition. Additional questions ask students to interpret the context of and relationships among terms in the lesson. Finally, students are asked to summarize what they have learned using various representation techniques.

WHEN TO USE This master can be used as a study tool when presenting the lesson or as an informal reading assessment after presenting the lesson. It is also a helpful tool for ELL (English Language Learner) students.

Enrichment There is one extension master for each lesson. These activities may extend the concepts in the lesson, offer an historical or multicultural look at the concepts, or widen students' perspectives on the mathematics they are learning. These are not written exclusively for honors students, but are accessible for use with all levels of students.

WHEN TO USE These may be used as extra credit, short-term projects, or as activities for days when class periods are shortened.

Assessment Options

The assessment masters in the *Chapter 3 Resources Masters* offer a wide range of assessment tools for intermediate and final assessment. The following lists describe each assessment master and its intended use.

Chapter Assessment CHAPTER TESTS

- *Form 1* contains multiple-choice questions and is intended for use with basic level students.
- Forms 2A and 2B contain multiple-choice questions aimed at the average level student. These tests are similar in format to offer comparable testing situations.
- Forms 2C and 2D are composed of freeresponse questions aimed at the average level student. These tests are similar in format to offer comparable testing situations. Grids with axes are provided for questions assessing graphing skills.
- *Form 3* is an advanced level test with free-response questions. Grids without axes are provided for questions assessing graphing skills.
 - All of the above tests include a freeresponse Bonus question.
- The Open-Ended Assessment includes performance assessment tasks that are suitable for all students. A scoring rubric is included for evaluation guidelines. Sample answers are provided for assessment.
- A **Vocabulary Test**, suitable for all students, includes a list of the vocabulary words in the chapter and ten questions assessing students' knowledge of those terms. This can also be used in conjunction with one of the chapter tests or as a review worksheet.

Intermediate Assessment

- Four free-response **quizzes** are included to offer assessment at appropriate intervals in the chapter.
- A **Mid-Chapter Test** provides an option to assess the first half of the chapter. It is composed of both multiple-choice and free-response questions.

Continuing Assessment

- The **Cumulative Review** provides students an opportunity to reinforce and retain skills as they proceed through their study of Algebra 1. It can also be used as a test. This master includes free-response questions.
- The **Standardized Test Practice** offers continuing review of algebra concepts in various formats, which may appear on the standardized tests that they may encounter. This practice includes multiple-choice, grid-in, and quantitative-comparison questions. Bubble-in and grid-in answer sections are provided on the master.

Answers

- Page A1 is an answer sheet for the Standardized Test Practice questions that appear in the Student Edition on pages 186–187. This improves students' familiarity with the answer formats they may encounter in test taking.
- The answers for the lesson-by-lesson masters are provided as reduced pages with answers appearing in red.
- Full-size answer keys are provided for the assessment masters in this booklet.

NAME	DATE	PERIOD	
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Reading to Learn Mathematics

Vocabulary Builder

This is an alphabetical list of the key vocabulary terms you will learn in Chapter 3. As you study the chapter, complete each term's definition or description. Remember to add the page number where you found the term. Add these pages to your Algebra Study Notebook to review vocabulary at the end of the chapter.

Vocabulary Term	Found on Page	Definition/Description/Example
consecutive integers		
kuhn-SEH-kyuh-tihv		
defining a variable		
dimensional analysis		
duh-MEHNCH-nuhl		
equivalent equation		
ih-KWIHV-luhnt		
extremes		
formula		
identity		
means		
multi-step equations		

(continued on the next page)

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3

Reading to Learn Mathematics

Vocabulary Builder (continued)

Vocabulary Term	Found on Page	Definition/Description/Example
number theory		
percent of change		
percent of decrease		
percent of increase		
proportion		
pruh-POHR-shun		
ratio		
rate		
scale		
solve an equation		
weighted average		
work backward		

3-1

Study Guide and Intervention

Writing Equations

Write Equations Writing equations is one strategy for solving problems. You can use a variable to represent an unspecified number or measure referred to in a problem. Then you can write a verbal expression as an algebraic expression.

Example 1 Translate each sentence into an equation or a formula.

a. Ten times a number x is equal to 2.8 times the difference y minus z.

$$10 \times x = 2.8 \times (y - z)$$

The equation is
$$10x = 2.8(y - z).$$

b. A number m minus 8 is the same as a number n divided by 2.

$$m-8=n \div 2$$

The equation is $m-8=\frac{n}{2}$.

c. The area of a rectangle equals the length times the width. Translate this sentence into a formula.

Let A = area, $\ell = \text{length}$, and w = width.

Formula: Area equals length times width.

 $A = \ell \times w$

The formula for the area of a rectangle is $A = \ell w$.

Example 2

Use the Four-Step

Problem-Solving Plan.

The population of the United States in 2001 was about 284,000,000, and the land area of the United States is about 3,500,000 square miles. Find the average number of people per square mile in the United States.

Source: www.census.gov

- **Step 1** *Explore* You know that there are 284,000,000 people. You want to know the number of people per square mile.
- **Step 2** *Plan* Write an equation to represent the situation. Let p represent the number of people per square mile. $3,500,000 \times p = 284,000,000$
- Step 3 Solve 3,500,000 \times p = 284,000,000. 3,500,000p = 284,000,000 Divide each side by $p \approx 81.14$ 3,500,000.

There about 81 people per square mile.

Step 4 *Examine* If there are 81 people per square mile and there are 3,500,000 square miles, $81 \times 3,500,000 = 283,500,000$, or about 284,000,000 people. The answer makes sense.

Exercises

Translate each sentence into an equation or formula.

- 1. Three times a number t minus twelve equals forty.
- **2.** One-half of the difference of a and b is 54.
- **3.** Three times the sum of d and 4 is 32.
- **4.** The area A of a circle is the product of π and the radius r squared.

WEIGHT LOSS For Exercises 5-6, use the following information.

Lou wants to lose weight to audition for a part in a play. He weighs 160 pounds now. He wants to weigh 150 pounds.

- **5.** If *p* represents the number of pounds he wants to lose, write an equation to represent this situation.
- 6. How many pounds does he need to lose to reach his goal?

3-1 Study Guide and Intervention (continued) Writing Equations

Write Verbal Sentences You can translate equations into verbal sentences.

Example

Translate each equation into a verbal sentence.

a.
$$4n - 8 = 12$$
.

4n

- 8 = 12

Four times n minus eight equals twelve.

b.
$$a^2 + b^2 = c^2$$

 $a^2 + b^2$

=

 c^2

The sum of the squares of a and b is equal to the square of c.

Exercises

Translate each equation into a verbal sentence.

1.
$$4a - 5 = 23$$

2.
$$10 + k = 4k$$

3.
$$6xy = 24$$

4.
$$x^2 + y^2 = 8$$

5.
$$p + 3 = 2p$$

6.
$$b = \frac{1}{3}(h-1)$$

7.
$$100 - 2x = 80$$

8.
$$3(g + h) = 12$$

9.
$$p^2 - 2p = 9$$

10.
$$C = \frac{5}{9}(F - 32)$$

11.
$$V = \frac{1}{3}Bh$$

12.
$$A = \frac{1}{2}hb$$

Skills Practice

Writing Equations

Translate each sentence into an equation.

- **1.** Two added to three times a number m is the same as 18.
- **2.** Twice a increased by the cube of a equals b.
- **3.** Seven less than the sum of p and q is as much as 6.
- **4.** The sum of x and its square is equal to y times z.
- **5.** Four times the sum of f and g is identical to six times g.

Translate each sentence into a formula.

- **6.** The perimeter P of a square equals four times the length of a side s.
- **7.** The area *A* of a square is the length of a side *s* squared.
- **8.** The perimeter P of a triangle is equal to the sum of the lengths of sides a, b, and c.
- **9.** The area A of a circle is pi times the radius r squared.
- **10.** The volume V of a rectangular prism equals the product of the length ℓ , the width w, and the height h.

Translate each equation into a verbal sentence.

$$11.g + 10 = 3g$$

12.
$$2p + 4q = 20$$

13.
$$4(a + b) = 9a$$

14.
$$8 - 6x = 4 + 2x$$

15.
$$\frac{1}{2}(f+y) = f-5$$

16.
$$s^2 - n^2 = 2b$$

Write a problem based on the given information.

17.
$$c = \cos t$$
 per pound of plain coffee beans $c + 3 = \cos t$ per pound of flavored coffee beans $2c + (c + 3) = 21$

18.
$$p = \cos t$$
 of dinner $0.15p = \cos t$ of a 15% tip $p + 0.15p = 23$

3-1 Practice

Writing Equations

Translate each sentence into an equation.

- **1.** Fifty-three plus four times c is as much as 21.
- **2.** The sum of five times h and twice g is equal to 23.
- **3.** One fourth the sum of r and ten is identical to r minus 4.
- **4.** Three plus the sum of the squares of w and x is 32.

Translate each sentence into a formula.

- **5.** Degrees Kelvin *K* equals 273 plus degrees Celsius *C*.
- **6.** The total cost C of gas is the price p per gallon times the number of gallons g.
- **7.** The sum S of the measures of the angles of a polygon is equal to 180 times the difference of the number of sides n and 2.

Translate each equation into a verbal sentence.

8.
$$q - (4 + p) = \frac{1}{3}q$$

9.
$$\frac{3}{5}t + 2 = t$$

10.
$$9(y^2 + x) = 18$$

11.
$$2(m-n)=v+7$$

Write a problem based on the given information.

12.
$$a = \cos t$$
 of one adult's ticket to zoo
$$a - 4 = \cos t \text{ of one children's ticket to zoo}$$

$$2a + 4(a - 4) = 38$$
13. $c = \text{regular cost of one airline ticket}$

$$0.20c = \text{amount of } 20\% \text{ promotional discount}$$

$$3(c - 0.20c) = 330$$

14. GEOGRAPHY About 15% of all federally-owned land in the 48 contiguous states of the United States is in Nevada. If F represents the area of federally-owned land in these states, and N represents the portion in Nevada, write an equation for this situation.

FITNESS For Exercises 15–17, use the following information.

Deanna and Pietra each go for walks around a lake a few times per week. Last week, Deanna walked 7 miles more than Pietra.

- **15.** If p represents the number of miles Pietra walked, write an equation that represents the total number of miles T the two girls walked.
- 16. If Pietra walked 9 miles during the week, how many miles did Deanna walk?
- **17.** If Pietra walked 11 miles during the week, how many miles did the two girls walk together?

Reading to Learn Mathematics

Writing Equations

Pre-Activity How are equations used to describe heights?

Read the introduction to Lesson 3-1 at the top of page 120 in your textbook.

Does the equation 305 - s = 154 also represent the situation? Explain.

Reading the Lesson

1. Translate each sentence into an equation.

a.	Two	times	the sum of x and three	minus	four	equals	four	times	Х.

b.	The difference of <i>k</i> and 3	is	two	times	k	divided by	five.

2. A 1 oz serving of chips has 140 calories. There are about 14 servings of chips in a bag. How many calories are there in a bag of chips? Write what your solution would be as you use each step in the Four-Step Problem-Solving Plan.

Explore What do you know?

What do you want to know?

Plan Write an equation.

Solve Solve the problem.

Examine Does your answer make sense?

Helping You Remember

3. If you cannot remember all the steps of the Four-Step Problem-Solving Plan, try to remember the first letters of the first word in each step. Write those letters here with their associated words.

Enrichment

Rep-Tiles

A rep-tile is a figure that can be subdivided into smaller copies of itself. The large figure is similar to the small ones and the small figures are all congruent.



Show that each figure is a rep-tile by subdividing it into four smaller and similar figures.

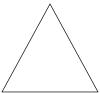
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2.



3.

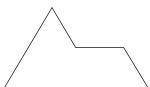


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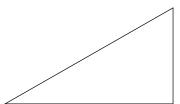


Subdivide each rep-tile into nine smaller and similar figures.

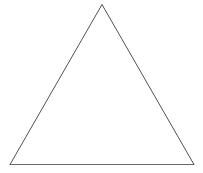
7.



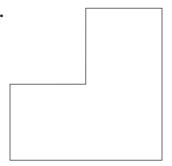
8.



9.



10.



Study Guide and Intervention

Solving Equations by Using Addition and Subtraction

Solve Using Addition If the same number is added to each side of an equation, the resulting equation is equivalent to the original one. In general if the original equation involves subtraction, this property will help you solve the equation.

Addition Property of Equality

For any numbers a, b, and c, if a = b, then a + c = b + c.

Example 1

Solve
$$m - 32 = 18$$
.

$$m-32=18$$
 Original equation $m-32+32=18+32$ Add 32 to each side. $m=50$ Simplify.

The solution is 50.

Example 2 Solve
$$-18 = p - 12$$
.

$$-18=p-12$$
 Original equation $-18+12=p-12+12$ Add 12 to each side. $p=-6$ Simplify.

The solution is -6.

Exercises

Solve each equation. Then check your solution.

1.
$$h - 3 = -2$$

2.
$$m - 8 = -12$$

$$3. p - 5 = 15$$

4.
$$20 = y - 8$$

5.
$$k - 0.5 = 2.3$$

6.
$$w - \frac{1}{2} = \frac{5}{8}$$

7.
$$h - 18 = -17$$

8.
$$-12 = -24 + k$$

$$9.j - 0.2 = 1.8$$

10.
$$b - 40 = -40$$

11.
$$m - (-12) = 10$$

12.
$$w - \frac{3}{2} = \frac{1}{4}$$

Write an equation for each problem. Then solve the equation and check the solution.

- **13.** Twelve subtracted from a number equals 25. Find the number.
- **14.** What number decreased by 52 equals -12?
- **15.** Fifty subtracted from a number equals eighty. Find the number.
- **16.** What number minus one-half is equal to negative one-half?
- 17. The difference of a number and eight is equal to 14. What is the number?
- **18.** A number decreased by fourteen is equal to eighteen. What is the number?

3-2

Study Guide and Intervention (continued)

Solving Equations by Using Addition and Subtraction

Solve Using Subtraction If the same number is subtracted from each side of an equation, the resulting equation is equivalent to the original one. In general if the original equation involves addition, this property will help you solve the equation.

Subtraction Property of Equality

For any numbers a, b, and c, if a = b, then a - c = b - c.

Example

Solve
$$22 + p = -12$$
.

$$22 + p = -12$$

Original equation

$$22 + p - 22 = -12 - 22$$

Subtract 22 from each side.

$$p = -34$$

Simplify.

The solution is -34.

Exercises

Solve each equation. Then check your solution.

$$1.x + 12 = 6$$

$$2.z + 2 = -13$$

$$3. -17 = b + 4$$

4.
$$s + (-9) = 7$$

$$5. -3.2 = \ell + (-0.2)$$

6.
$$-\frac{3}{8} + x = \frac{5}{8}$$

7.
$$19 + h = -4$$

$$8. -12 = k + 24$$

9.
$$j + 1.2 = 2.8$$

10.
$$b + 80 = -80$$

11.
$$m + (-8) = 2$$

12.
$$w + \frac{3}{2} = \frac{5}{8}$$

Write an equation for each problem. Then solve the equation and check the solution.

- 13. Twelve added to a number equals 18. Find the number.
- 14. What number increased by 20 equals -10?
- 15. The sum of a number and fifty equals eighty. Find the number.
- **16.** What number plus one-half is equal to four?
- 17. The sum of a number and 3 is equal to -15. What is the number?

3-2 Skills Practice

Solving Equations by Using Addition and Subtraction

Solve each equation. Then check your solution.

$$1.y - 7 = 8$$

$$3. p - 4 = 6$$

5.
$$98 = b + 34$$

$$7.s + (-28) = 0$$

9.
$$-1 = s + (-19)$$

11.
$$14 = d + (-10)$$

13.
$$11 = -16 + y$$

15.
$$47 = w - (-8)$$

17.
$$4 - (-h) = 68$$

2.
$$w + 14 = -8$$

$$4. -13 = 5 + x$$

6.
$$v - 32 = -1$$

8.
$$y + (-10) = 6$$

10.
$$i - (-17) = 36$$

12.
$$u + (-5) = -15$$

14.
$$c - (-3) = 100$$

16.
$$x - (-74) = -22$$

18.
$$-56 = 20 - (-e)$$

Write an equation for each problem. Then solve the equation and check your solution.

- **19.** A number decreased by 14 is -46. Find the number.
- **20.** Thirteen subtracted from a number is -5. Find the number.
- **21.** The sum of a number and 67 is equal to -34. Find the number.
- **22.** What number minus 28 equals -2?
- **23.** A number plus -73 is equal to 27. What is the number?
- **24.** A number plus -17 equals -1. Find the number.
- **25.** What number less 5 is equal to -39?

3-2 Practice

Solving Equations by Using Addition and Subtraction

Solve each equation. Then check your solution.

$$1.d - 8 = 17$$

2.
$$v + 12 = -5$$

$$3, b - 2 = -11$$

4.
$$-16 = s + 71$$

5.
$$29 = a - 76$$

6.
$$-14 + v = -2$$

7.
$$8 - (-c) = 1$$

8.
$$78 + r = -15$$

9.
$$f + (-3) = -9$$

10.
$$4.2 = n + 7.3$$

11.
$$w + 1.9 = -2.5$$

12.
$$4.6 - (-b) = -0.4$$

13.
$$y - (-1.5) = 0.5$$

14.
$$a - 0.13 = -0.58$$

15.
$$k + (-4.21) = -19$$

16.
$$r + \frac{1}{5} = \frac{9}{10}$$

17.
$$\frac{5}{9} + q = \frac{2}{3}$$

18.
$$\frac{1}{3} = h + \frac{2}{5}$$

19.
$$\frac{1}{4} + x = -\frac{7}{12}$$

20.
$$y + \frac{4}{5} = \frac{3}{4}$$

21.
$$-\frac{7}{8} - (-n) = -\frac{7}{12}$$

Write an equation for each problem. Then solve the equation and check your solution.

22. What number minus 9 is equal to -18?

23. A number plus 15 equals -12. What is the number?

24. The sum of a number and -3 is equal to -91. Find the number.

25. Negative seventeen equals 63 plus a number. What is the number?

26. The sum of negative 14, a number, and 6 is -5. What is the number?

27. What number plus one half is equal to three eighths?

HISTORY For Exercises 28 and 29, use the following information.

Galileo Galilei was born in 1564. Many years later, in 1642, Sir Isaac Newton was born.

28. Write an addition equation to represent the situation.

29. How many years after Galileo was born was Isaac Newton born?

HURRICANES For Exercises 30 and 31, use the following information.

The day after a hurricane, the barometric pressure in a coastal town has risen to 29.7 inches of mercury, which is 2.9 inches of mercury higher than the pressure when the eye of the hurricane passed over.

30. Write an addition equation to represent the situation.

31. What was the barometric pressure when the eye passed over?

Lesson 3-2

3-2

Reading to Learn Mathematics

Solving Equations by Using Addition and Subtraction

Pre-Activity How can equations be used to compare data?

Read the introduction to Lesson 3-2 at the top of page 128 in your textbook. In the equation m-66=5, the number 5 represents and the number 66 represents

Reading the Lesson

- **1.** To solve x + 17 = 46 using the Subtraction Property of Equality, you would subtract from each side.
- **2.** To solve y 9 = -30 using the Addition Property of Equality, you would add _____ to each side.
- **3.** Write an equation that you could solve by subtracting 32 from each side.
- **4.** A student used the Subtraction Property of Equality to solve an equation. Explain why it would also be possible to use the Addition Property of Equality to solve the equation.

Helping You Remember

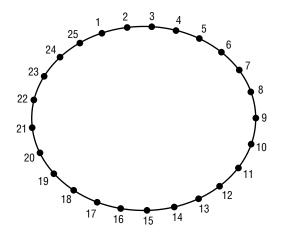
5. Explain how you decide whether to use the Addition Property or the Subtraction Property of Equality to solve an equation.

3-2 Enrichment

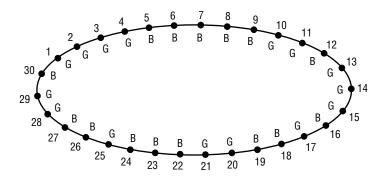
Counting-Off Puzzles

Solve each puzzle.

1. Twenty-five people are standing in a circle. Starting with person 1, they count off from 1 to 7 and then start over with 1. Each person who says "7" drops out of the circle. Who is the last person left?



- **2.** Forty people stand in a circle. They count off so that every third person drops out. Which two people are the last ones left?
- 3. Only half of the 30 students in Sharon's class can go on a field trip. Sharon arranges the boys and girls as shown. They count off from 1 to 9 and every ninth person drops out until only 15 people are left. Who gets to go on the field trip.



A group of people stand in a circle and count off 1, 2, 1, 2, 1 and so on. Every second person drops out. Person number 1 is the last person left.

- **4.** Draw a diagram to show why the number of people in the circle must be even. Then, explain your answer.
- **5.** When the count returns to person number 1 for the first time, how many people have dropped out?
- **6.** Find the number of people in the circle if the number is between 10 and 20. Do the same if the number is between 30 and 40. What can you conclude about the original number of people?

Study Guide and Intervention

Solving Equations by Using Multiplication and Division

Solve Using Multiplication If each side of an equation is multiplied by the same number, the resulting equation is equivalent to the given one. You can use the property to solve equations involving multiplication and division.

Multiplication Property of Equality

For any numbers a, b, and c, if a = b, then ac = bc.

Example 1 Solve
$$3\frac{1}{2}p = 1\frac{1}{2}$$
.

$$3\frac{1}{2}p = 1\frac{1}{2}$$

 $3\frac{1}{9}p = 1\frac{1}{9}$ Original equation

$$\frac{7}{2}p = \frac{3}{2}$$

 $\frac{7}{2}p = \frac{3}{2} \hspace{1cm} \text{Rewrite each mixed number as an improper fraction.}$

$$\frac{2}{7}\!\!\left(\!\frac{7}{2}p\right) = \frac{2}{7}\!\!\left(\!\frac{3}{2}\right) \quad \text{Multiply each side by } \tfrac{2}{7}.$$

$$p = \frac{3}{7}$$

Simplify.

The solution is $\frac{3}{7}$.

Example 2 Solve $-\frac{1}{4}n = 16$.

$$-rac{1}{4}n=16$$
 Original equation

$$-4\Bigl(-rac{1}{4}n\Bigr)=\,-4(16)$$
 Multiply each side by -4 .

$$n = -64$$

Simplify.

The solution is -64.

Exercises

Solve each equation. Then check your solution.

1.
$$\frac{h}{3} = -2$$

2.
$$\frac{1}{8}m = 6$$

3.
$$\frac{1}{5}p = \frac{3}{5}$$

4.
$$5 = \frac{y}{12}$$

$$5. -\frac{1}{4}k = -2.5$$

6.
$$-\frac{m}{8} = \frac{5}{8}$$

7.
$$-1\frac{1}{2}h = 4$$

8.
$$-12 = -\frac{3}{2}k$$

9.
$$\frac{j}{3} = \frac{2}{5}$$

10.
$$-3\frac{1}{3}b = 5$$

11.
$$\frac{7}{10}m = 10$$

12.
$$\frac{p}{5} = -\frac{1}{4}$$

Write an equation for each problem. Then solve the equation.

- **13.** One-fifth of a number equals 25. Find the number.
- **14.** What number divided by 2 equals -18?
- **15.** A number divided by eight equals 3. Find the number.
- **16.** One and a half times a number equals 6. Find the number.

3-3 Study Guide and Intervention (continued)

Solving Equations by Using Multiplication and Division

Solve Using Division To solve equations with multiplication and division, you can also use the Division Property of Equality. If each side of an equation is divided by the same number, the resulting equation is true.

Division Property of Equality

For any numbers a, b, and c, with $c \neq 0$, if a = b, then $\frac{a}{c} = \frac{b}{c}$.

Example 1

Solve 8n = 64.

$$8n = 64$$
 Original equation

$$\frac{8n}{8} = \frac{64}{8}$$
 Divide each side by 8.

$$n=8$$
 Simplify.

The solution is 8.

Example 2

Solve -5n = 60.

$$-5n = 60$$

Original equation

$$\frac{-5n}{-5} = \frac{60}{-5}$$

Divide each side by -5.

$$n=-12$$
 Simplify.

The solution is -12.

Exercises

Solve each equation. Then check your solution.

1.
$$3h = -42$$

2.
$$8m = 16$$

$$3. -3t = 51$$

$$4. -3r = -24$$

5.
$$8k = -64$$

6.
$$-2m = 16$$

7.
$$12h = 4$$

8.
$$-2.4p = 7.2$$

9.
$$0.5i = 5$$

10.
$$-25 = 5m$$

11.
$$6m = 15$$

12.
$$-1.5p = -75$$

Write an equation for each problem. Then solve the equation.

13. Four times a number equals 64. Find the number.

14. What number multiplied by -4 equals -16?

15. A number times eight equals -36. Find the number.

Skills Practice

Solving Equations by Using Multiplication and Division

Solve each equation. Then check your solution.

1.
$$12z = 108$$

3.
$$18e = -216$$

5.
$$-6d = -42$$

7.
$$\frac{c}{4} = 16$$

9.
$$-84 = \frac{d}{3}$$

11.
$$\frac{t}{4} = -13$$

13.
$$-6 = \frac{2}{3}z$$

15.
$$\frac{5}{9}p = -10$$

$$17. -0.4b = 5.2$$

$$2. -7t = 49$$

$$4. -22 = 11v$$

6.
$$96 = -24a$$

$$8. \frac{a}{16} = 9$$

10.
$$-\frac{d}{7} = -13$$

12.
$$31 = -\frac{1}{6}n$$

14.
$$\frac{2}{7}q = -4$$

16.
$$\frac{a}{10} = \frac{2}{5}$$

18.
$$1.6m = -4$$

Write an equation for each problem. Then solve the equation.

19. The opposite of a number is -9. What is the number?

20. Fourteen times a number is -42. Find the number.

21. Eight times a number equals 128. What is the number?

22. Negative twelve times a number equals -132. Find the number.

23. Negative eighteen times a number is -54. What is the number?

24. One sixth of a number is -17. Find the number.

25. Negative three fifths of a number is -15. What is the number?

3-3 Practice

Solving Equations by Using Multiplication and Division

Solve each equation. Then check your solution.

1.
$$8j = 96$$

2.
$$-13z = -39$$

$$3. -180 = 15m$$

4.
$$243 = 27c$$

5.
$$\frac{y}{9} = -8$$

6.
$$-\frac{j}{12} = -8$$

7.
$$\frac{a}{15} = \frac{4}{5}$$

8.
$$\frac{g}{27} = \frac{2}{9}$$

9.
$$\frac{q}{24} = \frac{1}{6}$$

10.
$$-1 = -\frac{4}{7}t$$

11.
$$-\frac{3}{8}w = -9$$

12.
$$-\frac{3}{15}s = 4$$

13.
$$-3x = \frac{3}{2}$$

14.
$$\frac{8}{5}a = \frac{4}{3}$$

15.
$$\frac{5}{3}h = \frac{11}{6}$$

16.
$$5n = \frac{11}{4}$$

17.
$$2.5k = 20$$

18.
$$-3.4e = -3.74$$

19.
$$-1.7b = 2.21$$

20.
$$0.26p = 0.104$$

21.
$$4.2q = -3.36$$

Write an equation for each problem. Then solve the equation.

22. Negative nine times a number equals -117. Find the number.

23. Negative one eighth of a number is $-\frac{3}{4}$. What is the number?

24. Five sixths of a number is $-\frac{5}{9}$. Find the number.

25. 2.7 times a number equals 8.37. What is the number?

26. One and one fourth times a number is one and one third. What is the number?

27. PUBLISHING Two units of measure used in publishing are the pica and the point. A pica is one sixth of an inch. There are 12 points in a pica, so Points = $12 \cdot \text{Picas}$. How many picas are equivalent to 108 points?

ROLLER COASTERS For Exercises 28 and 29, use the following information.

Superman the Escape in California is the fastest roller coaster in the world. Riders fall 415 feet in 7 seconds. Speeds reach a maximum of 100 miles per hour.

28. If x represents the average rate of fall of the roller coaster, write an expression to represent the situation (*Hint*: Use the distance formula d = rt.)

29. What is the average rate that riders fall in feet per second?

Reading to Learn Mathematics

Solving Equations by Using Multiplication and Division

Pre-Activity How can equations be used to find how long it takes light to reach Earth?

Read the introduction to Lesson 3-3 at the top of page 135 in your textbook.

- In the equation d = rt, shown in the introduction, what number is used for r? for d?
- What equation could you use to find the time it takes light to reach Earth from the farthest star in the Big Dipper?

Reading the Lesson

Complete the sentence after each equation to tell how you would solve the equation.

1.
$$\frac{x}{7} = 16$$
 ______ each side by _____.

2.
$$5x = 125$$
 _____ each side by _____, or multiply each side by _____.

3.
$$-8k = 96$$
 Divide each side by _____, or multiply each side by _____

4. Explain how rewriting $4\frac{1}{3}x = 2\frac{1}{8}$ as $\frac{13}{3}x = \frac{17}{8}$ helps you solve the equation.

Helping You Remember

5. One way to remember something is to explain it to someone else. Write how you would explain to a classmate how to solve the equation $\frac{2}{3}x = 12$.

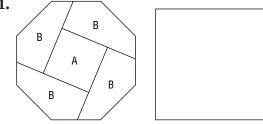
3-3 Enrichment

Dissection Puzzles: Make the Square

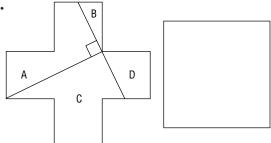
In a dissection puzzle, you are to cut apart one figure using only straight cuts and then rearrange the pieces to make a new figure. Usually the puzzle-solver must figure out where to make the given number of cuts. However, for these puzzles, the cut lines are shown. You must discover how to rearrange the pieces.

Cut apart each figure. Then rearrange the pieces to form a square.

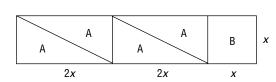
1.



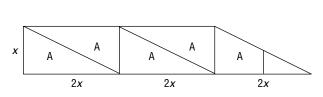
2.



3.



4. *Hint:* Cut one of the triangles into two pieces to make this square.





3-4

Study Guide and Intervention

Solving Multi-Step Equations

Work Backward Working backward is one of many problem-solving strategies that you can use to solve problems. To work backward, start with the result given at the end of a problem and undo each step to arrive at the beginning number.

by 2, and then 8 is subtracted from the quotient. The result is 16. What is the number?

Solve the problem by working backward.

The final number is 16. Undo subtracting 8 by adding 8 to get 24. To undo dividing 24 by 2, multiply 24 by 2 to get 48.

The original number is 48.

Example 2 A bacteria culture doubles each half hour. After 3 hours, there are 6400 bacteria. How many bacteria were there to begin with?

Solve the problem by working backward.

The bacteria have grown for 3 hours. Since there are 2 one-half hour periods in one hour, in 3 hours there are 6 one-half hour periods. Since the bacteria culture has grown for 6 time periods, it has doubled 6 times. Undo the doubling by halving the number of bacteria 6 times.

$$6,400 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = 6,400 \times \frac{1}{64}$$

$$= 100$$

There were 100 bacteria to begin with.

Exercises

Solve each problem by working backward.

- **1.** A number is divided by 3, and then 4 is added to the quotient. The result is 8. Find the number.
- **2.** A number is multiplied by 5, and then 3 is subtracted from the product. The result is 12. Find the number.
- **3.** Eight is subtracted from a number, and then the difference is multiplied by 2. The result is 24. Find the number.
- **4.** Three times a number plus 3 is 24. Find the number.
- **5. CAR RENTAL** Angela rented a car for \$29.99 a day plus a one-time insurance cost of \$5.00. Her bill was \$124.96. For how many days did she rent the car?
- **6. MONEY** Mike withdrew an amount of money from his bank account. He spent one fourth for gasoline and had \$90 left. How much money did he withdraw?
- **7. TELEVISIONS** In 1999, 68% of households with TV's subscribed to cable TV. If 8,000 more subscribers are added to the number of households with cable, the total number of households with cable TV would be 67,600,000. How many households were there with TV in 1999? **Source:** World Almanac

3-4

Study Guide and Intervention (continued)

Solving Multi-Step Equations

Solve Multi-Step Equations To solve equations with more than one operation, often called **multi-step equations**, undo operations by working backward. Reverse the usual order of operations as you work.

Example

Solve 5x + 3 = 23.

$$5x + 3 = 23$$

Original equation.

$$5x + 3 - 3 = 23 - 3$$

Subtract 3 from each side.

$$5x = 20$$

Simplify.

$$\frac{5x}{5} = \frac{20}{5}$$

Divide each side by 5.

$$x = 4$$

Simplify.

Exercises

Solve each equation. Then check your solution.

1.
$$5x + 2 = 27$$

2.
$$6x + 9 = 27$$

$$3.5x + 16 = 51$$

4.
$$14n - 8 = 34$$

5.
$$0.6x - 1.5 = 1.8$$

6.
$$\frac{7}{8}p - 4 = 10$$

7.
$$16 = \frac{d-12}{14}$$

8.
$$8 + \frac{3n}{12} = 13$$

9.
$$\frac{g}{-5} + 3 = -13$$

10.
$$\frac{4b+8}{-2}=10$$

11.
$$0.2x - 8 = -2$$

12.
$$3.2y - 1.8 = 3$$

13.
$$-4 = \frac{7x - (-1)}{-8}$$

14.
$$8 = -12 + \frac{k}{-4}$$

15.
$$0 = 10y - 40$$

Write an equation and solve each problem.

16. Find three consecutive integers whose sum is 96.

17. Find two consecutive odd integers whose sum is 176.

18. Find three consecutive integers whose sum is -93.

Salving Multi Stan Equation

Solving Multi-Step Equations

Solve each problem by working backward.

Skills Practice

1. A number is divided by 2, and then the quotient is added to 8. The result is 33. Find the number.

2. Two is subtracted from a number, and then the difference is divided by 3. The result is 30. Find the number.

3. A number is multiplied by 2, and then the product is added to 9. The result is 49. What is the number?

4. ALLOWANCE After Ricardo received his allowance for the week, he went to the mall with some friends. He spent half of his allowance on a new paperback book. Then he bought himself a snack for \$1.25. When he arrived home, he had \$5.00 left. How much was his allowance?

Solve each equation. Then check your solution.

5.
$$5x + 3 = 23$$

6.
$$4 = 3a - 14$$

7.
$$2y + 5 = 19$$

8.
$$6 + 5c = -29$$

9.
$$8-5w=-37$$

10.
$$18 - 4v = 42$$

11.
$$\frac{n}{3} - 8 = -2$$

12.
$$5 + \frac{x}{4} = 1$$

13.
$$-\frac{h}{3} - 4 = 13$$

14.
$$-\frac{d}{6} + 12 = -7$$

15.
$$\frac{a}{5} - 2 = 9$$

16.
$$\frac{w}{7} + 3 = -1$$

17.
$$\frac{3}{4}q - 7 = 8$$

18.
$$\frac{2}{3}g + 6 = -12$$

19.
$$\frac{5}{2}z - 8 = -3$$

20.
$$\frac{4}{5}m + 2 = 6$$

21.
$$\frac{c-5}{4}=3$$

22.
$$\frac{b+1}{3}=2$$

Write an equation and solve each problem.

23. Twice a number plus four equals 6. What is the number?

24. Sixteen is seven plus three times a number. Find the number.

25. Find two consecutive integers whose sum is 35.

26. Find three consecutive integers whose sum is 36.

3-4 Practice

Solving Multi-Step Equations

Solve each problem by working backward.

- 1. Three is added to a number, and then the sum is multiplied by 4. The result is 16. Find the number.
- **2.** A number is divided by 4, and the quotient is added to 3. The result is 24. What is the number?
- **3.** Two is subtracted from a number, and then the difference is multiplied by 5. The result is 30. Find the number.
- **4. BIRD WATCHING** While Michelle sat observing birds at a bird feeder, one fourth of the birds flew away when they were startled by a noise. Two birds left the feeder to go to another stationed a few feet away. Three more birds flew into the branches of a nearby tree. Four birds remained at the feeder. How many birds were at the feeder initially?

Solve each equation. Then check your solution.

5.
$$-12n - 19 = 77$$

6.
$$17 + 3f = 14$$

7.
$$15t + 4 = 49$$

8.
$$\frac{u}{5} + 6 = 2$$

9.
$$\frac{d}{-4} + 3 = 15$$

10.
$$\frac{b}{3} - 6 = -2$$

11.
$$\frac{1}{2}y - \frac{1}{8} = \frac{7}{8}$$

12.
$$-32 - \frac{3}{5}f = -17$$

13.
$$8 - \frac{3}{8}k = -4$$

14.
$$\frac{r+13}{12}=1$$

15.
$$\frac{15-a}{3}=-9$$

16.
$$\frac{3k-7}{5}=16$$

17.
$$\frac{x}{7} - 0.5 = 2.5$$

18.
$$2.5g + 0.45 = 0.95$$

19.
$$0.4m - 0.7 = 0.22$$

Write an equation and solve each problem.

- 20. Seven less than four times a number equals 13. What is the number?
- 21. Find two consecutive odd integers whose sum is 116.
- 22. Find two consecutive even integers whose sum is 126.
- 23. Find three consecutive odd integers whose sum is 117.
- **24. COIN COLLECTING** Jung has a total of 92 coins in his coin collection. This is 8 more than three times the number of quarters in the collection. How many quarters does Jung have in his collection?

3-4

Reading to Learn Mathematics

Solving Multi-Step Equations

Pre-Activity How can equations be used to estimate the age of an animal?

Read the introduction to Lesson 3-4 at the top of page 142 in your textbook.

- Write the equation 8 + 12a = 124 in words.
- How many operations are involved in the equation?

Reading the Lesson

- **1.** What does the phrase *undo the operations* mean to you? Give an example.
- **2. a.** If we undo operations in reverse of the order of operations, what operations do we do first?
 - **b.** What operations do we do last?
- **3.** Suppose you want to solve $\frac{x+3}{5} = 6$.
 - **a.** What is the grouping symbol in the equation $\frac{x+3}{5} = 6$?
 - **b.** What is the first step in solving the equation?
 - **c.** What is the next step in solving the equation?
- **4.** Write an equation for the problem below.

Seven	times	k	minus	five	equals	negative forty-seven

Helping You Remember

5. Explain why working backward is a useful strategy for solving equations.

3-4 Enrichment

Consecutive Integer Problems

Many types of problems and puzzles involve the idea of consecutive integers. Knowing how to represent these integers algebraically can help to solve the problem.

Example

Find four consecutive odd integers whose sum is -80.

An odd integer can be written as 2n + 1, where n is any integer.

If 2n + 1 is the first odd integer, then add 2 to get the next largest odd integer, and so on.

Now write an equation to solve this problem.

$$(2n + 1) + (2n + 3) + (2n + 5) + (2n + 7) = -80$$

Exercises

Write an equation for each problem. Then solve.

- 1. Complete the solution to the problem in the example.
- **2.** Find three consecutive even integers whose sum is 132.
- **3.** Find two consecutive integers whose sum is 19.
- **4.** Find two consecutive integers whose sum is 100.
- **5.** The lesser of two consecutive even integers is 10 more than one-half the greater. Find the integers.
- **6.** The greater of two consecutive even integers is 6 less than three times the lesser. Find the integers.
- **7.** Find four consecutive integers such that twice the sum of the two greater integers exceeds three times the first by 91.
- **8.** Find a set of four consecutive positive integers such that the greatest integer in the set is twice the least integer in the set.

3-5

NAME

Study Guide and Intervention

Solving Equations with the Variable on Each Side

Variables on Each Side To solve an equation with the same variable on each side, first use the Addition or the Subtraction Property of Equality to write an equivalent equation that has the variable on just one side of the equation. Then solve the equation.

Example 1

Solve 5v - 8 = 3v + 12.

$$5y - 8 = 3y + 12$$

$$5y - 8 - 3y = 3y + 12 - 3y$$

$$2y - 8 = 12$$

$$2y - 8 + 8 = 12 + 8$$

$$2y = 20$$

$$\frac{2y}{2} = \frac{20}{2}$$

$$y = 10$$

The solution is 10.

Example 2

Solve -11 - 3v = 8v + 1.

$$-11 - 3y = 8y + 1$$

$$-11 - 3y + 3y = 8y + 1 + 3y$$

$$-11 = 11y + 1$$

$$-11 - 1 = 11y + 1 - 1$$

$$-12 = 11y$$

$$\frac{-12}{11} = \frac{11y}{11}$$

$$-1\frac{1}{11} = y$$

The solution is $-1\frac{1}{11}$.

Exercises

1.
$$6 - b = 5b + 30$$

2.
$$5y - 2y = 3y + 2$$

$$3. 5x + 2 = 2x - 10$$

4.
$$4n - 8 = 3n + 2$$

5.
$$1.2x + 4.3 = 2.1 - x$$

6.
$$4.4s + 6.2 = 8.8s - 1.8$$

7.
$$\frac{1}{2}b + 4 = \frac{1}{8}b + 88$$

8.
$$\frac{3}{4}k - 5 = \frac{1}{4}k - 1$$

9.
$$8-5p=4p-1$$

10.
$$4b - 8 = 10 - 2b$$

11.
$$0.2x - 8 = -2 - x$$

12.
$$3y - 1.8 = 3y - 1.8$$

13.
$$-4 - 3x = 7x - 6$$

14.
$$8 + 4k = -10 + k$$

15.
$$20 - a = 10a - 2$$

16.
$$\frac{2}{3}n + 8 = \frac{1}{2}n + 2$$
 17. $\frac{2}{5}y - 8 = 9 - \frac{3}{5}y$

$$17. \frac{2}{5}y - 8 = 9 - \frac{3}{5}y$$

18.
$$-4r + 5 = 5 - 4r$$

19.
$$-4 - 3x = 6x - 6$$

20.
$$18 - 4k = -10 - 4k$$

21.
$$12 + 2y = 10y - 12$$

3-5 Study Guide and Intervention (continued)

Solving Equations with the Variable on Each Side

Grouping Symbols When solving equations that contain grouping symbols, first use the Distributive Property to eliminate grouping symbols. Then solve.

Example Solve 4(2a - 1) = -10(a - 5).

Solve
$$4(2a-1) = -10(a-5)$$

$$4(2a - 1) = -10(a - 5)$$

Original equation

$$8a - 4 = -10a + 50$$

Distributive Property

$$8a - 4 + 10a = -10a + 50 + 10a$$

Add 10a to each side.

$$18a-4=50$$

Simplify.

$$18a - 4 + 4 = 50 + 4$$
$$18a = 54$$

Add 4 to each side.

Simplify.

$$\overline{18} = \overline{18}$$
 $a = 3$

Divide each side by 18.

The solution is 3.

Exercises

1.
$$-3(x + 5) = 3(x - 1)$$

2.
$$2(7 + 3t) = -t$$

3.
$$3(a + 1) - 5 = 3a - 2$$

4.
$$75 - 9g = 5(-4 + 2g)$$

5.
$$5(f+2) = 2(3-f)$$

6.
$$4(p + 3) = 36$$

7.
$$18 = 3(2c + 2)$$

8.
$$3(d-8)=3d$$

9.
$$5(p+3)+9=3(p-2)+6$$

10.
$$4(b-2) = 2(5-b)$$

11.
$$1.2(x-2) = 2 - x$$

12.
$$\frac{3+y}{4} = \frac{-y}{8}$$

13.
$$\frac{a-8}{12} = \frac{2a+5}{3}$$

14.
$$2(4+2k)+10=k$$

15.
$$2(w-1)+4=4(w+1)$$

16.
$$6(n-1) = 2(2n+4)$$

17.
$$2[2 + 3(y - 1)] = 22$$

18.
$$-4(r+2) = 4(2-4r)$$

19.
$$-3(x - 8) = 24$$

20.
$$4(4-4k) = -10-16k$$

21.
$$6(2-2y)=5(2y-2)$$

3-5 **Skills Practice**

Solving Equations with the Variable on Each Side

Justify each step.

1.
$$4k - 3 = 2k + 5$$

 $4k - 3 - 2k = 2k + 5 - 2k$

$$2k - 3 = 5$$

$$2k - 3 + 3 = 5 + 3$$

$$0 + 0 - 0 +$$

$$2k = 8$$

$$\frac{2k}{2} = \frac{8}{2}$$

$$k = 4$$

2.
$$2(8u + 2) = 3(2u - 7)$$

 $16u + 4 = 6u - 21$

$$16u + 4 - 6u = 6u - 21 - 6u$$

$$10u + 4 = -21$$

$$10u + 4 - 4 = -21 - 4$$

$$0u + 4 - 4 = -21 - 4$$

$$10u = -25$$

$$\frac{10u}{10} = \frac{-25}{10}$$

$$u = -9$$

$$3.2m + 12 = 3m - 31$$

4.
$$2h - 8 = h + 17$$

5.
$$7a - 3 = 3 - 2a$$

6.
$$4n - 12 = 12 - 4n$$

7.
$$4x - 9 = 7x + 12$$

$$8. -6y - 3 = 3 - 6y$$

9.
$$5 + 3r = 5r - 19$$

10.
$$-9 + 8k = 7 + 4k$$

11.
$$8q + 12 = 4(3 + 2q)$$

12.
$$3(5j + 2) = 2(3j - 6)$$

13.
$$6(-3v + 1) = 5(-2v - 2)$$

14.
$$-7(2b-4) = 5(-2b+6)$$

15.
$$3(8-3t)=5(2+t)$$

16.
$$2(3u + 7) = -4(3 - 2u)$$

17.
$$8(2f-2) = 7(3f+2)$$

18.
$$5(-6 - 3d) = 3(8 + 7d)$$

19.
$$6(w-1) = 3(3w+5)$$

20.
$$7(-3y + 2) = 8(3y - 2)$$

21.
$$\frac{2}{3}v - 6 = 6 - \frac{2}{3}v$$

22.
$$\frac{1}{2} - \frac{5}{8}x = \frac{7}{8}x + \frac{7}{2}$$

3-5 Practice

Solving Equations with the Variable on Each Side

1.
$$5x - 3 = 13 - 3x$$

3.
$$1 - s = 6 - 6s$$

5.
$$\frac{1}{2}k - 3 = 2 - \frac{3}{4}k$$

7.
$$3(-2-3x)=-9x-4$$

9.
$$9(4b-1)=2(9b+3)$$

11.
$$-5x - 10 = 2 - (x + 4)$$

13.
$$\frac{5}{2}t - t = 3 + \frac{3}{2}t$$

15.
$$\frac{2}{3}x - \frac{1}{6} = \frac{1}{2}x + \frac{5}{6}$$

17.
$$\frac{1}{2}(3g-2) = \frac{g}{6}$$

19.
$$\frac{1}{4}(5-2h)=\frac{h}{2}$$

21.
$$3(d-8)-5=9(d+2)+1$$

2.
$$-4c - 11 = 4c + 21$$

4.
$$14 + 5n = -4n + 17$$

6.
$$\frac{1}{2}(6-z)=z$$

8.
$$4(4-w) = 3(2w+2)$$

10.
$$3(6 + 5y) = 2(-5 + 4y)$$

12.
$$6 + 2(3j - 2) = 4(1 + j)$$

14.
$$1.4f + 1.1 = 8.3 - f$$

16.
$$2 - \frac{3}{4}z = \frac{1}{8}z + 9$$

18.
$$\frac{1}{3}(c+1) = \frac{1}{6}(3c-5)$$

20.
$$\frac{1}{9}(2m-16) = \frac{1}{3}(2m+4)$$

22.
$$2(a-8)+7=5(a+2)-3a-19$$

- **23.** Two thirds of a number reduced by 11 is equal to 4 more than the number. Find the number.
- **24.** Five times the sum of a number and 3 is the same as 3 multiplied by 1 less than twice the number. What is the number?
- **25. NUMBER THEORY** Tripling the greater of two consecutive even integers gives the same result as subtracting 10 from the lesser even integer. What are the integers?
- **26. GEOMETRY** The formula for the perimeter of a rectangle is $P = 2\ell + 2w$, where ℓ is the length and w is the width. A rectangle has a perimeter of 24 inches. Find its dimensions if its length is 3 inches greater than its width.

Reading to Learn Mathematics

Solving Equations with the Variable on Each Side

Pre-Activity How can an equation be used to determine when two populations are equal?

Read the introduction to Lesson 3-5 at the top of page 149 in your textbook.

In the equation 12 + 7.6x = 6 + 8x, what do 7.6x and 8x represent?

Reading the Lesson

- **1.** Suppose you want to help a friend solve 6k + 7 = 3k 8. What would you advise her to do first? Why?
- **2.** When solving 2(3x 4) = 3(x + 5), why is it helpful first to use the Distributive Property to remove the grouping symbols?
- **3.** On a quiz, Jason solved three equations. His teacher said all the work was correct, but she asked him to write short sentences to tell what the solutions were. In what follows, you see the *last* equation in his work for each equation. Write sentences to describe the solutions.

a.
$$x = -4$$

b.
$$6m = 6m$$

c.
$$12 = 37$$

4. In Question 3, one of the equations Jason solved was an identity. Which equation was it? Explain how you know.

Helping You Remember

5. An equation with variables is an identity when the equation is always true. In other words, the expressions on the left and right sides always have the same value. Look up the word *identity* in the dictionary. Write all the definitions that are similar to the mathematical definition.

Enrichment

Identities

An equation that is true for every value of the variable is called an identity. When you try to solve an identity, you end up with a statement that is always true. Here is an example.

Example

Solve
$$8 - (5 - 6x) = 3(1 + 2x)$$
.

$$8 - (5 - 6x) = 3(1 + 2x)$$

$$8 - 5 - (-6x) = 3(1 + 2x)$$

$$8 - 5 + 6x = 3 + 6x$$

$$3+6x=3+6x$$

Exercises

State whether each equation is an identity. If it is not, find its solution.

1.
$$2(2-3x)=3(3+x)+4$$

2.
$$5(m+1)+6=3(4+m)+(2m-1)$$

3.
$$(5t + 9) - (3t - 13) = 2(11 + t)$$

4.
$$14 - (6 - 3c) = 4c - c$$

5.
$$3y - 2(y + 19) = 9y - 3(9 - y)$$
 6. $3(3h - 1) = 4(h + 3)$

6.
$$3(3h-1)=4(h+3)$$

7. Use the true equation 3x - 2 = 3x - 2 to create an identity of your own.

8. Use the false equation 1 = 2 to create an equation with no solution.

9. Create an equation whose solution is x = 3.

Lesson 3-6

3-6

Study Guide and Intervention

Ratios and Proportions

Ratios and Proportions A **ratio** is a comparison of two numbers by division. The ratio of x to y can be expressed as x to y, x:y or $\frac{x}{y}$. Ratios are usually expressed in simplest form. An equation stating that two ratios are equal is called a **proportion**. To determine whether two ratios form a proportion, express both ratios in simplest form or check cross products.

Example 1 Determine whether the ratios $\frac{24}{36}$ and $\frac{12}{18}$ form a proportion.

$$\frac{24}{36} = \frac{2}{3}$$
 when expressed in simplest form.

$$\frac{12}{18} = \frac{2}{3}$$
 when expressed in simplest form.

The ratios $\frac{24}{36}$ and $\frac{12}{18}$ form a proportion because they are equal when expressed in simplest form.

Example 2 Use cross products to determine whether $\frac{10}{18}$ and $\frac{25}{45}$ form a proportion.

$$\frac{10}{18} \stackrel{?}{=} \frac{25}{45}$$

Write the proportion.

$$10(45) \stackrel{?}{=} 18(25)$$
$$450 = 450$$

Simplify.

Cross products

The cross products are equal, so
$$\frac{10}{18} = \frac{25}{45}$$
.

Since the ratios are equal, they form a proportion.

Exercises

Use cross products to determine whether each pair of ratios forms a proportion.

1.
$$\frac{1}{2}$$
, $\frac{16}{32}$

2.
$$\frac{5}{8}$$
, $\frac{10}{15}$

3.
$$\frac{10}{20}$$
, $\frac{25}{49}$

4.
$$\frac{25}{36}$$
, $\frac{15}{20}$

5.
$$\frac{12}{32}$$
, $\frac{3}{16}$

6.
$$\frac{4}{9}$$
, $\frac{12}{27}$

7.
$$\frac{0.1}{2}$$
, $\frac{5}{100}$

8.
$$\frac{15}{20}$$
, $\frac{9}{12}$

9.
$$\frac{14}{21}$$
, $\frac{20}{30}$

12.
$$\frac{72}{64}$$
, $\frac{9}{8}$

16.
$$\frac{0.05}{1}$$
, $\frac{1}{20}$

17.
$$\frac{1.5}{2}$$
, $\frac{6}{8}$

18.
$$\frac{0.1}{0.2}$$
, $\frac{0.45}{0.9}$

Study Guide and Intervention (continued) Ratios and Proportions

Solve Proportions If a proportion involves a variable, you can use cross products to solve the proportion. In the proportion $\frac{x}{5} = \frac{10}{13}$, x and 13 are called **extremes** and 5 and 10 are called **means**. In a proportion, the product of the extremes is equal to the product of the means.

Means-Extremes Property of Proportions

For any numbers a, b, c, and d, if $\frac{a}{b} = \frac{c}{d}$, then ad = bc.

Example

Solve
$$\frac{x}{5} = \frac{10}{13}$$
.

$$\frac{x}{5} = \frac{10}{13}$$

Original proportion

$$13(x)=5(10)$$

Cross products

$$13x = 50$$

Simplify.

$$\frac{13x}{13} = \frac{50}{13}$$

Divide each side by 13.

$$x = 3\frac{11}{12}$$

Simplify.

The solution is $3\frac{11}{13}$.

Exercises

Solve each proportion.

1.
$$\frac{-3}{r} = \frac{2}{8}$$

2.
$$\frac{1}{t} = \frac{5}{3}$$

3.
$$\frac{0.1}{2} = \frac{0.5}{r}$$

$$4. \frac{x+1}{4} = \frac{3}{4}$$

5.
$$\frac{4}{6} = \frac{8}{r}$$

6.
$$\frac{x}{21} = \frac{3}{63}$$

7.
$$\frac{9}{y+1} = \frac{18}{54}$$

8.
$$\frac{3}{d} = \frac{18}{3}$$

9.
$$\frac{5}{8} = \frac{p}{24}$$

10.
$$\frac{4}{b-2} = \frac{4}{12}$$

11.
$$\frac{1.5}{x} = \frac{12}{x}$$

12.
$$\frac{3+y}{4} = \frac{-y}{8}$$

13.
$$\frac{a-8}{12} = \frac{15}{3}$$

14.
$$\frac{12}{k} = \frac{24}{k}$$

15.
$$\frac{2+w}{6}=\frac{12}{9}$$

Use a proportion to solve each problem.

- **16. MODELS** To make a model of the Guadeloupe River bed, Hermie used 1 inch of clay for 5 miles of the river's actual length. His model river was 50 inches long. How long is the Guadeloupe River?
- **17. EDUCATION** Josh finished 24 math problems in one hour. At that rate, how many hours will it take him to complete 72 problems?

Skills Practice 3-6

Ratios and Proportions

Use cross products to determine whether each pair of ratios forms a proportion. Write yes or no.

1.
$$\frac{4}{5}$$
, $\frac{20}{25}$

2.
$$\frac{5}{9}$$
, $\frac{7}{11}$

3.
$$\frac{6}{7}$$
, $\frac{24}{28}$

4.
$$\frac{8}{9}$$
, $\frac{72}{81}$

5.
$$\frac{7}{16}$$
, $\frac{42}{90}$

6.
$$\frac{13}{19}$$
, $\frac{26}{38}$

7.
$$\frac{3}{14}$$
, $\frac{21}{98}$

8.
$$\frac{12}{17}$$
, $\frac{50}{85}$

Solve each proportion. If necessary, round to the nearest hundredth.

9.
$$\frac{1}{a} = \frac{2}{14}$$

10.
$$\frac{5}{b} = \frac{3}{9}$$

11.
$$\frac{9}{g} = \frac{15}{10}$$

12.
$$\frac{3}{a} = \frac{1}{6}$$

13.
$$\frac{6}{7} = \frac{3}{5}$$

14.
$$\frac{5}{e} = \frac{35}{21}$$

15.
$$\frac{12}{7} = \frac{36}{8}$$

16.
$$\frac{6}{23} = \frac{y}{69}$$

17.
$$\frac{42}{56} = \frac{6}{f}$$

18.
$$\frac{7}{h} = \frac{1}{9}$$

19.
$$\frac{10}{14} = \frac{30}{m}$$

20.
$$\frac{11}{15} = \frac{n}{60}$$

21.
$$\frac{9}{c} = \frac{27}{39}$$

22.
$$\frac{5}{12} = \frac{20}{g}$$

23.
$$\frac{4}{21} = \frac{s}{84}$$

24.
$$\frac{22}{x} = \frac{11}{30}$$

25. BOATING Hue's boat used 5 gallons of gasoline in 4 hours. At this rate, how many gallons of gasoline will the boat use in 10 hours?

3-6 Practice

Ratios and Proportions

Use cross products to determine whether each pair of ratios forms a proportion. Write yes or no.

1.
$$\frac{7}{6}$$
, $\frac{52}{48}$

2.
$$\frac{3}{11}$$
, $\frac{15}{66}$

3.
$$\frac{18}{24}$$
, $\frac{36}{48}$

4.
$$\frac{12}{11}$$
, $\frac{108}{99}$

5.
$$\frac{8}{9}$$
, $\frac{72}{81}$

6.
$$\frac{1.5}{9}$$
, $\frac{1}{6}$

7.
$$\frac{3.4}{5.2}$$
, $\frac{7.14}{10.92}$

8.
$$\frac{1.7}{1.2}$$
, $\frac{2.9}{2.4}$

9.
$$\frac{7.6}{1.8}$$
, $\frac{3.9}{0.9}$

Solve each proportion. If necessary, round to the nearest hundredth.

10.
$$\frac{5}{a} = \frac{30}{54}$$

11.
$$\frac{v}{46} = \frac{34}{23}$$

12.
$$\frac{40}{56} = \frac{k}{7}$$

13.
$$\frac{28}{49} = \frac{4}{w}$$

14.
$$\frac{3}{u} = \frac{27}{162}$$

15.
$$\frac{y}{3} = \frac{48}{9}$$

16.
$$\frac{2}{v} = \frac{10}{60}$$

17.
$$\frac{5}{11} = \frac{35}{x}$$

18.
$$\frac{3}{51} = \frac{z}{17}$$

19.
$$\frac{6}{61} = \frac{12}{h}$$

20.
$$\frac{g}{16} = \frac{6}{4}$$

21.
$$\frac{14}{49} = \frac{2}{a}$$

22.
$$\frac{7}{9} = \frac{8}{c}$$

23.
$$\frac{3}{q} = \frac{5}{6}$$

24.
$$\frac{m}{6} = \frac{5}{8}$$

25.
$$\frac{v}{0.23} = \frac{7}{1.61}$$

26.
$$\frac{3}{0.72} = \frac{12}{b}$$

27.
$$\frac{6}{n} = \frac{3}{0.51}$$

28.
$$\frac{7}{a-4} = \frac{14}{6}$$

29.
$$\frac{3}{12} = \frac{2}{y+6}$$

30.
$$\frac{m-1}{8}=\frac{2}{4}$$

$$31. \frac{5}{12} = \frac{x+1}{4}$$

32.
$$\frac{r+2}{7}=\frac{5}{7}$$

33.
$$\frac{3}{7} = \frac{x-2}{6}$$

- **34. PAINTING** Ysidra paints a room that has 400 square feet of wall space in $2\frac{1}{2}$ hours. At this rate, how long will it take her to paint a room that has 720 square feet of wall space?
- **35. VACATION PLANS** Walker is planning a summer vacation. He wants to visit Petrified National Forest and Meteor Crater, Arizona, the 50,000-year-old impact site of a large meteor. On a map with a scale where 2 inches equals 75 miles, the two areas are about $1\frac{1}{2}$ inches apart. What is the distance between Petrified National Forest and Meteor Crater?

Reading to Learn Mathematics

Ratios and Proportions

Pre-Activity How are ratios used in recipes?

Read the introduction to Lesson 3-6 at the top of page 155 in your textbook.

- How many servings of honey frozen yogurt are made by this recipe?
- How many recipes would be needed to make enough honey frozen yogurt for all the students in your class?

Reading the Lesson

1. Complete the following sentence.

A ratio is a comparison of two numbers by _____

- **2.** Describe two ways to decide whether the sentence $\frac{2}{5} = \frac{8}{20}$ is a proportion.
- **3.** For each proportion, tell what the extremes are and what the means are.

a.
$$\frac{14}{35} = \frac{6}{15}$$

Extremes:

Means:

b.
$$\frac{6}{8} = \frac{12}{16}$$

b. $\frac{6}{8} = \frac{12}{16}$ Extremes: ______ Means: _____

4. A jet flying at a steady speed traveled 825 miles in 2 hours. If you solved the proportion $\frac{825}{2} = \frac{x}{1.5}$, what would the answer tell you about the jet?

Helping You Remember

5. Write how you would explain solving a proportion to a friend who missed Lesson 3-6.

3-6 Enrichment

Angles of a Triangle

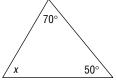
In geometry, many statements about physical space are proven to be true. Such statements are called **theorems**. Here are two examples of geometric theorems.

a. The sum of the measures of the angles of a triangle is 180°.

b. If two sides of a triangle have equal measure, then the two angles opposite those sides also have equal measure.

For each of the triangles, write an equation and then solve for x. (A tick mark on two or more sides of a triangle indicates that the sides have equal measure.)

1.



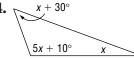
2.



3.



4.



5.



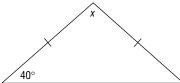
6.



7.



8.



9.



10.



- 11. Two angles of a triangle have the same measure. The sum of the measures of these angles is one-half the measure of the third angle. Find the measures of the angles of the triangle.
- 12. The measure of one angle of a triangle is twice the measure of a second angle. The measure of the third angle is 12 less than the sum of the other two. Find the measures of the angles of the triangle.

Study Guide and Intervention

Percent of Change

Percent of Change When an increase or decrease in an amount is expressed as a percent, the percent is called the **percent of change**. If the new number is greater than the original number, the percent of change is a **percent of increase**. If the new number is less than the original number, the percent of change is the **percent of decrease**.

Example 1

Find the percent of increase. original: 48 new: 60

First, subtract to find the amount of increase. The amount of increase is 60 - 48 = 12.

Then find the percent of increase by using the original number, 48, as the base.

$$\frac{12}{48} = \frac{r}{100} \qquad \text{Percent proportion}$$

$$12(100) = 48(r) \qquad \text{Cross products}$$

$$1200 = 48r \qquad \text{Simplify.}$$

$$\frac{1200}{48} = \frac{48r}{48} \qquad \text{Divide each side by 48.}$$

$$25 = r \qquad \text{Simplify.}$$

The percent of increase is 25%.

Example 2

Find the percent of decrease. original: 30 new: 22

First, subtract to find the amount of decrease. The amount of decrease is 30 - 22 = 8.

Then find the percent of decrease by using the original number, 30, as the base.

$$\frac{8}{30} = \frac{r}{100} \qquad \text{Percent proportion}$$

$$8(100) = 30(r) \qquad \text{Cross products}$$

$$800 = 30r \qquad \text{Simplify.}$$

$$\frac{800}{30} = \frac{30r}{30} \qquad \text{Divide each side by 30.}$$

$$26\frac{2}{3} = r \qquad \text{Simplify.}$$

The percent of decrease is $26\frac{2}{3}\%$, or about

Exercises

State whether each percent of change is a percent of increase or a percent of decrease. Then find each percent of change. Round to the nearest whole percent.

1. original: 50 new: 80

2. original: 90 new: 100

3. original: 45 new: 20

4. original: 77.5 new: 62

5. original: 140 new: 150

6. original: 135 new: 90

7. original: 120 new: 180

8. original: 90 new: 270

9. original: 27.5 new: 25

10. original: 84 new: 98

- **11.** original: 12.5 new: 10
- **12.** original: 250 new: 500

3-7

Study Guide and Intervention (continued)

Percent of Change

Solve Problems Discounted prices and prices including tax are applications of percent of change. Discount is the amount by which the regular price of an item is reduced. Thus, the discounted price is an example of percent of decrease. Sales tax is amount that is added to the cost of an item, so the price including tax is an example of percent of increase.

A coat is on sale for 25% off the original price. If the original price of the coat is \$75, what is the discounted price?

The discount is 25% of the original price.

$$25\% \text{ of } \$75 = 0.25 \times 75$$
 $25\% = 0.25$ $= 18.75$ Use a calculator.

Subtract \$18.75 from the original price.

$$$75 - $18.75 = $56.25$$

The discounted price of the coat is \$56.25.

Exercises

Find the final price of each item. When a discount and a sales tax are listed, compute the discount price before computing the tax.

1. Compact disc: \$16 Discount: 15% **2.** Two concert tickets: \$28 Student discount: 28%

3. Airline ticket: \$248.00 Superair discount: 33%

4. Shirt: \$24.00 Sales tax: 4%

5. CD player: \$142.00 Sales tax: 5.5%

6. Celebrity calendar: \$10.95 Sales tax: 7.5%

7. Class ring: \$89.00 Group discount: 17% Sales tax: 5%

8. Software: \$44.00 Discount: 21% Sales tax: 6% 9. Video recorder: \$110.95 Discount: 20%

Sales tax: 5%

- **10. VIDEOS** The original selling price of a new sports video was \$65.00. Due to the demand the price was increased to \$87.75. What was the percent of increase over the original price?
- **11. SCHOOL** A high school paper increased its sales by 75% when it ran an issue featuring a contest to win a class party. Before the contest issue, 10% of the school's 800 students bought the paper. How many students bought the contest issue?
- **12. BASEBALL** Baseball tickets cost \$15 for general admission or \$20 for box seats. The sales tax on each ticket is 8%, and the municipal tax on each ticket is an additional 10% of the base price. What is the final cost of each type of ticket?

Skills Practice

Percent of Change

State whether each percent of change is a percent of increase or a percent of decrease. Then find each percent of change. Round to the nearest whole percent.

1. original: 25 new: 10

2. original: 50 new: 75

3. original: 55 new: 50

4. original: 25 new: 28

5. original: 50 new: 30

6. original: 90 new: 95

7. original: 48 new: 60

8. original: 60 new: 45

Find the total price of each item.

9. dress: \$69.00 tax: 5%

10. binder: \$14.50 tax: 7%

11. hardcover book: \$28.95 tax: 6%

12. groceries: \$47.52 tax: 3%

13. filler paper: \$6.00

14. shoes: \$65.00 tax: 4%

tax: 6.5%

16. concert tickets: \$48.00

15. basketball: \$17.00

tax: 7.5%

tax: 6%

Find the discounted price of each item.

17. backpack: \$56.25 discount: 20%

18. monitor: \$150.00 discount: 50%

19. CD: \$15.99 discount: 20% **20.** shirt: \$25.50 discount: 40%

21. sleeping bag: \$125 discount: 25%

- **22.** coffee maker: \$102.00
 - discount: 45%

3-7

Practice

Percent of Change

State whether each percent of change is a percent of increase or a percent of decrease. Then find each percent of change. Round to the nearest whole percent.

1. original: 18 new: 10

2. original: 140 new: 160

3. original: 200 new: 320

4. original: 10 new: 25

5. original: 76 new: 60

6. original: 128 new: 120

7. original: 15 new: 35.5

- 8. original: 98.6 new: 64
- **9.** original: 58.8 new: 65.7

Find the total price of each item.

- **10.** concrete blocks: \$95.00 tax: 6%
- **11.** crib: \$240.00 tax: 6.5%
- **12.** jacket: \$125.00 tax: 5.5%

- **13.** class ring: \$325.00 tax: 6%
- **14.** blanket: \$24.99 tax: 7%
- **15.** kite: \$18.90 tax: 5%

Find the discounted price of each item.

- **16.** dry cleaning: \$25.00 discount: 15%
- **17.** computer game: \$49.99 discount: 25%
- **18.** luggage: \$185.00 discount: 30%

- **19.** stationery: \$12.95 discount: 10%
- **20.** prescription glasses: \$149 discount: 20%
- **21.** pair of shorts: \$24.99 discount: 45%

Find the final price of each item.

- **22.** television: \$375.00 discount: 25% tax: 6%
- **23.** DVD player: \$269.00 discount: 20% tax: 7%
- **24.** printer: \$255.00 discount: 30% tax: 5.5%
- **25. INVESTMENTS** The price per share of an internet-related stock decreased from \$90 per share to \$36 per share early in 2001. By what percent did the price of the stock decrease?
- **26. HEATING COSTS** Customers of a utility company received notices in their monthly bills that heating costs for the average customer had increased 125% over last year because of an unusually severe winter. In January of last year, the Garcia's paid \$120 for heating. What should they expect to pay this January if their bill increased by 125%?

Reading to Learn Mathematics

Percent of Change

Pre-Activity How can percents describe growth over time?

Read the introduction to Lesson 3-7 at the top of page 160 in your textbook.

- How many area codes were in use in 1947?
- How many *more* area codes were in use in 1999?

Reading the Lesson

- 1. If you use (original amount) (new amount) to find the change for a percent of change problem, then the problem involves a percent of _ (increase/decrease).
- 2. If you use (new amount) (original amount) to find the change for a percent of change problem, then the problem involves a percent of (increase/decrease).

Complete the chart.

	Original Amount	New Amount	Percent Proportion	Percent Increase or Percent Decrease?
3.	10	13		
4.	10	7		
5.	50	42		
6.	50	58		

7. When you find a discount price, do you add to or subtract from the original price?

Helping You Remember

8. If you remember only two things about the ratio used for finding percent of change, what should they be?

3-7 Enrichment

Using Percent

Use what you have learned about percent to solve each problem.

A TV movie had a "rating" of 15 and a 25 "share." The rating is the percentage of the nation's total TV households that were tuned in to this show. The share is the percentage of homes with TVs turned on that were tuned to the movie. How many TV households had their TVs turned off at this time?

To find out, let T = the number of TV households

and x = the number of TV households with the TV off.

Then T - x = the number of TV households with the TV on.

Since 0.15T and 0.25(T-x) both represent the number of households tuned to the movie,

$$0.15T = 0.25(T - x)$$

$$0.15T = 0.25T - 0.25x.$$

Solve for *x*. 0.25x = 0.10T

$$x = \frac{0.10T}{0.25} = 0.40T$$

Forty percent of the TV households had their TVs off when the movie was aired.

Answer each question.

- **1.** During that same week, a sports broadcast had a rating of 22.1 and a 43 share. Show that the percent of TV households with their TVs off was about 48.6%.
- **2.** Find the percent of TV households with their TVs turned off during a show with a rating of 18.9 and a 29 share.
- **3.** Show that if T is the number of TV households, r is the rating, and s is the share, then the number of TV households with the TV off is $\frac{(s-r)T}{s}$.
- **4.** If the fraction of TV households with no TV on is $\frac{s-r}{s}$ then show that the fraction of TV households with TVs on is $\frac{r}{s}$.
- **5.** Find the percent of TV households with TVs on during the most watched serial program in history: the last episode of M*A*S*H, which had a 60.3 rating and a 77 share.
- **6.** A local station now has a 2 share. Each share is worth \$50,000 in advertising revenue per month. The station is thinking of going commercial free for the three months of summer to gain more listeners. What would its new share have to be for the last 4 months of the year to make more money for the year than it would have made had it not gone commercial free?

3-8

Solving Equations and Formulas

Solve for Variables Sometimes you may want to solve an equation such as $V = \ell w h$ for one of its variables. For example, if you know the values of V, w, and h, then the equation $\ell = \frac{V}{wh}$ is more useful for finding the value of ℓ . If an equation that contains more than one variable is to be solved for a specific variable, use the properties of equality to isolate the specified variable on one side of the equation.

Example 1

Solve 2x - 4y = 8 for y.

$$2x - 4y = 8$$

$$2x - 4y - 2x = 8 - 2x$$

$$-4y = 8 - 2x$$

$$\frac{-4y}{-4} = \frac{8 - 2x}{-4}$$

$$y = \frac{8 - 2x}{-4} \text{ or } \frac{2x - 8}{4}$$

The value of *y* is $\frac{2x-8}{4}$.

Example 2

Solve 3m - n = km - 8 for m.

$$3m - n = km - 8$$

$$3m - n - km = km - 8 - km$$

$$3m - n - km = -8$$

$$3m - n - km + n = -8 + n$$

$$3m - km = -8 + n$$

$$m(3 - k) = -8 + n$$

$$\frac{m(3 - k)}{3 - k} = \frac{-8 + n}{3 - k}$$

$$m = \frac{-8 + n}{3 - k}, \text{ or } \frac{n - 8}{3 - k}$$

The value of m is $\frac{n-8}{3-k}$. Since division by 0 is undefined, $3-k \neq 0$, or $k \neq 3$.

Exercises

Solve each equation or formula for the variable specified.

$$1. ax - b = c \text{ for } x$$

2.
$$15x + 1 = y$$
 for x

3.
$$(x + f) + 2 = j$$
 for x

4.
$$xy + z = 9$$
 for y

5.
$$x(4-k) = p \text{ for } k$$

6.
$$7x + 3y = m \text{ for } y$$

7.
$$4(c + 3) = t$$
 for c

$$8.\ 2x + b = c \text{ for } x$$

9.
$$x(1 + y) = z$$
 for x

10.
$$16z + 4x = y$$
 for x

11.
$$d = rt$$
 for r

12.
$$A = \frac{h(a+b)}{2}$$
 for h

13.
$$C = \frac{5}{9}(F - 32)$$
 for F

14.
$$P = 2\ell + 2w$$
 for w

15.
$$A = \ell w$$
 for ℓ

-8 Study Guide and Intervention (continued)

Solving Equations and Formulas

Use Formulas Many real-world problems require the use of formulas. Sometimes solving a formula for a specified variable will help solve the problem.

The formula $C = \pi d$ represents the circumference of a circle, or the distance around the circle, where d is the diameter. If an airplane could fly around Earth at the equator without stopping, it would have traveled about 24,900 miles. Find the diameter of Earth.

$$C=\pi d$$
 Given formula $d=\frac{C}{\pi}$ Solve for d . $d=\frac{24,900}{3.14}$ Use $\pi=3.14$. $dpprox 7930$ Simplify.

The diameter of Earth is about 7930 miles.

Exercises

- **1. GEOMETRY** The volume of a cylinder V is given by the formula $V = \pi r^2 h$, where r is the radius and h is the height.
 - **a.** Solve the formula for h.
 - **b.** Find the height of a cylinder with volume 2500π feet and radius 10 feet.
- **2. WATER PRESSURE** The water pressure on a submerged object is given by P = 64d, where P is the pressure in pounds per square foot, and d is the depth of the object in feet.
 - **a.** Solve the formula for d.
 - **b.** Find the depth of a submerged object if the pressure is 672 pounds per square foot.
- **3. GRAPHS** The equation of a line containing the points (a, 0) and (0, b) is given by the formula $\frac{x}{a} + \frac{y}{b} = 1$.
 - **a.** Solve the equation for y.
 - **b.** Suppose the line contains the points (4, 0), and (0, -2). If x = 3, find y.
- **4. GEOMETRY** The surface area of a rectangular solid is given by the formula $S = 2\ell w + 2\ell h + 2wh$, where $\ell = \text{length}$, w = width, and h = height.
 - **a.** Solve the formula for h.
 - **b.** The surface area of a rectangular solid with length 6 centimeters and width 3 centimeters is 72 square centimeters. Find the height.

Skills Practice 3-8

Solving Equations and Formulas

Solve each equation or formula for the variable specified.

1.
$$7t = x$$
, for t

2.
$$e = wp$$
, for p

3.
$$q - r = r$$
, for r

4.
$$4m - n = m$$
, for m

5.
$$7a - b = 15a$$
, for a

6.
$$-5c + d = 2c$$
, for c

7.
$$x - 2y = 1$$
, for y

8.
$$m + 3n = 1$$
, for n

9.
$$7f + g = 5$$
, for f

10.
$$ax - c = b$$
, for x

11.
$$rt - 2n = y$$
, for t

12.
$$bc + 3g = 2k$$
, for c

13.
$$kn + 4f = 9v$$
, for n

14.
$$8c + 6j = 5p$$
, for c

15.
$$\frac{x-c}{2} = d$$
, for x

16.
$$\frac{x-c}{2} = d$$
, for c

17.
$$\frac{p+9}{5} = q$$
, for p

18.
$$\frac{b-4z}{7} = a$$
, for *b*

Write an equation and solve for the variable specified.

19. Five more than a number g is six less than twice a number h. Solve for g.

20. One fourth of a number q is three more than three times a number w. Solve for q.

21. Eight less than a number s is three more than four times a number t. Solve for s.

3-8 Practice

Solving Equations and Formulas

Solve each equation or formula for the variable specified.

1.
$$d = rt$$
, for r

$$3. mx + 4y = 3c, \text{ for } x$$

5.
$$ab + 3c = 2d$$
, for b

7.
$$\frac{2}{3}m + a = a + c$$
, for m

9.
$$\frac{2}{3}y + v = s$$
, for y

11.
$$\frac{rx+9}{5} = h$$
, for x

13.
$$2w - y = 7w - 2$$
, for w

2.
$$6w - y = 2z$$
, for w

4.
$$9s - 5g = -4u$$
, for s

6.
$$2p = kx - q$$
, for x

8.
$$\frac{2}{5}h + g = d$$
, for h

10.
$$\frac{3}{4}a - q = k$$
, for a

12.
$$\frac{3b-4}{2}=c$$
, for b

14.
$$3\ell + \nu = 5 + 5\ell$$
, for ℓ

Write an equation and solve for the variable specified.

15. Three times a number s plus 4 times a number y is 1 more than 6 times the number s. Solve for s.

16. Five times a number k minus 9 is two thirds of a number j. Solve for j.

ELECTRICITY For Exercises 17 and 18, use the following information.

The formula for Ohm's Law is E = IR, where E represents voltage measured in volts, I represents current measured in amperes, and R represents resistance measured in ohms.

- **17.** Solve the formula for R.
- **18.** Suppose a current of 0.25 ampere flows through a resistor connected to a 12-volt battery. What is the resistance in the circuit?

MOTION For Exercises 19 and 20, use the following information.

In *uniform circular motion*, the speed v of a point on the edge of a spinning disk is $v = \frac{2\pi}{T}r$, where r is the radius of the disk and T is the time it takes the point to travel once around the circle.

- **19.** Solve the formula for r.
- **20.** Suppose a merry-go-round is spinning once every 3 seconds. If a point on the outside edge has a speed of 12.56 feet per second, what is the radius of the merry-go-round? (Use 3.14 for π .)

Solving Equations and Formulas

Solving Equations and Formulas

Pre-Activity How are equations used to design roller coasters?

Reading to Learn Mathematics

Read the introduction to Lesson 3-8 at the top of page 166 in your textbook. The equation $g(195 - h) = \frac{1}{2}v^2$ contains several variables. What number values do you know for these variables in this situation?

Reading the Lesson

- 1. Suppose you have an equation with several variables. You want to solve for a particular variable. How does the procedure compare with that for solving an equation with just one variable? How does the solution compare with the solution for an equation with one variable?
- 2. Describe what dimensional analysis involves.
- **3.** What do you have to be careful about when you use variables in denominators of fractions?

Helping You Remember

4. When you give the dimensions of a rectangle, you have to tell how many units long it is and how many units wide it is. How can this help you remember what dimensional analysis involves.

NAME DATE PERIOD	DATE PERIOD
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3-8 Enrichment

Dr. Bernardo Houssay

Even though researchers have been studying the disease *diabetes mellitus* for hundreds of years, scientists have only recently discovered the cause of the disease and developed methods for reducing its severity. Dr. Bernardo Houssay, an Argentine physiologist, was one of the pioneers of this more modern research. He studied the relationship between diabetes and the pituitary gland, and in 1947 became the first Latin American to win the Nobel Prize in Medicine and Physiology.

Though there is no cure for diabetes, specific diets and exercise can help people control the disease. The American Diabetes Association (ADA) has helped establish flexible dietary guidelines for consumers to follow. These guidelines include some of the following general nutrition rules.

- Fat intake should be equal to or less than 30% of daily calories.
- Saturated fat intake should be equal to or less than 10% of daily calories.
- Protein should be limited to 10% to 20% of daily calories. Persons showing the initial signs of diabetes-induced kidney disease should limit protein to 10% of daily calories.
- Cholesterol intake should be 300 milligrams or less daily.

Refer to the information above for Exercises 1-4.

- **1.** Robert consumed 2100 calories on Tuesday. His fat intake totaled 70 grams, and of that 70 grams, 14 were saturated.
 - **a.** What percentage of his calorie consumption was fat, and what percentage of that fat was saturated? (To find the percentage of calories from fat, multiply the number of fat grams by 9 before dividing by the number of calories.)
 - **b.** Did Robert stay within the recommended allowance of fats?
- **2.** Anna's cholesterol intake was 330 milligrams on Sunday. By what percentage does she need to reduce her cholesterol consumption to remain within the guidelines?
- **3.** What number of fat grams is 30% of 240 calories?
- **4.** Sharon follows a diet that provides about 50 grams of protein each day. Sharon's doctor has just told her to reduce her daily protein intake by 30%. About how much protein will be in her reduced protein diet?

Lesson 3-9

3-9

Study Guide and Intervention

Weighted Averages

Mixture Problems

Weighted Average

The weighted average M of a set of data is the sum of the product of each number in the set and its weight divided by the sum of all the weights.

Mixture Problems are problems where two or more parts are combined into a whole. They involve weighted averages. In a mixture problem, the weight is usually a price or a percent of something.

Delectable Cookie Company sells chocolate chip cookies for \$6.95 per pound and white chocolate cookies for \$5.95 per pound. How many pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies to obtain a mixture that sells for \$6.75 per pound.

Let w = the number of pounds of chocolate chip cookies

	Number of Pounds	Price per Pound	Total Price
Chocolate Chip	W	6.95	6.95 <i>w</i>
White Chocolate	4	5.95	4(5.95)
Mixture	w + 4	6.75	6.75(w + 4)

Equation: 6.95w + 4(5.95) = 6.75(w + 4)

Solve the equation.

16 pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies.

Exercises

- **1. SOLUTIONS** How many grams of sugar must be added to 60 grams of a solution that is 32% sugar to obtain a solution that is 50% sugar?
- **2. NUTS** The Quik Mart has two kinds of nuts. Pecans sell for \$1.55 per pound and walnuts sell for \$1.95 per pound. How many pounds of walnuts must be added to 15 pounds of pecans to make a mixture that sells for \$1.75 per pound?
- **3. INVESTMENTS** Alice Gleason invested a portion of \$32,000 at 9% interest and the balance at 11% interest. How much did she invest at each rate if her total income from both investments was \$3,200.
- **4. MILK** Whole milk is 4% butterfat. How much skim milk with 0% butterfat should be added to 32 ounces of whole milk to obtain a mixture that is 2.5% butterfat?

3-9

Study Guide and Intervention (continued) Weighted Averages

Uniform Motion Problems Motion problems are another application of weighted averages. **Uniform motion problems** are problems where an object moves at a certain speed, or rate. Use the formula d = rt to solve these problems, where d is the distance, r is the rate, and t is the time.

Bill Gutierrez drove at a speed of 65 miles per hour on an expressway for 2 hours. He then drove for 1.5 hours at a speed of 45 miles per hour on a state highway. What was his average speed?

$$M=rac{65\cdot 2+45\cdot 1.5}{2+1.5}$$
 Definition of weighted average $pprox 56.4$ Simplify.

Bill drove at an average speed of about 56.4 miles per hour.

Exercises

- **1. TRAVEL** Mr. Anders and Ms. Rich each drove home from a business meeting. Mr. Anders traveled east at 100 kilometers per hour and Ms. Rich traveled west at 80 kilometers per hours. In how many hours were they 100 kilometers apart.
- **2. AIRPLANES** An airplane flies 750 miles due west in $1\frac{1}{2}$ hours and 750 miles due south in 2 hours. What is the average speed of the airplane?
- **3. TRACK** Sprinter A runs 100 meters in 15 seconds, while sprinter B starts 1.5 seconds later and runs 100 meters in 14 seconds. If each of them runs at a constant rate, who is further in 10 seconds after the start of the race? Explain.

- **4. TRAINS** An express train travels 90 kilometers per hour from Smallville to Megatown. A local train takes 2.5 hours longer to travel the same distance at 50 kilometers per hour. How far apart are Smallville and Megatown?
- **5. CYCLING** Two cyclists begin traveling in the same direction on the same bike path. One travels at 15 miles per hour, and the other travels at 12 miles per hour. When will the cyclists be 10 miles apart?
- **6. TRAINS** Two trains leave Chicago, one traveling east at 30 miles per hour and one traveling west at 40 miles per hour. When will the trains be 210 miles apart?

3-9

Skills Practice

Weighted Averages

SEASONING For Exercises 1-4, use the following information.

A health food store sells seasoning blends in bulk. One blend contains 20% basil. Sheila wants to add pure basil to some 20% blend to make 16 ounces of her own 30% blend. Let b represent the amount of basil Sheila should add to the 20% blend.

1. Complete the table representing the problem.

	Ounces	Amount of Basil
20% Basil Blend		
100% Basil		
30% Basil Blend		

- **2.** Write an equation to represent the problem.
- **3.** How many ounces of basil should Sheila use to make the 30% blend?
- **4.** How many ounces of the 20% blend should she use?

HIKING For Exercises 5-7, use the following information.

At 7:00 A.M., two groups of hikers begin 21 miles apart and head toward each other. The first group, hiking at an average rate of 1.5 miles per hour, carries tents, sleeping bags, and cooking equipment. The second group, hiking at an average rate of 2 miles per hour, carries food and water. Let t represent the hiking time.

5. Copy and complete the table representing the problem.

	r	t	d = rt
First group of hikers			
Second group of hikers			

- **6.** Write an equation using t that describes the distances traveled.
- 7. How long will it be until the two groups of hikers meet?

SALES For Exercises 8 and 9, use the following information.

Sergio sells a mixture of Virginia peanuts and Spanish peanuts for \$3.40 per pound. To make the mixture, he uses Virginia peanuts that cost \$3.50 per pound and Spanish peanuts that cost \$3.00 per pound. He mixes 10 pounds at a time.

- 8. How many pounds of Virginia peanuts does Sergio use?
- 9. How many pounds of Spanish peanuts does Sergio use?

NAME	DATE	PERIOD

3-9 Practice

Weighted Averages

GRASS SEED For Exercises 1-4, use the following information.

A nursery sells Kentucky Blue Grass seed for \$5.75 per pound and Tall Fescue seed for \$4.50 per pound. The nursery sells a mixture of the two kinds of seed for \$5.25 per pound. Let k represent the amount of Kentucky Blue Grass seed the nursery uses in 5 pounds of the mixture.

1. Complete the table representing the problem.

	Number of Pounds	Price per Pound	Cost
Kentucky Blue Grass			
Tall Fescue			
Mixture			

2. Write an equation to represent the problem.

3. How much Kentucky Blue Grass does the nursery use in 5 pounds of the mixture?

4. How much Tall Fescue does the nursery use in 5 pounds of the mixture?

TRAVEL For Exercises 5-7, use the following information.

Two commuter trains carry passengers between two cities, one traveling east, and the other west, on different tracks. Their respective stations are 150 miles apart. Both trains leave at the same time, one traveling at an average speed of 55 miles per hour and the other at an average speed of 65 miles per hour. Let t represent the time until the trains pass each other.

5. Copy and complete the table representing the problem.

	r	t	d = rt
First Train			
Second Train			

6. Write an equation using t that describes the distances traveled.

7. How long after departing will the trains pass each other?

8. TRAVEL Two trains leave Raleigh at the same time, one traveling north, and the other south. The first train travels at 50 miles per hour and the second at 60 miles per hour. In how many hours will the trains be 275 miles apart?

9. JUICE A pineapple drink contains 15% pineapple juice. How much pure pineapple juice should be added to 8 quarts of the drink to obtain a mixture containing 50% pineapple juice?

Reading to Learn Mathematics

Weighted Averages

Pre-Activity How are scores calculated in a figure skating competition?

Read the introduction to Lesson 3-9 at the top of page 171 in your textbook. Why is the sum of Ilia Kulik's scores divided by 3?

Reading the Lesson

- 1. Read the definition of weighted average on page 171 of your textbook. What is meant by the weight of a number in a set of data?
- 2. Linda's quiz scores in science are 90, 85, 85, 75, 85, and 90. What is the weight of the score 85?
- **3.** Suppose Clint drives at 50 miles per hour for 2 hours. Then he drives at 60 miles per hour for 3 hours.
 - **a.** Write his speed for each hour of the trip.

Speed					
Hour	1	2	3	4	5

b. What is the weight of each of the two speeds?

Helping You Remember

4. Making a table can be helpful in solving mixture problems. In your own words, explain how you use a table to solve mixture problems.

3-9 Enrichment

Diophantine Equations

The first great algebraist, Diophantus of Alexandria (about A.D. 300), devoted much of his work to the solving of indeterminate equations. An indeterminate equation has more than one variable and an unlimited number of solutions. An example is x + 2y = 4.

When the coefficients of an indeterminate equation are integers and you are asked to find solutions that must be integers, the equation is called *diophantine*. Such equations can be quite difficult to solve, often involving trial and error—and some luck!

Solve each diophantine equation by finding at least one pair of positive integers that makes the equation true. Some hints are given to help you.

1.
$$2x + 5y = 32$$

a. First solve the equation for x.

b. Why must *y* be an even number?

c. Find at least one solution.

2.
$$5x + 2y = 42$$

a. First solve the equation for x.

b. Rewrite your answer in the form x = 8 + some expression.

c. Why must (2 - 2y) be a multiple of 5?

d. Find at least one solution.

$$3. 2x + 7y = 29$$

4.
$$7x + 5y = 118$$

5.
$$8x - 13y = 100$$

6.
$$3x + 4y = 22$$

7.
$$5x - 14y = 11$$

8.
$$7x + 3y = 40$$

Chapter 3 Test, Form 1

SCORE ___

Write the letter for the correct answer in the blank at the right of each question.

1. Solve
$$x + 19 = 5$$
.

2. Solve
$$y - 18 = -3$$
.

A.
$$-21$$

$$\mathbf{C.} - 15$$

3. Solve
$$5n = 35$$
.

4. Solve
$$\frac{c}{3} = 6$$
.

5. Solve
$$\frac{3}{5}x = 15$$
.

6. Solve
$$2t + 1 = 3$$
.

7. Translate the following sentence into an equation.

Twice a number m minus three equals the sum of m and five.

A.
$$2(m-3)=m+5$$

B.
$$2m - 3 = m + 5$$

C.
$$2m - 3 = 5m$$

D.
$$2(m-3)=5m$$

8. Translate the following equation into a verbal sentence.

$$x + 5 = 2(7 + x)$$

- **A.** The quotient of x and five is two times seven plus x.
- **B.** The number x plus five is two times the sum of seven and x.
- **C.** The number x plus five is two times seven plus x.
- **D.** The product of x and five is the sum of two times seven and x.

9. A number is added to 9. The result is then multiplied by 4 to give a new result of 120. What is the number?

D.
$$4(n+9)+120$$
 9. ____

10. Which ratio forms a proportion with
$$\frac{7}{14}$$
?

A.
$$\frac{4}{9}$$

B.
$$\frac{5}{12}$$

C.
$$\frac{2}{5}$$

D.
$$\frac{3}{6}$$

Chapter 3 Test, Form 1 (continued)

- **11.** Solve the proportion $\frac{2}{7} = \frac{x}{42}$.
 - **A.** $\frac{1}{2}$
- **B.** 12
- **C.** $\frac{2}{7}$
- **D.** 6
- 11. ____

- **12.** Solve 3t 6 = t 2.
 - **A.** -2
- **B.** -4
- **C.** 2
- **D.** 1
- 12. ____

- **13.** Solve 4(t+1) = 6t 1.
 - **A.** $2\frac{1}{2}$
- **B.** 1
- **C.** 0
- **D.** $1\frac{1}{2}$
- 13. _____

- **14.** Solve 5(g-2) + g = 6(g-4).
 - A. all numbers
- **B.** 0
- **C.** 2
- **D.** no solution
- 14. ____

- **15.** Solve ax 5 = b for *a*.
 - **A.** x(b + 5)
- **B.** $\frac{b-5}{r}$
- C. $\frac{b+5}{x}$
- **D.** x(b-5)
- 15. _____

- **16.** Find the percent of change. original: 10 new: 12
 - **A.** 12%
- **B.** 25%
- C. 20%
- **D.** 18%
- 16. _____
- 17. A baseball costs \$4.00. If the sales tax is 5%, what is the total price?
 - **A.** \$3.80
- **B.** \$4.20
- **C.** \$4.05
- **D.** \$4.50
- 17. _____
- **18.** How many liters of pure acid must be added to 3 liters of a 50% acid solution to obtain a 75% acid solution?
 - **A.** 1 L
- **B.** 4.5 L
- **C.** 1.5 L
- **D.** 3 L
- 18. ____
- **19.** Joe and Janna leave home at the same time, traveling in opposite directions. Joe drives 45 miles per hour and Janna drives 40 miles per hour. In how many hours will they be 510 miles apart?
 - **A.** 7 hours
- **B.** 6 hours
- C. 5 hours
- **D.** 4 hours
- 19. ____
- **20. TEMPERATURE** In Death Valley, California, the highest ground temperature recorded was 94°C on July 15, 1972. In the formula
 - $C = \frac{5}{9}(F 32)$, C represents the temperature in degrees Celsius and F represents the temperature in degrees Fahrenheit. To the nearest degree,

what is the highest ground temperature in Death Valley in Fahrenheit?

- **A.** 201°F
- **B.** 84°F
- **C.** 34°F
- **D.** 137°F
- 20. ____

Bonus A concrete mixture is made with 3 parts water and 5 parts cement. If 27 parts of water are being used in the current batch of concrete, how many parts of cement are being used?



Chapter 3 Test, Form 2A

SCORE _____

Write the letter for the correct answer in the blank at the right of each question.

1. Solve
$$m - (-4) = 7$$
.

C.
$$-3$$

2. Solve
$$m - 13 = 8$$
.

3. Solve
$$5w = -75$$
.

4. Solve
$$-\frac{n}{4} = -12$$
.

5. Solve
$$-\frac{3}{8}y = -24$$
.

6. Solve
$$5x + 3 = 23$$
.

B.
$$5\frac{1}{2}$$

7. Translate the following sentence into an equation.

The sum of twice a number x and 13 is two less than three times x.

A.
$$2(x+13)=3x-2$$

B.
$$2x + 13 = 2 - 3x$$

C.
$$2x + 13 = 3x - 2$$

D.
$$2x + 13 = 3(x - 2)$$

8. Translate the following equation into a verbal sentence.

$$3x - y = 5(y + 2x)$$

- **A.** Three times the difference of x and y equals five times the sum of y and two times x.
- **B.** Three times x less than y is five times y plus two times x.
- **C.** The sum of three times x and y is five times y plus two times x.
- **D.** Three times x minus y is five times the sum of y and two times x.

10. Which ratio forms a proportion with
$$\frac{25}{35}$$
?

A.
$$\frac{3}{5}$$

B.
$$\frac{15}{21}$$

C.
$$\frac{24}{34}$$

D.
$$\frac{5}{10}$$

Chapter 3 Test, Form 2A (continued)

11. Solve the proportion $\frac{5}{3c} = \frac{1}{6}$.

- **A.** 2
- **B.** 10
- **C.** 30
- **D.** $\frac{11}{3}$
- 11. ____

12. Solve 2x + 7 = 5x + 16.

- **A.** −3
- **B.** $\frac{2}{3}$
- C. $-7\frac{2}{3}$
- **D.** 3
- **12.**

13. Solve $\frac{2}{3}(6x + 30) = x + 5(x + 4) - 2x$.

- **A.** 6
- **B.** 0
- **C.** all numbers
- **D.** no solution
- 13. _____

14. Solve -3(h-6) = 5(2h+3).

- **A.** $-\frac{3}{13}$ **B.** $\frac{3}{13}$
- $C_{\bullet} \frac{9}{13}$
- **D.** $\frac{9}{13}$
- 14. ____

15. Solve 2x - y = y for *x*.

- **A.** 2y 2
- **B.** $\nu 2$
- \mathbf{C} . γ
- **D.** 0
- 15. _____

16. Find the percent of change. original: 80 new: 64

- **A.** 25%
- **B.** 20%
- **C.** 16%
- **D.** 10%
- 16. _____

17. A calculator costs \$32.00. If the sales tax is 6%, what is the total price?

- **A.** \$31.40
- **B.** \$30.08
- **C.** \$32.60
- **D.** \$33.92
- 17. _____

18. How many liters of a 40% acid solution must be added to 12 liters of a 20% solution to obtain a 25% solution?

- **A.** 4
- **B.** 1
- **C.** 16
- **D.** $\frac{4}{5}$
- 18. _____

19. Mandy begins bicycling west at 30 miles per hour at 11 A.M. If Liz leaves from the same point 20 minutes later bicycling west at 36 miles per hour, when will she catch Mandy?

- **A.** 2:00 P.M.
- **B.** 1:00 P.M.
- **C.** 1:30 P.M.
- **D.** 2:30 P.M.
- 19. _____

20. GEOMETRY The formula for the volume of a cone is $V = \frac{1}{3}\pi r^2 h$ where Vrepresents the volume, r represents the radius of the base, and h represents the height. What is the height of a cone with a volume of 66 cubic

centimeters and a base with a radius of 3 centimeters?

B. 69.14 cm

- **C.** 7 cm
- **D.** 0.78 cm
- 20. ____

Bonus A mixture of 10% acid and 90% water is added to 5 liters of pure acid. The final mixture is 40% water. How many



liters of water are in the final mixture?

A. 21 cm

Write the letter for the correct answer in the blank at the right of each question.

1. Solve
$$4 = n - (-3)$$
.

D.
$$-7$$

2. Solve
$$x - 12 = 5$$
.

A.
$$-17$$

3. Solve
$$6z = -84$$
.

A.
$$-90$$

4. Solve
$$-15 = -\frac{w}{3}$$
.

5. Solve
$$-\frac{4}{7}s = -28$$
.

6. Solve
$$2 + 7y = 44$$
.

A.
$$6\frac{4}{7}$$

7. Translate the following sentence into an equation.

The product of five and a number y is two less than the quotient of four and y.

A.
$$5 + y = \frac{4}{y} - 2$$

B.
$$5y = \frac{4}{y} - 2$$

C.
$$5y = 2 - \frac{4}{y}$$

D.
$$5 + y = 2 - \frac{4}{v}$$

8. Translate the following equation into a verbal sentence.

$$x(7-5y) = \frac{x}{2}$$

- **A.** x times seven minus five times y equals x divided by two.
- **B.** The product of x and seven minus five times y equals the quotient of x and two.
- **C.** x times the difference of seven and the product of five and y equals the quotient of x and two.
- **D.** x times the sum of seven and five times y equals x divided by two.

C.
$$21\frac{1}{2}$$

D.
$$3\frac{1}{2}$$

10. What ratio forms a proportion with
$$\frac{8}{36}$$
?

A.
$$\frac{1}{4}$$

B.
$$\frac{6}{27}$$

C.
$$\frac{7}{30}$$

D.
$$\frac{2}{7}$$

Chapter 3 Test, Form 2B (continued)

- **11.** Solve the proportion $\frac{1}{8} = \frac{7}{2h}$.
 - **A.** 4
- C. 56
- **D.** 16
- 11. ____

- **12.** Solve 9a + 28 = 4a + 3.
 - **A.** -30
- **B.** -20
- C. $6\frac{1}{5}$
- **D.** -5
- 12. _____

- **13.** Solve $3x + 4(x 8) x = \frac{3}{5}(10x + 15)$.
 - **A.** 0
- B. all numbers
- C. no solution
- **D.** 41
- 13. _____

- **14.** Solve 4(3r-2) = -3(r+7).

 - **A.** $-\frac{13}{15}$ **B.** $-1\frac{4}{15}$
- C. $1\frac{14}{15}$
- **D.** $-1\frac{3}{10}$
- 14. _____

- **15.** Solve 3b = 6v 3b, for v.
 - **A.** 6b 6
- **B.** *b*
- **C.** b 6
- **D.** 0
- 15. _____

- **16.** Find the percent of change. original: 45 new: 54
 - **A.** $33\frac{1}{2}\%$
- **B.** 25%
- C. $16\frac{2}{3}\%$
- **D.** 20%
- 16. _____

- 17. Find the discounted price. radio: \$45.00 discount: 30%
 - **A.** \$15.00
- **B.** \$31.50
- **C.** \$36.00
- **D.** \$42.00
- 17. _____
- 18. Nature Drinks wants to combine orange juice they sell for \$0.09 per ounce with guava juice they sell for \$0.14 per ounce to create an orange-guava drink. How many ounces of orange juice should they use to create a 16-ounce drink that would sell for \$1.74?
 - **A.** 10
- **B.** 6
- **C.** 16
- **D.** 0
- 18. _____
- 19. Teri begins walking east at 2 miles per hour at 1 P.M. If Cindy leaves from the same point 30 minutes later walking east at 3 miles per hour, when will she catch Teri?
 - **A.** 2:30 P.M.
- **B.** 1:30 P.M.
- C. 2:00 P.M.
- **D.** 3:00 P.M.
- 19. _____
- **20. GEOMETRY** The formula for the volume of a cone is $V = \frac{1}{2}\pi r^2 h$, where V

represents the volume, r represents the radius of the base, and h represents the height. What is the height of a cone with a volume of 110 cubic centimeters and a base with a radius of 5 centimeters?

- **A.** 21 cm
- **B.** 0.47 cm
- **C.** 4.2 cm
- **D.** 41.49 cm
- 20. ____

Bonus In a bag of blue, green, and red marbles, 50% are blue and 30% are green. There are 6 red marbles in the bag. If you increase the number of blue marbles by 40%, how many blue marbles will be in the bag?



For Questions 1-8, solve each equation.

1.
$$12 + r = 3$$

2.
$$\frac{1}{5} = x - \frac{2}{5}$$

3.
$$-12 = p - 7$$

4.
$$-7b = -35$$

5.
$$31 = -\frac{n}{6}$$

6.
$$-\frac{5}{8}w = -9$$

7.
$$\frac{9}{25} = \frac{p}{125}$$

8.
$$-3a + 4 = -14$$

- **9.** Translate the following sentence into an equation. A number x subtracted from 36 is three times the sum of four and x.
- **10.** Translate the following equation into a verbal sentence. 3(x + y) = 2y x

- 11. What number decreased by 3.5 equals 12.7?
- **12.** Twelve is added to the product of a number and 5. The result is -3. Find the number.
- **13.** Solve the following problem by working backward. Julie cashed a paycheck and repaid her brother \$10 that she had borrowed from him. She then spent \$30 on fuel for her car and half of the remaining money on a new tent for camping. She bought a pair of running shoes for \$29.45 and had \$17.75 left. How much did Julie receive when she cashed her paycheck?
- **14.** Use cross products to determine whether the pair of ratios $\frac{4}{6}$ and $\frac{14}{21}$ form a proportion. Write *yes* or *no*.

11._____





14. _____

3

Chapter 3 Test, Form 2C (continued)

15. Solve the proportion
$$\frac{x}{6} = \frac{2}{9}$$
.

16. Solve the proportion
$$\frac{12}{15} = \frac{18}{h}$$
.

For Questions 17-19, solve each equation.

17.
$$-x + 4 = x + 6$$

18.
$$5n + 7 = 7(n + 1) - 2n$$

19.
$$-4(p+2) + 8 = 2(p-1) - 7p + 15$$

20. Solve
$$\frac{a}{b}x - c = 0$$
 for x .

- **21.** State whether the percent of change is a percent of increase or a percent of decrease. Then find the percent of change. original: 55 new: 44
- 21. _____
- **22.** A shirt costs \$12.00. If the sales tax is 7%, find the total cost.
- 22. _____
- **23.** How many liters of a 90% acid solution must be added to 6 liters of a 15% acid solution to obtain a 40% acid solution?
- 23. _____
- **24.** A freight train leaves a station traveling 60 miles per hour. Thirty minutes later a passenger train leaves the station in the same direction on a parallel track at a speed of 72 miles per hour. How long will it take the passenger train to catch the freight train?
- 24. _____
- **25. GEOMETRY** A container company wants to make a cylindrical can with a volume of 1188 cubic inches. The formula $V = \pi r^2 h$ represents the volume of a cylinder. In this formula, V represents the volume, r represents the radius of the cylinder's base, and h represents the height of the cylinder. Solve for h. What height should the company make the can if the radius of the base must be 6 inches?
- 25. _____

- **Bonus** A clown is preparing for a party by inflating one balloon for every invited guest. Just when she has half of the necessary balloons inflated, 3 of them pop. She inflates 5 more balloons, and two pop. Then 6 balloons are carried away by the wind. She finishes by inflating 16 more balloons, and then learns that only 12 guests will attend the party. How many extra balloons did the clown inflate?
- B: _____

Chapter 3 Test, Form 2D

SCORE _____

For Questions 1-8, solve each equation.

1.
$$7 + t = 11$$

2.
$$\frac{1}{9} = y - \frac{5}{9}$$

3.
$$-5 = v - 12$$

4.
$$-8x = -56$$

5.
$$14 = -\frac{s}{5}$$

6.
$$-\frac{7}{9}y = -6$$

7.
$$\frac{10}{27} = \frac{a}{135}$$

8.
$$3-5b=-32$$

10. Translate the following equation into a verbal sentence.
$$\frac{3}{y} - 5 = x(y+7)$$

For Questions 11 and 12, write an equation for each problem. Then solve the equation.

11. What number decreased by
$$8.1$$
 equals 4.9 ?

14. Use cross products to determine whether the pair of ratios
$$\frac{9}{21}$$
 and $\frac{12}{26}$ form a proportion. Write *yes* or *no*.

3

Chapter 3 Test, Form 2D (continued)

15. Solve the proportion
$$\frac{3}{25} = \frac{y}{15}$$
.

16. Solve the proportion
$$\frac{9}{12} = \frac{15}{a}$$
.

For Questions 17-19, solve each equation.

17.
$$9 - t = t + 3$$

18.
$$2(y-6) = 3y + 12 - y$$

19.
$$17 + 3(z - 2) - 11z = -7(z + 2) + 14$$

20. Solve
$$\frac{r}{s} + t = 4v$$
 for r .

21. State whether the percent of change is a percent of *increase* or a percent of *decrease*. Then find the percent of change. original: 60, new: 75

21. _____

22. Find the discounted price. flashlight: \$18.00 discount: 25%

22. _____

23. Nature's Best wants to combine nuts they sell for \$3.60 a pound with dried fruit they sell for \$2.40 a pound to create a trail mix. How much of each snack should they use to make 10 pounds of trail mix that would sell for \$3.30 a pound?

23. _____

24. Paula leaves home driving 40 miles per hour. One hour later, her brother Dan leaves home, driving in the same direction at a speed of 50 miles per hour. How long will it take Dan to catch up to Paula?

24. _____

25. GEOMETRY A container company wants to make a cylindrical cardboard container with a volume of 4752 cubic inches. The formula $V = \pi r^2 h$ represents the volume of a cylinder. In this formula, V represents the volume, r represents the radius of the cylinder's base, and h represents the height of the cylinder. Solve for h. What height should the company make the container if the radius of the base must be 9 inches?

25. _____

Bonus A store has all board games on sale for 25% off the regular price. A checker set has a sale price of \$12. It is then moved to a clearance table where every item is discounted 40% off its regular price. What is the clearance price of the checker set?

B: _____

Chapter 3 Test, Form 3

SCORE _____

For Questions 1-6, solve each equation.

1.
$$n + 39 = 12$$

2.
$$w + (-8) = -21$$

3.
$$-6n = 16$$

4.
$$-13 = -\frac{n}{4}$$

$$5. \ \frac{3}{4}h = -\frac{45}{52}$$

6.
$$-\frac{a}{6} + 7 = -14$$

7. If
$$x - 5 = 12$$
, what is the value of $x - 9$?

1. _____

2.

3. _____

4. _____

5. _____

6. _____

7. _____

result of five times the difference of 32 and the number x.

For Questions 9 and 10, write an equation for each problem. Then solve the equation.

9. Three-fifths of what number equals one?

9. _____

10. The product of 2 more than a number and 10 is 36 more than 8 times the number. What is the number?

10. _____

11. Translate the following equation into a verbal sentence. $5(2x + 3y) = y^2 - 2x^3$

11. _____

12. Solve the following problem by working backward. Shyam invested money in the stock market. In the first year, his stock increased 20%. He paid his stock broker \$300 and then lost \$450. He withdrew \$500, and then his remaining investment doubled. Shyam's investment is now worth \$7100. How much was Shyam's original investment?

12. _____

13. Use cross products to determine whether the pair of ratios $\frac{42}{48}$ and $\frac{63}{72}$ form a proportion. Write *yes* or *no*.

13. _____

14. Solve the proportion $\frac{t+4}{t-2} = \frac{1}{4}$.

14. _____

15. A blueprint for a house states that 2 inches represents 8 feet. If the width of a window is 2.5 inches on the blueprint, what is the width of the actual window?

15. _____

3

Chapter 3 Test, Form 3 (continued)

For Questions 16-18, solve each equation.

16.
$$6 - 2y = 7y + 13$$

17.
$$3x - 5(x - 6) = 2(10 - x) + 10$$

18.
$$5(7-a) - 3(a+4) - 4 = 4(a-3) + 7$$

19. Solve
$$ax - n = r$$
 for x .

20. Solve
$$\frac{4x + t}{r} = s$$
 for *x*.

original: 75, new: 84

25. PHYSICS A ball is thrown straight up at an initial velocity of 53 feet per second. In the first 1.5 seconds, it travels 42 feet. The formula
$$s = \left(\frac{u+v}{2}\right)t$$
 represents the vertical distance s that an object travels in t seconds, where u represents the initial velocity of the object and v represents the velocity of the object at the end of t seconds. Find the velocity of the ball at the end of 1.5 seconds.

Bonus Paloma Rey drove to work on Wednesday at 40 miles per hour and arrived one minute late. She left home at the same time on Thursday, drove 45 miles per hour, and arrived one minute early. How far does Ms. Rey drive to work?



Demonstrate your knowledge by giving a clear, concise solution to each problem. Be sure to include all relevant drawings and justify your answers. You may show your solution in more than one way or investigate beyond the requirements of the problem.

- **1.** Phrase 1: x times y plus z Phrase 2: x times the sum of y and z
 - **a.** Discuss what is different between the two phrases.
 - **b.** Find values for x, y and z that make the two phrases equal.
- **2. a.** Solve $\frac{ry+s}{m}-t=x$ for y, and explain each step in your solution.
 - **b.** Would there be any limitations for the value of each variable? If so, explain the limitation.
- **3.** You buy a stereo at a local store. The stereo has been discounted by 10%. The store then charges 10% tax.
 - a. Compare the final price with the original price.
 - **b.** Would the final price be different if the tax was added first and then the discount was applied to this new amount?
- **4.** Tony and Ivia started walking south from the same location at the same time. Ivia walked 8 miles and walked 1 mile per hour faster than Tony who walked 6 miles. They each walked for the same amount of time.
 - **a.** Describe how a proportion could be used to find the rate that each person walked.
 - **b.** The next day they both walked 6 miles, and Ivia again walked 1 mile per hour faster than Tony, who walked 3 miles per hour. Determine whether a proportion could be used to find how long each person walked.
- **5. a.** Write four equivalent equations to x = 8 using one of the four operations of addition, subtraction, multiplication and division for each equivalent equation. Use each operation only once.
 - **b.** Write an equivalent equation to x = 8 that has the variable x on both sides.
 - **c.** Determine if $\frac{n}{6} = \frac{15}{18}$ and 2(n+1) = 3(n-1) are equivalent equations. Determine if either equation is equivalent to any of the equations created for parts **a** and **b**.

3

Chapter 3 Vocabulary Test/Review

SCORE ____

Addition Property of Equality means rate consecutive integers mixture problem ratio defining a variable Multiplication Property of scale dimensional analysis Equality solve an equation Subtraction Property of Division Property of Equality multi-step equations equivalent equation number theory Equality extremes percent of change uniform motion problem formula percent of decrease weighted average four-step problem-solving plan percent of increase work backward identity proportion

Write whether each sentence is *true* or *false*. If false, replace the underlined word or number to make a true sentence.

- **1.** The Addition Property of Equality states that if the same number is <u>subtracted from</u> each side of an equation, the resulting equation is true.
- 1. _____
- **2.** If the <u>same number</u> is added to each side of a true equation, then the result is a true equation.
- 2. _____
- **3.** The Multiplication Property of Equality states that if each side of a true equation is multiplied by the same number, the resulting equation is true.
- 3. _____
- **4.** Multi-step equations are equations with <u>less</u> than one operation.
- 4. _____
- **5.** An equation that is <u>false</u> for every value of the variable is called an identity.
- 5. _____
- **6.** A ratio is a comparison of two numbers by <u>multiplication</u>.
- 6. _____
- **7.** The ratio of two measurements having different units of measure is called a rate.
- 7. _____

8. A percent of increase or decrease is called a percent of change.

- 8. _____
- **9.** If the new number is less than the original number, the percent of change is a <u>percent of increase</u>.
- 9. _____
- **10.** If the new number is greater than the original number, the percent of change is a <u>percent of decrease</u>.
- 10. _____

In your own words— Define each term.

- 11. proportion
- 12. formula

Chapter 3 Quiz (Lessons 3–1 through 3–3)

SCORE ___

Translate each sentence into an equation.

- **1.** Two times a number n is three times the sum of n and nine.
- **2.** The difference of the square of *y* and twelve is the same as the product of five and x.

Translate each equation into a verbal sentence.

3.
$$2b - 10 = 4$$

4.
$$y + 3x^2 = 5x$$

Solve each equation.

5.
$$d - 8 = 6$$

6.
$$-28 = p + 21$$

5.
$$d - 8 = 6$$

6.
$$-28 = p + 21$$

7.
$$-3 - (-g) = -12$$

8.
$$-7x = 63$$

9.
$$-\frac{t}{5} = -8$$

10.
$$\frac{4}{5}d = -32$$

_____ PERIOD ____ NAME _

Chapter 3 Quiz (Lessons 3–4 and 3–5)

SCORE _____

Solve each equation.

1.
$$3x + 8 = 29$$

A. -11

2.
$$\frac{a}{6} - 5 = 9$$

 $\mathbf{C.} - 39$

3.
$$5r - 14 = -42$$

4.
$$7n + 6 = 4n - 9$$

5.
$$3b - 13 + 4b = 7b + 1$$

6.
$$5 - 3(w + 4) = w - 7$$

D. 9

7.
$$2x - 5(x - 3) = 2(x - 10)$$

8. Standardized Test Practice Solve
$$-6(2r + 8) = -10(r - 3)$$
.

- **9.** A number is multiplied by 4, and then 5 is subtracted from the product. The result is 3. What is the number?
- 10. Three is subtracted from a number, and then the difference is divided by 11. The result is 12. What is the number?

Chapter 3 Quiz (Lessons 3–6 and 3–7)

SCORE ____

Use cross products to determine whether each pair of ratios forms a proportion. Write yes or no.

1.
$$\frac{5}{7}$$
, $\frac{20}{28}$

2.
$$\frac{11}{13}$$
, $\frac{22}{25}$

3.
$$\frac{4.2}{6.3}$$
, $\frac{0.3}{0.5}$

Solve each proportion.

4.
$$\frac{3}{4} = \frac{n}{20}$$

5.
$$\frac{6}{4} = \frac{x}{18}$$

4.
$$\frac{3}{4} = \frac{n}{20}$$
 5. $\frac{6}{4} = \frac{x}{18}$ **6.** $\frac{33}{b} = \frac{15}{45}$

6.

For Questions 7 and 8, state whether the percent of change is a percent of *increase* or a percent of *decrease*. Then find the percent of change.

7. original: 25 new: 18

8. original: 36 new: 45

8.

9. The cost of a compact disc is \$18. If the sales tax is 6%, find the total price.

10. Find the discounted price. camera: \$108

discount: 30%

10.

DATE _____ PERIOD ____

Chapter 3 Quiz (Lessons 3–8 and 3–9)

SCORE _____

For Questions 1 and 2, solve each equation or formula for the variable specified.

1.
$$nx - m = p$$
, for x

$$2. \ \frac{x-b}{a} = c, \text{ for } b$$

5. The formula
$$p = 2\ell + 2w$$
 represents the perimeter of a rectangle. In this formula, ℓ is the length of the rectangle and w is the width. Solve the formula for ℓ . Find the length when the width is 4 meters and the perimeter is 36 meters.

SCORE ____

(Lessons 3–1 through 3–5)

Part I Write the letter for the correct answer in the blank at the right of each question.

1. Translate the following sentence into an equation.

The product of five and the sum of a number x and three is twelve.

A.
$$5 + 3x = 12$$

B.
$$5(x + 3) = 12$$

C.
$$5x + 3 = 12$$

D.
$$5x + 3 = x$$

2. Solve y + (-16) = -12.

C.
$$\frac{3}{4}$$

3. Solve $-\frac{a}{6} + 5 = 2$.

C.
$$\frac{1}{2}$$

4. Solve $\frac{3}{5}y = -9$.

A.
$$-5\frac{2}{5}$$

D.
$$-\frac{5}{9}$$

5. Solve -6d = -42.

6. Solve
$$-18 = v - (-4)$$
.

Part II

For Questions 7-9, solve each equation.

7.
$$5(12 - 3p) = 15p + 60$$

8.
$$3(y-2) = 6(y-1) - 3y$$

9.
$$3a + 21 = 7 - 4a$$

- 10. Solve the following problem by working backward. Liza earned some money delivering newspapers. She bought a battery for \$1.95, and gave her mother \$30. She bought a ring for \$7.20, and then spent half of the remaining money on a radio. If Liza has \$38.50 left, how much money did she earn delivering newspapers?
- 10. _____

For Questions 11 and 12, translate each equation into a verbal sentence.

11.
$$4n = m(5 - n)$$

12.
$$3(y + 5) = 7y$$

3.

Chapter 3 Cumulative Review

SCORE ____

(Chapters 1–3)

1. Evaluate
$$3y - x^2z$$
 if $x = 2$, $y = 14$, and $z = 5$. (Lesson 1–2)

2. Simplify
$$2(u + 3v) + 3(u + v)$$
. (Lesson 1–6)

Find each of the following. (Lessons 2–2 through 2–4, 2–7)

6.
$$52 \div (-4)$$

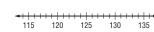
7.
$$-\sqrt{1.69}$$

5. 12(-32)

128 120 134 118 118 121 125

122121 120 119 120 120 118 **Source**: World Almanac

Make a line plot of the data. (Lesson 2-5)



- **9.** A baseball player has a batting average of 0.250. What are the odds that the next time the player bats he gets a hit? (Lesson 2-6)
- **10.** Translate the following sentence into an algebraic equation. Nine times a number y subtracted from 85 is seven times the sum of four and y. (Lesson 3-1)
- 10. _____
- 11. Solve the following problem by working backward. Three is added to a number. The result is divided by two, and then the new result is added to eighteen. The final result is 35. What is the number? (Lesson 3–4)
- 11. _____

For Questions 12-14, solve each equation.

(Lessons 3-2 through 3-5)

13.
$$7a + 2 = 3a - 10$$

12.
$$-27 = -6 - 3p$$

14. 2(x-3) + 6x = 3(9-x)

15 Solve
$$a = \frac{m}{n} + n$$
 for m (Lesson 2.9)

15. Solve
$$q = \frac{m}{n} + p$$
 for m . (Lesson 3–8)

Standardized Test Practice

(Chapters 1-3)

Part 1: Multiple Choice

Instructions: Fill in the appropriate oval for the best answer.

1. Write an algebraic expression for the following verbal expression. The sum of n and 5. (Lesson 1–1)

A. 5*n*

C. n + 5 **D.** n - 5 **1.** (A) (B) (C) (D)

2. State the hypothesis of the following statement. If I complete my algebra homework daily, then I will learn the

concepts. (Lesson 1-7)

E. I will learn the concepts.

F. I don't do my algebra homework.

G. I won't learn the concepts.

H. I complete my algebra homework daily.

2. E F G H

3. Simplify the expression 7(x-y)-2(y-x)+4x. (Lesson 1–5)

A. 13x - 9y **B.** 9x - 5y **C.** 9x - 9y **D.** 13x - 5y

3. A B C D

4. Evaluate $a(b-c^2)$ if $a=\frac{2}{3}, b=\frac{3}{4}$, and $c=\frac{1}{2}$. (Lesson 2–3)

E. $\frac{1}{6}$

F. $\frac{1}{2}$ **G.** $\frac{1}{4}$ **H.** $\frac{2}{3}$

4. (E) (F) (G) (H)

5. The heights in feet of the 10 largest National Champion trees are listed below. Source: World Almanac

275 321 159 191 281 83 108 232 219 102

Which measure of central tendency best represents the data? (Lesson 2-5)

A. the mode

B. the mean or the median

C. the mean or the mode

D. the median or the mode

5. A B C D

6. A letter is chosen at random from the name *Antarctica*. What is the probability that the chosen letter is a vowel? (Lesson 2-6)

F. $\frac{3}{10}$ **G.** $\frac{1}{2}$ **H.** $\frac{3}{5}$

6. (E) (F) (G) (H)

Assessment

7. Solve $-\frac{3}{4}y = \frac{8}{20}$. (Lesson 3–3)

B. $-\frac{3}{10}$ **C.** $\frac{8}{15}$ **D.** $-\frac{8}{15}$

7. A B C D

8. Which equation has a solution of -2? (Lesson 3–4)

E. 4n + 3 = 11

G. 5(1+n)=-5

F. 4 = 3n - 2

H. 3(n+1)=2

8. E F G H

9. A car dealership has 180 cars on their lot. If they increase their inventory by 25%, how many cars will be on the lot? (Lesson 3-7)

A. 230

B. 225

C. 135

D. 205

9. A B C D

Standardized Test Practice (continued)

Part 2: Grid In

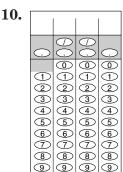
Instructions: Enter your answer by writing each digit of the answer in a column box and then shading in the appropriate oval that corresponds to that entry.

10. Solve
$$2\frac{1}{3} - \frac{5}{6} = t$$
. (Lesson 1–3)

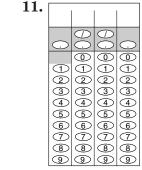
11. Find
$$\frac{1}{3} + (-\frac{1}{4})$$
. (Lesson 2–2)

12. Solve
$$7 - 3x = 4 + 9x$$
. (Lesson 3–5)

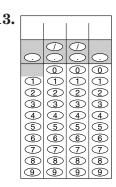
13. Sasha drove from her house to the grocery store in 20 minutes. Her return trip took 15 minutes. If the store is 7 miles from her house, what was Sasha's average speed for the round trip, in miles per hour? (Lesson 3–9)



12.



				1
0	00	00	0	
	0 1 2 3 4 5 6 7 8 (



Part 3: Quantitative Comparison

Instructions: Compare the quantities in columns A and B. Shade in

- A if the quantity in column A is greater;
- B if the quantity in column B is greater;
- © if the quantities are equal; or
- ① if the relationship cannot be determined from the information given.

Column A

Column B

14.
$$(4 \cdot 1 - 4) + \frac{1}{5}(10 - 5)$$

$$(2+0)\left(\frac{1}{2}\right)+5(7-3\cdot 2)$$

(Lesson 1-4)

15. Let
$$u = 4$$
, $v = -3$, and $t = 2$.

(Lesson 2-4)

16. Let
$$\frac{x}{7} = \frac{12}{28}$$
.

$$\frac{1}{x}$$

(Lesson 3-6)

Other

18%

Carame

Strawberries

Hot Fudge 29%

SCORE ____

Unit 1 Test

(Chapters 1–3)

1. Write an algebraic expression for the difference of 5 and n cubed.

- 1. _____
- **2.** Evaluate $2x + 5y^2 3z$ if x = 6, y = 4, and z = 7.
- 2. _____
- **3.** Find the solution set for 3b-4=8 if the replacement set is $\{1, 2, 3, 4, 5\}$.
- 3. _____
- **4.** Name the property used in the equation 1 = 6n. Then find the value of n.
- 4. _____

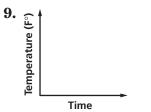
For Questions 5-7, simplify each expression.

5.
$$2t^2 + 5t^2 + 3t$$

6.
$$7(r+2t)-5t$$

7.
$$5(4a+b)+3a+b$$

- **8.** Identify the hypothesis and conclusion of the statement. Then write the statement in if-then form. *All triangles are polygons*.
- 8. _____
- **9.** Draw a reasonable graph showing the relationship between the temperature of a pizza as it is removed from an oven and placed on a counter at room temperature, and time.



10. A recent survey asked consumers to identify their favorite ice cream topping. The results are displayed in the circle graph. If 250 people were surveyed, how many chose strawberries as their favorite topping?



11. Graph {4, 5, 6, 7, 8, ...}.

11. -3-2-1 0 1 2 3 4 5 6 7 8

Find each sum, product, or quotient.

12.
$$31 + (-78)$$

13.
$$\left(-\frac{8}{9}\right)\left(\frac{3}{4}\right)$$

14.
$$37.6 \div (-8)$$

- **15.** A card is selected at random from a standard deck of 52 cards. What is the probability of selecting a diamond?
- 15. _____
- 16. Find the odds of rolling a number less than 6 on a die.
- 16

Unit 1 Test (continued)

For Questions 17 and 18, use the list that shows the number of hours Mrs. Wentworth's piano students spent practicing last week.

17. Make a line plot of the data.

17.

18. Which measure of central tendency best describes the data? Explain.

18. _____

19. Name the set or sets of numbers to which $\sqrt{48}$ belongs.

19. _____

20. Write $-3.\overline{65}$, $\sqrt{13}$, $\frac{75}{21}$, $-\frac{18}{5}$ in order from least to greatest.

20. _____

For Questions 21-27, solve each equation.

21.
$$m-5=-23$$

22.
$$-4 = 8 + k$$

23.
$$\frac{a}{2} + 9 = 30$$

24.
$$-\frac{2}{7}x = -16$$

25.
$$5(c+3) = 15 + 2(2c-1)$$

26.
$$10(a+1) - 14a = 9 - (4a-1)$$

27.
$$\frac{7}{10} = \frac{3}{x+1}$$

28. A magazine is on sale for 15% off the original price. If the original price of the magazine is \$4.60, what is the discounted price?

29. Solve
$$\frac{t-v}{r} = s$$
, for v .

30. How many pounds of peanuts costing \$3.00 a pound should be mixed with 4 pounds of cashews costing \$4.50 a pound to obtain a mixture costing \$3.50 a pound?

Standardized Test Practice

Student Record Sheet (Use with pages 186–187 of the Student Edition.)

Part 1 Multiple Choice

Select the best answer from the choices given and fill in the corresponding oval.

Part 2 Short Response/Grid In

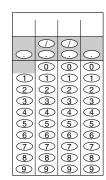
Solve the problem and write your answer in the blank.

For Questions 10, 12, and 14, also enter your answer by writing each number or symbol in a box. Then fill in the corresponding oval for that number or symbol.

10

0				
	0	00	90	0
		0	0	0
	1	1	1	1
	2	2	2	2
	3	3	3	3
	4	4	4	4
	(5)	(5)	(5)	(5)
	6	6	6	6
	\bigcirc	7	7	7
	8	8	8	8
	9	9	9	9

12



14

0	00	00	0
	0	0	0
1	1	1	1
2	2	2	2
3	3	3	3
4	4	4	4
(5)	(5)	(5)	(5)
6	6	6	6
7	7	7	7
8	8	8	8
9	9	9	9

Part 3 Quantitative Comparison

Select the best answer from the choices given and fill in the corresponding oval.

Part 4 Open-Ended

Record your answers for Questions 19-20 on the back of this paper.

Study Guide and Intervention Writing Equations 3-1

Write Equations Writing equations is one strategy for solving problems. You can use a variable to represent an unspecified number or measure referred to in a problem. Then you can write a verbal expression as an algebraic expression.

Example 2

sentence into an equation or a Translate each

- a. Ten times a number x is equal to 2.8 times the difference y minus z. The equation is 10x = 2.8(y - z). $10 \times x = 2.8 \times (y)$
- A number m minus 8 is the same as a number n divided by 2. $m-8=n\div 2$ The equation is $m-8=\frac{n}{2}$.
- The area of a rectangle equals the length times the width. Translate Formula: Area equals length times this sentence into a formula. Let A = area, $\ell = \text{length}$, and $A=\ell \times w$ The formula for the area of a rectangle is A =

The population of the United States in 2001 was about 284,000,000, and the land area of the United States is about 3,500,000 square miles. Find the average number of people per square mile in the United States. Use the Four-Step Problem-Solving Plan.

- Plan Write an equation to represent the situation. Let p represent the number of **Step 1** Explore You know that there are 284,000,000 people. You want to know the number of people per square mile. $3,500,000 \times p = 284,000,000$ people per square mile. Step 3 Step 2
- $3,500,000p = 284,000,000 \; {\rm Divide \; each \; side \; by}$ $n \approx 81 \; 14 \qquad 3,500,000.$ There about 81 people per square mile. Examine If there are 81 people per square mile and there are 3,500,000 Solve $3,500,000 \times p = 284,000,000$.

square miles, $81 \times 3,500,000 = 288,500,000$, or about 284,000,000 people. The answer makes sense. Step 4

Exercises

Franslate each sentence into an equation or formula.

- 1. Three times a number t minus twelve equals forty. 3t 12 = 40
- 2. One-half of the difference of a and b is 54. $\frac{1}{2}(a-b)=54$
- 3. Three times the sum of d and 4 is 32. 3(d + 4) = 32
- **4.** The area A of a circle is the product of π and the radius r squared. $A = \pi r^2$

WEIGHT LOSS For Exercises 5-6, use the following information.

ou wants to lose weight to audition for a part in a play. He weighs 160 pounds now. He wants to weigh 150 pounds.

- 5. If p represents the number of pounds he wants to lose, write an equation to represent this situation. 160 p = 150
- 6. How many pounds does he need to lose to reach his goal? 10 lb

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Writing Equations

(continued) Study Guide and Intervention

Write Verbal Sentences You can translate equations into verbal sentences

Translate each equation into a verbal sentence.

4n - 8 = 12Four times n minus eight equals twelve.

4n - 8 = 12.

Example

 $a^2+b^2 = c^2$ The sum of the squares of a and b is equal to the square of cb. $a^2 + b^2 = c^2$

L-E nossal

Franslate each equation into a verbal sentence.

4 times a minus 5 is equal to 23.

1. 4a - 5 = 23

2. 10 + k = 4k

The sum of 10 and k is equal to times k.

1. $x^2 + y^2 = 8$

The sum of the squares of x and y is equal to 8.

6 times the product of x and y is equal to 24.

3. 6xy = 24

6. $b = \frac{1}{3}(h-1)$

b is $\frac{1}{3}$ of the difference of h and 1.

The sum of p and 3 is equal to

5. p + 3 = 2p

2 times p.

8. 3(g+h)=12

3 times the sum of g and h is 12.

100 minus 2 times x is equal

7. 100 - 2x = 80

of the difference of ര|വ C is equal to F and 32. **10.** $C = \frac{5}{9}(F - 32)$

The square of p minus 2 times

p is equal

11. $V = \frac{1}{3}Bh$

9. $p^2 - 2p = 9$

12. $A = \frac{1}{2}hb$

of the product of -|0 A is equal to $\frac{1}{2}$ h and b.

₽

of the product

-|ღ

V is equal to B and B.

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Glencoe Algebra 1

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Glencoe Algebra 1

Answers

Translate each sentence into an equation. **Skills Practice** Writing Equations 3-1

1. Two added to three times a number m is the same as 18. 3m + 2 = 18

2. Twice a increased by the cube of a equals b. $2a + a^3 = b$

9 **3.** Seven less than the sum of p and q is as much as 6. (p + q) –

= 6g5. Four times the sum of f and g is identical to six times g. 4(f+g)**4.** The sum of x and its square is equal to y times z. $x + x^2 = yz$

Franslate each sentence into a formula.

6. The perimeter P of a square equals four times the length of a side s. P = 4s

7. The area A of a square is the length of a side s squared. $A = S^2$

8. The perimeter P of a triangle is equal to the sum of the lengths of sides a,b, and c.

9. The area A of a circle is pi times the radius r squared. $A = \pi r^2$

10. The volume V of a rectangular prism equals the product of the length ℓ , the width w, and the height h. $V=\ell wh$

Franslate each equation into a verbal sentence.

Twice *p* plus 4 times *q* is 20. 12. 2p + 4q = 20g plus 10 is the same as 3 times g. **13.** 4(a + b) = 9a11.g + 10 = 3g

8 minus 6 times x is 4 plus **14.** 8-6x=4+2x2 times x. 4 times the sum of a and b is 9 times a.

16. $s^2 - n^2 = 2b$

s squared minus n squared is twice b. Half of the sum of fand y is **15.** $\frac{1}{9}(f+y) = f-5$ f minus 5.

Write a problem based on the given information.

Sample answer: The cost of dinner plus a 15% tip was \$23. How much was the dinner? = cost of a 15% tip **18.** $p = \cos t$ of dinner $0.15p = \cos t$ of a 1 p + 0.15p = 23

> Sample answer: The cost of two pounds of plain coffee beans plus one pound of

 $c + 3 = \cos t \text{ per pound of flavored coffee beans}$

2c + (c + 3) = 21

17. c = cost per pound of plain coffee beans

flavored beans is \$21. How much does 33 1 pound of plain beans cost? Glencoe/McGraw-Hill

NAME

PERIOD

DATE

PERIOD

DATE

Practice (Average)

Writing Equations

Franslate each sentence into an equation.

1. Fifty-three plus four times c is as much as 21. 53 + 4c = 21

2. The sum of five times h and twice g is equal to 23. 5h + 2g = 23

4. Three plus the sum of the squares of w and x is 32. $3 + (w^2 + x^2) = 32$

3. One fourth the sum of r and ten is identical to r minus 4. $\frac{1}{4}(r+10) = r -$

Franslate each sentence into a formula.

5. Degrees Kelvin K equals 273 plus degrees Celsius C. K = 273 + C

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6. The total cost C of gas is the price p per gallon times the number of gallons g. C = pg

7. The sum S of the measures of the angles of a polygon is equal to 180 times the difference of the number of sides n and 2. S = 180(n-2)

Franslate each equation into a verbal sentence.

 $9. \, \frac{3}{5}t + 2 = t$ **8.** $q - (4 + p) = \frac{1}{3}q$ *q* **minus the sum** of 4 and p equals $\frac{1}{2}$ times q.

Two more than $\frac{3}{5}$ of tequals t.

11. 2(m-n)=v+7 Twice the quantity m minus n is v plus 7. **10.** $9(y^2 + x) = 18$ **9 times the sum** of y squared and x is 18.

Write a problem based on the given information. **12.** $a = \cos t$ of one adult's ticket to zoo

0.20c = amount of 20% promotional discount 3(c - 0.20c) = 33013. c = regular cost of one airline ticket $a-4=\cos t$ of one children's ticket to zoo Sample answer: The cost of two adult's tickets and 4 children's tickets to the zoo is \$38. How much is an adult's ticket? 2a + 4(a - 4) = 38

airline tickets that are discounted Sample answer: The cost of three 20% is \$330. What is the regular cost of a ticket? 14. GEOGRAPHY About 15% of all federally-owned land in the 48 contiguous states of the United States is in Nevada. If F represents the area of federally-owned land in these states, and N represents the portion in Nevada, write an equation for this situation.

FITNESS For Exercises 15-17, use the following information.

Deanna and Pietra each go for walks around a lake a few times per week. Last week, Deanna walked 7 miles more than Pietra. 15. If p represents the number of miles Pietra walked, write an equation that represents the total number of miles T the two girls walked. T = p + (p + 7)

16. If Pietra walked 9 miles during the week, how many miles did Deanna walk? 16 mi

17. If Pietra walked 11 miles during the week, how many miles did the two girls walk

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Glencoe Algebra 1

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Glencoe Algebra 1

Glencoe Algebra 1 PERIOD Show that each figure is a rep-tile by subdividing it into four smaller and Subdivide each rep-tile into nine smaller and similar figures. DATE A rep-tile is a figure that can be subdivided into smaller copies of itself. The large figure is similar to the small ones and the small figures are all congruent. 10. 142 **Enrichment** Glencoe/McGraw-Hill similar figures. Rep-Tiles ij 6 L-E nossal 2. A 1 oz serving of chips has 140 calories. There are about 14 servings of chips in a bag. How many calories are there in a bag of chips? Write what your solution would be as you Glencoe Algebra 1 Read the introduction to Lesson 3-1 at the top of page 120 in your textbook. Yes; the total height minus the height of the statue itself gives the height of the pedestal. 3. If you cannot remember all the steps of the Four-Step Problem-Solving Plan, try to remember the first letters of the first word in each step. Write those letters here with Does the equation 305 - s = 154 also represent the situation? Explain. PERIOD 140 \cdot 14 = 1960; There are 1960 calories in a bag of chips. A 1 oz serving of chips has 140 calories and there are 14 servings of chips in a bag. × × times Reading to Learn Mathematics four 4 Pre-Activity How are equations used to describe heights? divided by How many calories are in a bag of chips? ednals II use each step in the Four-Step Problem-Solving Plan. four 4

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EPSE; Explore, Plan, Solve, Examine

Does your answer make sense?

Examine

See students' work.

Helping You Remember

What do you want to know?

Write an equation.

Plan

Solve the problem.

Solve

What do you know?

Explore

minus

the sum of x and three

times ×

Two

ä

(x + 3)

Translate each sentence into an equation.

Reading the Lesson

Writing Equations

3-1

×

two

<u>.s</u>

The difference of k and 3

þ.

k-3

Answers

Study Guide and Intervention

Solving Equations by Using Addition and Subtraction

Solving Equations by Using Addition and Subtraction

Study Guide and Intervention

(continued)

Solve Using Subtraction If the same number is subtracted from each side of an equation, the resulting equation is equivalent to the original one. In general if the original equation involves addition, this property will help you solve the equation.

Subtraction Property of Equality | For any numbers a, b, and c, if a = b, then a - c = b - c.

Subtract 22 from each side.

22 + p - 22 = -12 - 22

22 + p = -12

The solution is -34.

Solve 22 + p = -12.

Example

Solve Using Addition If the same number is added to each side of an equation, the resulting equation is equivalent to the original one. In general if the original equation involves subtraction, this property will help you solve the equation.

Addition Property of Equality | For any numbers a, b, and c, if a=b, then a+c=b+c.

Solve m - 32 = 18. Example 1

m - 32 = 18m - 32 + 32 = 18 + 32

Add 32 to each side. Simplify.

The solution is 50.

Exercises

Solve -18 = p - 12. Example 2

Add 12 to each side. -18 + 12 = p - 12 + 12-18 = p - 12

The solution is -6.

Solve each equation. Then check your solution. **4.** s + (-9) = 7 **16** 1. x + 12 = 6 - 6

$$\mathbf{5.} - 3.2 = \ell + (-0.2)$$

3.
$$-17 = b + 4$$
 -21
6. $-\frac{3}{8} + x = \frac{5}{8}$ 1

9

8.
$$-12 = k + 24$$

7. 19 + h = -4 -23

-36

9.
$$j + 1.2 = 2.8$$
 1.6
12. $w + \frac{3}{2} = \frac{5}{8} - \frac{7}{8}$

11. m + (-8) = 2 10

10. b + 80 = -80 - 160

13. Twelve added to a number equals 18. Find the number: n + 12 = 18;

Write an equation for each problem. Then solve the equation and check the

14. What number increased by 20 equals -10? n + 20 = -10;

15. The sum of a number and fifty equals eighty. Find the number. n+50=80;30

16. What number plus one-half is equal to four? $n + \frac{1}{2} = 4$; $3\frac{1}{2}$

17. The sum of a number and 3 is equal to -15. What is the number? n + 3 = -15; -18

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3. p - 5 = 15 20

2. m-8=-12 -4

Solve each equation. Then check your solution.

5. k - 0.5 = 2.3 **2.8**

6. $w - \frac{1}{2} = \frac{5}{8} \cdot 1\frac{1}{8}$

9.j - 0.2 = 1.8 2

8. -12 = -24 + k 12

7. h - 18 = -17 1

12. $w - \frac{3}{2} =$ 11. m - (-12) = 10 -2

10. b - 40 = -40

Write an equation for each problem. Then solve the equation and check the solution.

13. Twelve subtracted from a number equals 25. Find the number. n-12=25;37

14. What number decreased by 52 equals -12? n - 52 = -12; 40

15. Fifty subtracted from a number equals eighty. Find the number. n-50=80;130

16. What number minus one-half is equal to negative one-half? $n - \frac{1}{2} = -\frac{1}{2}$; 17. The difference of a number and eight is equal to 14. What is the number?

18. A number decreased by fourteen is equal to eighteen. What is the number? n - 14 = 18;32

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Glencoe Algebra 1

4. 20 = y - 8 **28**

DATE **Skills Practice**

Solving Equations by Using Addition and Subtraction

Solve each equation. Then check your solution.

1.
$$y - 7 = 8$$
 15

3.
$$p-4=6$$
 10

2.
$$w + 14 = -8$$
 -22

5.
$$98 = b + 34$$
 64

4.
$$-13 = 5 + x$$
 -18

$$7.s + (-28) = 0$$
 28

6.
$$y - 32 = -1$$
 31

8.
$$y + (-10) = 6$$
 16

9.
$$-1 = s + (-19)$$
 18

$$10.j - (-17) = 36 19$$

11.
$$14 = d + (-10)$$
 24

$$y_{\bullet} j - (-17) = 36 \text{ } 19$$

13.
$$11 = -16 + y$$
 27

$$12. \ u + (-5) = -15 \ -10$$

15.
$$47 = w - (-8)$$
 39

16.
$$x - (-74) = -22$$
 -96

14. c - (-3) = 100 97

17.
$$4 - (-h) = 68$$
 64

18.
$$-56 = 20 - (-e)$$
 -76

Write an equation for each problem. Then solve the equation and check your

- 19. A number decreased by 14 is -46. Find the number. n 14 = -46; -32
- 20. Thirteen subtracted from a number is -5. Find the number. n-13=-5; 8
- 21. The sum of a number and 67 is equal to -34. Find the number. n + 67 = -34; -101
- **22.** What number minus 28 equals -2? n 28 = -2; 26
- **23.** A number plus -73 is equal to 27. What is the number? n + (-73) = 27; 100
- **24.** A number plus -17 equals -1. Find the number. n + (-17) = -1; 16
- **25.** What number less 5 is equal to -39? n-5=-39; -34

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Practice (Average)

DATE

Solving Equations by Using Addition and Subtraction

Solve each equation. Then check your solution.

1.
$$d - 8 = 17$$
 25 2. $v -$

4. -16 = s + 71 **-87**

7.8 -(-c) = 1 -7

2.
$$v + 12 = -5$$

3. b-2=-11

5.
$$29 = a - 76$$
 105

6.
$$-14 + y = -2$$
 12
9. $f + (-3) = -9$ -6
12. $4.6 - (-b) = -0.4$ -5

8.
$$78 + r = -15 - 93$$

11.
$$w + 1.9 = -2.5$$
 -4.4 12. 4.

$$1.9 = -2.5$$
 -4.4 $0.13 = -0.58$ -0.45

14.
$$a - 0.13 = -0.58$$
 -0.45 15 17. $\frac{5}{9} + q = \frac{2}{3} \frac{1}{9}$ **18**

13. y - (-1.5) = 0.5 -1 10. 4.2 = n + 7.3 - 3.1

.58 **-0.45** 15.
$$k + (-4)$$
 18. $\frac{1}{2} = h + (-4)$

0.45 15.
$$k + (-4.21) = -19$$

18. $\frac{1}{3} = h + \frac{2}{5} - \frac{1}{15}$
21. $-\frac{7}{8} - (-n) = -\frac{7}{12} \frac{7}{24}$

20.
$$y + \frac{4}{5} = \frac{3}{4} - \frac{1}{20}$$
 21. $-\frac{7}{8} - (-n) = -\frac{1}{8}$

Write an equation for each problem. Then solve the equation and check your solution.

19. $\frac{1}{4} + x = -\frac{7}{12} - \frac{5}{6}$

 $16. \ r + \frac{1}{5} = \frac{9}{10} \ \frac{7}{10}$

23. A number plus 15 equals -12. What is the number? n + 15 = -12; -27

22. What number minus 9 is equal to -18? n-9=-18;

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- **24.** The sum of a number and -3 is equal to -91. Find the number. n + (-3) = -91; -88
- 25. Negative seventeen equals 63 plus a number. What is the number? -17 = 63 + n; -80
- **26.** The sum of negative 14, a number, and 6 is -5. What is the number? -14 + n + 6 = -5; 3

27. What number plus one half is equal to three eighths? $n + \frac{1}{2} = \frac{3}{8}$.

HISTORY For Exercises 28 and 29, use the following information.

Galileo Galilei was born in 1564. Many years later, in 1642, Sir Isaac Newton was born.

- 28. Write an addition equation to represent the situation. 1564 + y = 1642
- 29. How many years after Galileo was born was Isaac Newton born? 78

HURRICANES For Exercises 30 and 31, use the following information.

The day after a hurricane, the barometric pressure in a coastal town has risen to 29.7 inches of mercury, which is 2.9 inches of mercury higher than the pressure when the

- **30.** Write an addition equation to represent the situation. b + 2.9 = 29.7
- 31. What was the barometric pressure when the eye passed over? 26.8 in. of mercury

Answers

Pre-Activity How can equations be used to compare data?

Solving Equations by Using Addition and Subtraction Reading to Learn Mathematics

Read the introduction to Lesson 3-2 at the top of page 128 in your textbook. In the equation m-66=5, the number 5 represents

the difference between the percent of growth for medical assistants and the percent of growth for travel agents,

the rate of growth for travel agents. and the number 66 represents

7-E uossa7

1. To solve x+17=46 using the Subtraction Property of Equality, you would subtract from each side

Reading the Lesson

To solve y-9=-30 using the Addition Property of Equality, you would add to each side.

3. Write an equation that you could solve by subtracting 32 from each side.

Sample answer: m + 32 = 50

4. A student used the Subtraction Property of Equality to solve an equation. Explain why it would also be possible to use the Addition Property of Equality to solve the equation. Subtracting one number from another gives the same result as adding the opposite of the number that was subtracted

Helping You Remember

5. Explain how you decide whether to use the Addition Property or the Subtraction

Sample answer: If the given equation has a number added to the variable, then use the Subtraction Property of Equality. If the equation has a number subtracted from the variable, then use the Addition Property of Equality.

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PERIOD

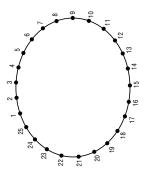
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Enrichment

Counting-Off Puzzles

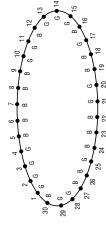
Solve each puzzle.

1. Twenty-five people are standing in a circle. Starting with person 1, they count off from person who says "7" drops out of the circle. Who is the last person left? number 15 1 to 7 and then start over with 1. Each



person drops out. Which two people are the last ones left? 13th and 28th people 2. Forty people stand in a circle. They count off so that every third

Sharon's class can go on a field 3. Only half of the 30 students in off from 1 to 9 and every ninth 15 people are left. Who gets to go on the field trip. the girls trip. Sharon arranges the boys person drops out until only



A group of people stand in a circle and count off 1, 2, 1, 2, 1 and so on. Every second person drops out. Person number 1 is the last person left.

circle must be even. Then, explain your answer. If the numbe is odd, person 1 would drop out after the first round. 4. Draw a diagram to show why the number of people in the

5. When the count returns to person number 1 for the first time, how many people have dropped out? half of the original number

6. Find the number of people in the circle if the number is between 10 and 20. Do the same if the number is between 30 and 40. What can you conclude about the original number of people? 16; 32; The number must be a power of 2.

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Study Guide and Intervention <u>ო</u>-ო

Solving Equations by Using Multiplication and Division

Solve Using Multiplication If each side of an equation is multiplied by the same number, the resulting equation is equivalent to the given one. You can use the property to solve equations involving multiplication and division.

Multiplication Property of Equality For any numbers a, b, and c, if a=b, then ac=bc.

Solve $3\frac{1}{2}p = 1\frac{1}{2}$. Example 1

Solve
$$3\frac{p}{2}p = 3\frac{1}{2}$$
 Original equation 7

Rewrite again mixed number as an improper fraction.

3 Rewrite as mixed number as an improper fraction.

$$\frac{3}{2}$$
 Multiply each side by $\frac{7}{7}$.

$$\left(-\frac{2}{7} \left(\frac{3}{2} \right) \right)$$
 Multiply each $p = \frac{3}{7}$ Simplify.

te solution is
$$\frac{3}{7}$$
.

The solution is

$Solve -\frac{1}{4}n = 16.$ Example 2

$$-rac{1}{4}n=16$$
 Original equation
$$-4\Big(-rac{1}{4}n\Big)=-4(16)$$
 Multiply each side by -4

$$n = -64$$
 Simpli The solution is -64 .

Solve each equation. Then check your solution.

1.
$$\frac{h}{3} = -2$$
 -6

9

4. $5 = \frac{y}{12}$ (

2.
$$\frac{1}{8}m = 6$$
 48 5. $-\frac{1}{4}k = -2.5$ **10**

3.
$$\frac{1}{5}p = \frac{3}{5}$$
 3 6. $-\frac{m}{8} = \frac{5}{8}$

-2

$$9. \frac{j}{3} = \frac{2}{5} \cdot 1\frac{1}{5}$$

œ

8. $-12 = -\frac{3}{2}k$

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7. $-1\frac{1}{2}h = 4$

12.
$$\frac{p}{5} = -\frac{1}{4} - 1\frac{1}{4}$$

11. $\frac{7}{10}m = 10$ 14 $\frac{2}{7}$

 $10. -3\frac{1}{3}b = 5 -1\frac{1}{2}$

F-E nossal

Write an equation for each problem. Then solve the equation.

- 13. One-fifth of a number equals 25. Find the number. $\frac{1}{5}n = 25$; 125
- **14.** What number divided by 2 equals -18? $\frac{n}{2} = -18$; -36
- 15. A number divided by eight equals 3. Find the number. $\frac{n}{8} = 3$; 24
- 16. One and a half times a number equals 6. Find the number: $1\frac{1}{2}n = 6$; 4

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Solving Equations by Using Multiplication and Division (continued) Study Guide and Intervention 3-3

Solve Using Division To solve equations with multiplication and division, you can also use the Division Property of Equality. If each side of an equation is divided by the same number, the resulting equation is true.

Division Property of Equality

Solve -5n = 60. Divide each side by -5. 0.0 Original equation For any numbers a, b, and c, with $c \neq 0$, if a = b, then $\frac{a}{c}$. Example 2 9 = -5n = 60-5nSolve 8n = 64.

Example 1

8n = 64 $\frac{8n}{8} = \frac{64}{8}$ Simplify.

n = -12

Divide each side by 8. Original equation

Simplify.

n = 8

The solution is 8.

The solution is -12.

Exercises

Solve each equation. Then check your solution.

1.
$$3h = -42$$
 -14

-3r = -24

6.
$$-2m = 16$$
 —

3. -3t = 51

8.
$$-2.4p = 7.2$$

-|ღ

7. 12h = 4

9.0.5j = 5.10

12.
$$-1.5p = -75$$
 50

11. $6m = 152\frac{1}{2}$

10. -25 = 5m

Write an equation for each problem. Then solve the equation.

- 13. Four times a number equals 64. Find the number. 4n = 64; 16
- 14. What number multiplied by -4 equals -16? -4n = -16; 4
- 15. A number times eight equals -36. Find the number. 8n = -36; $-4\frac{1}{2}$

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Exercises

Answers

DATE

Skills Practice

Solving Equations by Using Multiplication and Division

Solve each equation. Then check your solution.

1.
$$12z = 108$$
 9

2.
$$-7t = 49 - 7$$

$$12z = 108$$
 9

4.
$$-22 = 11v$$
 -2

$$5. -6d = -42$$
 7

3. 18*e* = -216 **-12**

6.
$$96 = -24a$$
 -4

7.
$$\frac{c}{4} = 16$$
 64

8.
$$\frac{a}{16} = 9$$
 144

$$9. - 84 = \frac{d}{3} - 252$$

$$11. \frac{t}{4} = -13 - 52$$

10.
$$-\frac{d}{7} = -13$$
 91

12.
$$31 = -\frac{1}{6}n$$
 -186

13.
$$-6 = \frac{2}{3}z$$
 -9
15. $\frac{5}{9}p = -10$ -18

14.
$$\frac{2}{7}q = -4$$
 -14

$$16. \ \frac{a}{10} = \frac{2}{5} \ 4$$

18.
$$1.6m = -4$$
 -2.5

17. -0.4b = 5.2 - 13

Write an equation for each problem. Then solve the equation.

- **19.** The opposite of a number is -9. What is the number? -n = -9; 9
- 20. Fourteen times a number is -42. Find the number. 14n = -42; -3
- 21. Eight times a number equals 128. What is the number? 8n = 128; 16
- 22. Negative twelve times a number equals -132. Find the number. -12n = -132; 11
- 23. Negative eighteen times a number is -54. What is the number? -18n = -54; 3
- 24. One sixth of a number is -17. Find the number: $\frac{1}{6}n = -17$; -102
- 25. Negative three fifths of a number is -15. What is the number? $-\frac{3}{5}n = -15$; 25

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Practice (Average)

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Solving Equations by Using Multiplication and Division

Solve each equation. Then check your solution

1.
$$8j = 96$$
 12

4. 243 = 27c **9**

7. $\frac{a}{15} = \frac{4}{5}$ 12

2.
$$-13z = -39$$
 3
5. $\frac{y}{9} = -8$ -72

3.
$$-180 = 15m - 12$$

6. $-\frac{j}{12} = -8$ 96

9.
$$\frac{q}{24} = \frac{1}{6}$$
 4. 12. $-\frac{3}{8}s = 4$ - 13.

9

0 | 2 **8.** $\frac{g}{27} = ...$

12.
$$-\frac{3}{15}s = 4$$
 -20
15. $\frac{5}{3}h = \frac{11}{6} \frac{11}{10}$

11. $-\frac{3}{8}w = -9$ 24

$$15.5 \frac{5}{3}h$$

0 2

14. $\frac{8}{5}\alpha = \frac{4}{3}$

 $13. -3x = \frac{3}{2} - \frac{1}{2}$ $10. -1 = -\frac{4}{7}t \frac{7}{4}$

 $16. \ 5n = \frac{11}{4} \ \frac{11}{20}$

18.
$$-3.4e = -3.74$$
 1.1

17.
$$2.5k = 20$$
 8
20. $0.26p = 0.104$ **0.4**

21.
$$4.2a = -3.36$$

21.
$$4.2q = -3.36$$
 -0.8

19. -1.7b = 2.21 **-1.3**

Write an equation for each problem. Then solve the equation.

- 22. Negative nine times a number equals -117. Find the number. -9n = -117; 13
- 23. Negative one eighth of a number is $-\frac{3}{4}$. What is the number? $-\frac{1}{8}n = -\frac{3}{4}$; 6
- 24. Five sixths of a number is $-\frac{5}{9}$. Find the number: $\frac{5}{6}n = -\frac{5}{9}$; $-\frac{2}{3}$
- **25.** 2.7 times a number equals 8.37. What is the number? 2.7n = 8.37; 3.1

resson 3-3

26. One and one fourth times a number is one and one third. What is the number?

27. PUBLISHING Two units of measure used in publishing are the pica and the point. A pica is one sixth of an inch. There are 12 points in a pica, so Points = $12 \cdot \text{Picas}$. How many picas are equivalent to 108 points? 9 picas $1\frac{1}{4}n = 1\frac{1}{3}; 1\frac{1}{15}$

ROLLER COASTERS For Exercises 28 and 29, use the following information.

Superman the Escape in California is the fastest roller coaster in the world. Riders fall 415 feet in 7 seconds. Speeds reach a maximum of 100 miles per hour.

- **28.** If x represents the average rate of fall of the roller coaster, write an expression to represent the situation (*Hint*: Use the distance formula d = rt.) 7x = 415
- 29. What is the average rate that riders fall in feet per second? about 59.3 ft/s

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Solving Equations by Using Multiplication and Division Reading to Learn Mathematics

Pre-Activity How can equations be used to find how long it takes light to reach Earth?

Read the introduction to Lesson 3-3 at the top of page 135 in your textbook.

• In the equation d=rt, shown in the introduction, what number is used

5,870,000,000,000; 311,110,000,000,000

• What equation could you use to find the time it takes light to reach Earth from the farthest star in the Big Dipper?

5,870,000,000,000t = 821,800,000,000,000

Reading the Lesson

Complete the sentence after each equation to tell how you would solve the equation.

1.
$$\frac{x}{7} = 16$$
 Multiply each side by

1.
$$\frac{7}{7} = 16$$
 with ply each side by 7. 2. $5x = 125$ Divide each side by 5, or multiply each side by

3.
$$-8k = 96$$
 Divide each side by $\frac{-8}{}$, or multiply each side by

It makes it easier for you to see what number you need to multiply by 4. Explain how rewriting $4\frac{1}{3}x = 2\frac{1}{8}$ as $\frac{13}{3}x = \frac{17}{8}$ helps you solve the equation.

Helping You Remember

5. One way to remember something is to explain it to someone else. Write how you would Sample answer: Multiply each side of the equation by the reciprocal of explain to a classmate how to solve the equation $\frac{2}{3}x = 12$.

 $\frac{2}{3}$ so you can isolate x on the left side.

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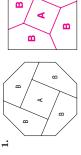
3-3

Enrichment

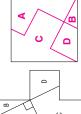
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Dissection Puzzles: Make the Square

In a dissection puzzle, you are to cut apart one figure using only straight cuts and then rearrange the pieces to make a new figure. Usually the puzzle-solver must figure out where to make the given number of cuts. However, for these pizzles, the cut lines are shown. You must discover how to rearrange the pieces. Cut apart each figure. Then rearrange the pieces to form a square.











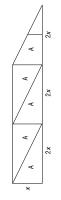
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4. Hint: Cut one of the triangles into two pieces to make this square.



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3. Eight is subtracted from a number, and then the difference is multiplied by 2. The result is 24. Find the number. 20 A number is multiplied by 5, and then 3 is subtracted from the product. The result is 12. 1. A number is divided by 3, and then 4 is added to the quotient. The result is 8. Find the number. 12 4. Three times a number plus 3 is 24. Find the number. Solve each problem by working backward. The original number is 48. Find the number. is the number? Exercises number.

Study Guide and Intervention

Solving Multi-Step Equations

Work Backward Working backward is one of many problem-solving strategies that you can use to solve problems. To work backward, start with the result given at the end of a problem and undo each step to arrive at the beginning number.

A number is divided by 2, and then 8 is subtracted from the quotient. The result is 16. What

Solve the problem by working backward. subtracting 8 by adding 8 to get 24. To undo dividing 24 by 2, multiply 24 by 2 The final number is 16. Undo

A bacteria culture doubles 6400 bacteria. How many bacteria were each half hour. After 3 hours, there are there to begin with? Example 2

The bacteria have grown for 3 hours. Since there are 2 one-half hour periods in one hour, in 3 hours there are 6 one-half hour periods. Since the bacteria culture has grown for 6 time periods, it has doubled 6 times. Undo the doubling by halving the number of bacteria 6 times. Solve the problem by working backward.

6,400
$$\times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = 6,400 \times \frac{1}{64}$$

There were 100 bacteria to begin with.

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5. CAR RENTAL Angela rented a car for \$29.99 a day plus a one-time insurance cost of \$5.00. Her bill was \$124.96. For how many days did she rent the car? 4 days

MONEY Mike withdrew an amount of money from his bank account. He spent one fourth for gasoline and had \$90 left. How much money did he withdraw? \$120

7. TELEVISIONS In 1999, 68% of households with TV's subscribed to cable TV. If 8,000 more subscribers are added to the number of households with cable, the total number of households with cable TV would be 67,600,000. How many households were there with TV in 1999? Source World Manage 99,400,000 households 3lencoe Algebra 1

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3-4

Study Guide and Intervention Solving Multi-Step Equations

(continued)

Solve Multi-Step Equations To solve equations with more than one operation, often called **multi-step equations**, undo operations by working backward. Reverse the usual order of operations as you work.

Solve 5x + 3 = 23. Example

$$5x + 3 = 23$$
 Original equation.
$$5x + 3 - 3 = 23 - 3$$
 Subtract 3 from each side.
$$5x = 20$$
 Simplify.
$$\frac{5x}{5} = \frac{20}{5}$$
 Divide each side by 5.
$$x = 4$$
 Simplify.

Exercises

Solve each equation. Then check your solution.

1.
$$5x + 2 = 27$$
 5

5.
$$0.6x - 1.5 = 1.8$$
 5.5

က

4. 14n - 8 = 34

6.
$$\frac{7}{8}p-4=10$$

3. 5x + 16 = 51

က

2. 6x + 9 = 27

9

9.
$$\frac{g}{-5} + 3 = -13$$
 80

= 13 20

 $\frac{3n}{12}$

* * *

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7. $16 = \frac{d-12}{1}$

12.
$$3.2y - 1.8 = 3$$
 1.5

30

-2

00

11. 0.2x

_7

= 10

10. $\frac{4b+8}{-2}$:

15.
$$0 = 10y - 40$$
 4

80

4 T

14. 8 = -12 +

13. $-4 = \frac{7x - (-1)}{-8} = 4\frac{3}{7}$

Write an equation and solve each problem.

16. Find three consecutive integers whose sum is 96. n + (n + 1) + (n + 2) = 96;31,32,33

n + (n + 2) = 176; 87, 89

Find three consecutive integers whose sum is -93.

$$n + (n + 1) + (n + 2) = -93; -32, -31, -30$$

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10. $\frac{b}{3} - 6 = -2$ **12**

7. 15t + 4 = 49 3

NAME	Skills Practice	Solving Multi-Step Equatio
	3-4	

ns

Solve each problem by working backward

- 1. A number is divided by 2, and then the quotient is added to 8. The result is 33. Find the number. 50
- $\bf 2.$ Two is subtracted from a number, and then the difference is divided by 3. The result is 30. Find the number: $\bf 92$
- 3. A number is multiplied by 2, and then the product is added to 9. The result is 49. What is the number? 20
- bought himself a snack for \$1.25. When he arrived home, he had \$5.00 left. How much 4. ALLOWANCE After Ricardo received his allowance for the week, he went to the mall with some friends. He spent half of his allowance on a new paperback book. Then he

Solve each equation. Then check your solution.

5.
$$5x + 3 = 23$$
 4

6.
$$4 = 3a - 14$$
 6

7. 2y + 5 = 19 7

9.
$$8 - 5w = -37$$
 9 10. $18 - 4v = 42$ **12.** $5 + \frac{x}{4} = 1$ **-16 13.** $-\frac{h}{3} - 4 = 13$

13.
$$-\frac{h}{3} - 4 = 13$$
 -51

16.
$$\frac{w}{7} + 3 = -1$$
 -2
19. $\frac{5}{2}z - 8 = -3$ 2

-27

 $\frac{2}{3}g + 6 = -12$

18

17. $\frac{3}{4}q - 7 = 8$ 20

21. $\frac{c-5}{4} = 3$ **17**

20. $\frac{4}{5}m + 2 = 6$ **5**

 $\frac{a}{5} - 2 = 9$ 55

15.

14. $-\frac{d}{6} + 12 = -7$ 114

19.
$$\frac{2}{2}z - o - o 2$$
 22. $\frac{b+1}{3} = 2$ **5**

Write an equation and solve each problem.

- 23. Twice a number plus four equals 6. What is the number? 2n + 4 = 6; 1
- 24. Sixteen is seven plus three times a number. Find the number. 16 = 7 + 3n; 3
- 25. Find two consecutive integers whose sum is 35. n + (n + 1) = 35; 17, 18
- **26.** Find three consecutive integers whose sum is 36. n + (n + 1) + (n + 2) = 36; 11, 12, 13

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Solving Multi-Step Equations Practice (Average)

Solve each problem by working backward.

- 1. Three is added to a number, and then the sum is multiplied by 4. The result is 16. Find
- 2. A number is divided by 4, and the quotient is added to 3. The result is 24. What is the number? 84
- another stationed a few feet away. Three more birds flew into the branches of a nearby tree. Four birds remained at the feeder. How many birds were at the feeder initially? 12 4. BIRD WATCHING While Michelle sat observing birds at a bird feeder, one fourth of the 3. Two is subtracted from a number, and then the difference is multiplied by 5. The result is 30. Find the number. 8 birds flew away when they were startled by a noise. Two birds left the feeder to go to

Solve each equation. Then check your solution.

5.
$$-12n - 19 = 77$$
 -8

8. $\frac{u}{5} + 6 = 2$ -20

N

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11. $\frac{1}{2}y - \frac{1}{8} = -\frac{1}{8}$

6.
$$17 + 3f = 14 - 1$$

9.
$$\frac{d}{-4} + 3 = 15 - 48$$

12.
$$-32 - \frac{3}{5}f = -17$$
 -25
15. $\frac{15 - a}{2} = -9$ **42**

32

13. $8 - \frac{3}{8}k = -4$ 16. $\frac{3k-7}{2}$

15.
$$\frac{15-a}{3} = -9$$
 42

18.
$$2.5g + 0.45 = 0.95$$
 0.2 19. $0.4m$

19.
$$0.4m - 0.7 = 0.22$$
 2.3

= 16 29

17. $\frac{x}{7} - 0.5 = 2.5$ 21

14. $\frac{r+13}{12} = 1$ -1

Write an equation and solve each problem.

- 20. Seven less than four times a number equals 13. What is the number? 4n-7=13;5
- **21.** Find two consecutive odd integers whose sum is 116. n + (n + 2) = 116; 57,

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- 64 22. Find two consecutive even integers whose sum is 126. n + (n + 2) = 126; 62,
- 23. Find three consecutive odd integers whose sum is 117. n + (n + 2) + (n + 4) = 117; 37, 39, 41
- 24. COIN COLLECTING Jung has a total of 92 coins in his coin collection. This is 8 more than three times the number of quarters in the collection. How many quarters does Jung have in his collection? 28

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8. 6+5c=-29

Answers

Reading to Learn Mathematics

Solving Multi-Step Equations

Read the introduction to Lesson 3-4 at the top of page 142 in your textbook. Pre-Activity How can equations be used to estimate the age of an animal?

- Write the equation 8 + 12a = 124 in words.
- Eight plus twelve times a equals one hundred twenty-four.
- How many operations are involved in the equation? two

Reading the Lesson

- Using the opposite operations in the opposite order undoes the operations; subtraction undoes addition. 1. What does the phrase undo the operations mean to you? Give an example
- 2. a. If we undo operations in reverse of the order of operations, what operations do we do first? addition or subtraction
 - b. What operations do we do last? multiplication or division
- Suppose you want to solve $\frac{x+3}{5} = 6$.
- a. What is the grouping symbol in the equation $\frac{x+3}{5}=6$? the fraction bar b. What is the first step in solving the equation? Multiply each side by 5.
- c. What is the next step in solving the equation? Subtract 3 from each side.
- 4. Write an equation for the problem below.

-47	II	2	ı	K	•	7
negative forty-seve	equals	five	minus	K	times	Seven
				•	•	

ue,

Helping You Remember

5. Explain why working backward is a useful strategy for solving equations.

Sample answer: You can undo the operations to get back to the value of the variable that will make the equation true. That value is the solution.

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NAME 3-4

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Enrichment

Consecutive Integer Problems

Many types of problems and puzzles involve the idea of consecutive integers. Knowing how to represent these integers algebraically can help to solve the problem.

Example Find four consecutive odd integers whose sum is -80.

If 2n + 1 is the first odd integer, then add 2 to get the next largest odd An odd integer can be written as 2n + 1, where n is any integer.

(2n + 1) + (2n + 3) + (2n + 5) + (2n + 7) = -80Now write an equation to solve this problem.

Write an equation for each problem. Then solve.

- 1. Complete the solution to the problem in the example.
- 2n + (2n + 2) + (2n + 4) = 132; n = 21; 42, 44, 46 2. Find three consecutive even integers whose sum is 132.
- 3. Find two consecutive integers whose sum is 19.

$$n + (n + 1) = 19; 9, 10$$

- 4. Find two consecutive integers whose sum is 100. n + (n + 1) = 100; no solution
- 5. The lesser of two consecutive even integers is 10 more than one-half the greater. Find the integers.

$$2n = 10 + \frac{1}{2}(2n + 2)$$
; 22 and 24

6. The greater of two consecutive even integers is 6 less than three times the lesser. Find the integers.

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$$2n + 2 = 3(2n) - 6; 4, 6$$

7. Find four consecutive integers such that twice the sum of the two 2[(n + 2) + (n + 3)] = 3n + 91; 81, 82, 83, 84 greater integers exceeds three times the first by 91

8. Find a set of four consecutive positive integers such that the greatest integer in the set is twice the least integer in the set. n+3=2n; {3, 4, 5, 6}

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3. 3(a+1)-5=3a-2

all numbers **6.** 4(p+3)=36

PERIOD Study Guide and Intervention 3-5

Variables on Each Side To solve an equation with the same variable on each side, first use the Addition or the Subtraction Property of Equality to write an equivalent equation that has the variable on just one side of the equation. Then solve the equation.

Solving Equations with the Variable on Each Side

Solve 5y - 8 = 3y + 12. 33 5y - 8 = 3y + 125y - 8 - 3y = 3y + 12 - 32y - 8 = 12-8+8=12+82y = 20 $\frac{2y}{2} = \frac{20}{2}$ y = 10The solution is 10. Example 1 8

Example 2 Solve -11 - 3y = 8y + 1. -11 - 3y + 3y = 8y + 1 + 3y-11 - 1 = 11y + 1 - 1-11 = 11y + 1-11 - 3y = 8y + 1-12 = 11yThe solution is $-1\frac{1}{11}$. $-1\frac{1}{11}=y$

Solve each equation. Then check your solution.

3. $5x + 2 = 2x - 10$	-4	6. $4.4s + 6.2 = 8.8s - 1$	20 11	9. 8 $-5p = 4p - 1$	-	12. $3y - 1.8 = 3y - 1.8$
2. $5y - 2y = 3y + 2$	no solution	5. $1.2x + 4.3 = 2.1 - x$	۲	$\mathbf{8.\frac{3}{4}}k-5=\frac{1}{4}k-1$	80	11. $0.2x - 8 = -2 - x$
1. $6-b=5b+30$	-4	4. $4n-8=3n+2$	10	7. $\frac{1}{2}b + 4 = \frac{1}{8}b + 88$	224	10. $4b - 8 = 10 - 2b$

10.
$$4b - 8 = 10 - 2b$$
 11. 0
3
3
13. $-4 - 3x = 7x - 6$ 14. 8
5

$$16.\frac{2}{3}n + 8 = \frac{1}{2}n + 2$$

$$-36$$

$$\mathbf{6.} \frac{2}{3}n + 8 = \frac{1}{2}n + 2$$

$$-36$$

$$19. -4 - 3x = 6x$$

$$9. -4 - 3x = 6x - 6$$

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$$\frac{1}{2} + 8 = \frac{1}{2}n + 2$$
 17.

$$6x - 6$$
 20

20.
$$18 - 4k = -10 - 4k$$
 no solution

Exercises

$$= 5b + 30$$
2. $5y - 2y = 3y + 2$
3. $5x + 2 = 2x - 10$
no solution -4

$$8 = 3n + 2$$
5. $1.2x + 4.3 = 2.1 - x$
6. $4.4s + 6.2 = 8.8s - 1.8$

11.
$$0.2x - 8 = -2 - x$$

14.
$$8 + 4k = -10 + k$$

15. 20 - a = 10a all numbers

$$17. \frac{2}{5}y - 8 = 9 - \frac{3}{5}y$$

18. -4r + 5 = 5 - 4r

all numbers

$$\frac{5}{3}$$
 $\frac{2}{3}$ $\frac{2}{3}$ $\frac{2}{3}$ $\frac{1}{3}$ $\frac{2}{3}$ $\frac{1}{3}$ $\frac{1}$

$$9. -4 - 3x = 6x - 6$$

$$9. -4 - 3x = 6x - 6$$

$$-4 - 3x = 6x - 6$$

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21. 12 + 2y = 10y - 12

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Solving Equations with the Variable on Each Side Study Guide and Intervention (continued)

3-5

Grouping Symbols When solving equations that contain grouping symbols, first use the Distributive Property to eliminate grouping symbols. Then solve.

Example Solve $4(2a-1) = -10(a-5)$.	-10(a-5).
4(2a-1) = -10(a-5)	Original equation
8a - 4 = -10a + 50	Distributive Property
8a - 4 + 10a = -10a + 50 + 10a	Add 10a to each side.
18a-4=50	Simplify.
18a - 4 + 4 = 50 + 4	Add 4 to each side.
18a = 54	Simplify.
$\frac{18a}{18} = \frac{54}{18}$	Divide each side by 18
© ≡ 33	Simplify

Exercises

The solution is 3.

Solve each equation. Then check your solution.

2. $2(7+3t)=-t$	-2	5. $5(f+2) = 2(3-f)$	8. $3(d-8)=3d$
13(x+5) = 3(x-1)	-2	1. $75 - 9g = 5(-4 + 2g)$	7.18 = 3(2c + 2)

	(q)
	- 1
	2(5
	II
	\overline{S}
	- 1
N	4(b)

10.
$$4(b-2) = 2(5-b)$$

11. 1.2(x-2)=2

N

no solution

12. $\frac{3+y}{x}$

$$4(b-2) = 2(5-b)$$

9. 5(p+3)+9=3(p-2)+6

9

$$4(b-2)=2(a$$



15. 2(w-1)+4=4(w+1)

14. 2(4 + 2k) + 10 = k

T

-4r

18. -4(r+2) = 4(2)

= 22

17. 2[2 + 3(y - 1)]



16.
$$6(n-1) = 2(2n+4)$$

19.
$$-3(x-8) = 24$$

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21. 6(2-2y)=5(2y-

20. 4(4-4k) = -10-16k

no solution

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Skills Practice

Solving Equations with the Variable on Each Side

Justify each step.

$$4k - 3 = 2k + 5$$
$$4k - 3 - 2k = 2k + 5 - 2k$$

$$2k - 3 = 5$$
 $2k - 3 = 5$

2k = 8 $\frac{2k}{2} = \frac{8}{2}$ k = 4

2(8u + 2) = 3(2u - 7)

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16u + 4 = 6u - 21

$$16u + 4 - 6u = 6u - 21 - 6u$$
 b. Subtract 6u from each side.

10u + 4 - 4 = -21 - 4

10u + 4 = -21

Solve each equation. Then check your solution.

$$3. 2m + 12 = 3m - 31$$

5. 7a - 3 = 3 - 2a

4.
$$2h - 8 = h + 17$$
 25

8.
$$-6y - 3 = 3 - 6y$$
 no solution

7. 4x - 9 = 7x + 12 - 7**9.** 5 + 3r = 5r - 19 **12**

6. 4n - 12 = 12 - 4n **3**

10.
$$-9 + 8k = 7 + 4k$$
 4
12. $3(5j + 2) = 2(3j - 6)$ -2

11.
$$8q + 12 = 4(3 + 2q)$$
 all numbers 12. $3(5j + 2) = 2(3j - 6)$ -2
13. $6(-3v + 1) = 5(-2v - 2)$ 14. $-7(2b - 4) = 5(-2b + 6)$ -0.5 or

13.
$$6(-3v + 1) = 5(-2v - 2)$$
 2

13.
$$6(-3v + 1) = 5(-2v - 2)$$

15. $3(8 - 3t) = 5(2 + t)$ **1**

19.
$$6(w-1) = 3(3w+5)$$

17. 8(2f-2) = 7(3f+2) **-6**

21.
$$\frac{2}{3}v - 6 = 6 - \frac{2}{3}v$$
 9

22.
$$\frac{1}{2} - \frac{5}{8}x = \frac{7}{8}x + \frac{7}{2}$$
 -2

resson 3-5

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20. 7(-3y + 2) = 8(3y - 2)

-1₂

18. 5(-6-3d)=3(8+7d) **-1.5** or

16. 2(3u + 7) = -4(3 - 2u) **13**

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3-5

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Practice (Average)

Solving Equations with the Variable on Each Side

Solve each equation. Then check your solution.

1.
$$5x - 3 = 13 - 3x$$
 2

2.
$$-4c - 11 = 4c + 21$$
 4. $14 + 5n = -4n + 17$

3.
$$1 - s = 6 - 6s$$
 1
5. $\frac{1}{2}k - 3 = 2 - \frac{3}{4}k$ 4

8.
$$4(4-w) = 3(2w+2)$$
 1

7.
$$3(-2-3x) = -9x - 4$$
 no solution

10.
$$3(6+5y) = 2(-5+4y)$$
 -4

9.
$$9(4b-1) = 2(9b+3)$$
 $\frac{5}{6}$
11. $-5x - 10 = 2 - (x+4)$ -2

9. 9(4b-1)=2(9b+3)

12.
$$6 + 2(3j - 2) = 4(1 + j)$$
 1

14. 1.4f + 1.1 = 8.3 - f **3**

13.
$$\frac{5}{2}t - t = 3 + \frac{3}{2}t$$
 no solution

$$\frac{2}{2}t$$
 110 solution

16.
$$2 - \frac{3}{4}z = \frac{1}{8}z + 9$$
 -8

15.
$$\frac{2}{3}x - \frac{1}{6} = \frac{1}{2}x + \frac{5}{6}$$
 6

18.
$$\frac{1}{3}(c+1) = \frac{1}{6}(3c-5)$$
 7

20.
$$\frac{1}{9}(2m-16) = \frac{1}{3}(2m+4)$$
 -7

19. $\frac{1}{4}(5-2h) = \frac{h}{2} \cdot 1\frac{1}{4}$

17. $\frac{1}{2}(3g-2) = \frac{g}{6}$

22. 2(a-8) + 7 = 5(a+2) - 3a - 19**21.** 3(d-8)-5=9(d+2)+1 -8

23. Two thirds of a number reduced by 11 is equal to 4 more than the number. Find the number. -45

24. Five times the sum of a number and 3 is the same as 3 multiplied by 1 less than twice the number. What is the number? 18

25. NUMBER THEORY Tripling the greater of two consecutive even integers gives the same result as subtracting 10 from the lesser even integer. What are the integers? -8, -6

GEOMETRY The formula for the perimeter of a rectangle is $P=2\ell+2w$, where ℓ is the length and w is the width. A rectangle has a perimeter of 24 inches. Find its dimensions if its length is 3 inches greater than its width. **4.5 in. by 7.5 in.**

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 $\frac{10u = -25}{10} = \frac{-25}{10}$ u = -2.5

3-5

PERIOD

Reading to Learn Mathematics

Solving Equations with the Variable on Each Side

Pre-Activity How can an equation be used to determine when two populations

Read the introduction to Lesson 3-5 at the top of page 149 in your textbook 7.6x represents the increase (in millions) in the number of male Internet users, and 8x represents the increase (in millions) in the number of female Internet users. In the equation 12 + 7.6x = 6 + 8x, what do 7.6x and 8x represent?

Reading the Lesson

1. Suppose you want to help a friend solve 6k + 7 = 3k - 8. What would you advise her to do first? Why?

Subtract 3k from each side; after she does that and simplifies, all of the variables will be on the left side **2.** When solving 2(3x-4)=3(x+5), why is it helpful first to use the Distributive Property to remove the grouping symbols?

Once you have removed the grouping symbols, you can tell what you need to add or subtract to each side to get all of the variables on one side.

On a quix, Jason solved three equations. His teacher said all the work was correct, but she asked him to write short sentences to tell what the solutions were. In what follows, you see the *last* equation in his work for each equation. Write sentences to describe the

a. x = -4 The solution is -4.

- **b.** 6m = 6m All numbers are solutions.
- c. 12 = 37 There are no solutions.
- 4. In Question 3, one of the equations Jason solved was an identity. Which equation was it? Explain how you know.

The one for which the last step was 6m = 6m; the expressions on the left and right sides are the same.

Helping You Remember

words, the expressions on the left and right sides always have the same value. Look up the word *identity* in the dictionary. Write all the definitions that are similar to the mathematical definition. See students' work. 5. An equation with variables is an identity when the equation is always true. In other

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Identities

An equation that is true for every value of the variable is called an **identity**. When you try to solve an identity, you end up with a statement that is always true. Here is an example.

Solve 8 - (5 - 6x) = 3(1 + 2x). Example

$$8 - (5 - 6x) = 3(1 + 2x)$$
$$8 - 5 - (-6x) = 3(1 + 2x)$$

$$8 - 5 + 6x = 3 + 6x$$

3 + 6x = 3 + 6x

Exercises

State whether each equation is an identity. If it is not, find its solution.

1.
$$2(2-3x) = 3(3+x) + 4$$

2.
$$5(m+1)+6=3(4+m)+(2m-1)$$
 identity

3. (5t + 9) - (3t - 13) = 2(11 + t)identity

4.
$$14 - (6 - 3c) = 4c$$
 no solution

5.
$$3y - 2(y + 19) = 9y - 3(9)$$

V = -1

6.
$$3(3h - 1) = 4(h + 3)$$

h = **3**

$$9y - 3(9 - y)$$
 6. 3(3)

7. Use the true equation 3x - 2 = 3x - 2 to create an identity of your own.

Sample answer: 6x - 4 = 2(3x - 2)

8. Use the false equation 1 = 2 to create an equation with no solution.

Sample answer: 2x + 1 = 2x + 2

9. Create an equation whose solution is x = 3.

Sample answer: 3x + 2(x + 1) = 20

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 $\frac{0.5}{x}$ 10

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3. $\frac{0.1}{2}$

2 3

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Study Guide and Intervention Ratios and Proportions

Ratios and Proportions A ratio is a comparison of two numbers by division. The ratio An equation stating that two ratios are equal is called a **proportion**. To determine whether two ratios form a proportion, express both ratios in simplest form or check cross products. of x to y can be expressed as x to y, x;y or $\frac{x}{x}$. Ratios are usually expressed in simplest form.

$=\frac{2}{3}$ when expressed in The ratios $\frac{24}{36}$ and $\frac{12}{18}$ form ratios $\frac{24}{36}$ and $\frac{12}{18}$ form a when expressed in Determin because they are equal wh Example 1 \parallel 24 36 11 18

ne whether the	Example 2	Use cros
a proportion.	determine whether $\frac{10}{18}$	ther $\frac{10}{18}$
	proportion.	10
n simplest form.	$\frac{10}{18} \stackrel{?}{=} \frac{25}{45}$	Write the p
n simplest form.	$10(45) \stackrel{?}{=} 18(25)$	Cross proc
n a proportion	450 = 450	Simplify.
hen expressed in	The cross products are eq	ets are equ
•	Since the ratios are equal,	are equal,
	proportion	

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Solve Proportions If a proportion involves a variable, you can use cross products to solve

PERIOD

(continued)

Study Guide and Intervention

3-6

Ratios and Proportions

called means. In a proportion, the product of the extremes is equal to the product of the means.

Means-Extremes Property of Proportions $\left| \text{ For any numbers } a,b,c, \text{ and }d, \text{ if } \frac{a}{b} = \frac{c}{d}, \text{ then } ad = bc.$

the proportion. In the proportion $\frac{x}{5} = \frac{10}{13}$, x and 13 are called **extremes** and 5 and 10 are

Use cross products to	ermine whether $\frac{10}{18}$ and $\frac{25}{45}$ form a portion.	$\frac{2}{4} \frac{25}{45}$ Write the proportion.	$ 45) \stackrel{?}{=} 18(25)$ Cross products	50 = 450 Simplify.	cross products are equal, so $\frac{10}{18} = \frac{25}{45}$.	ce the ratios are equal, they form a
	ermin portic	$\frac{10}{18} \stackrel{?}{=} \frac{25}{45}$	45) ≟ 1	60 = 4	cross	ce the

Solve $\frac{x}{5} = \frac{10}{13}$.	Original proportion	Cross products	Simplify.	Divide each side by 13.	Simplify.
Ехатріе	$\frac{x}{5} = \frac{10}{13}$	13(x) = 5(10)	13x = 50	$\frac{13x}{13} = \frac{50}{13}$	$x = 3\frac{11}{13}$

The solution is $3\frac{11}{13}$.

Solve each proportion.

1.
$$\frac{-3}{x} = \frac{2}{8} - 12$$

$$\frac{x+1}{4} = \frac{3}{4}$$
 2

$$7. \frac{9}{y+1} = \frac{18}{54} 26$$

12

 $\frac{p}{24}$

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6

-10

3 | 3

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 $q \mid 3$

3 + 3

12.

no solution

 $s \mid 5$

1.5

3

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 $\frac{x}{21}$

72

$$\frac{9}{y+1} = \frac{18}{54} 26$$

 $\frac{14}{21}$, $\frac{20}{30}$

 $\frac{9}{12}$

œ

 $\frac{15}{20}$

7. $\frac{0.1}{2}$, $\frac{5}{100}$

yes

6. $\frac{4}{9}$, $\frac{12}{27}$ **yes**

ö

10.
$$\frac{4}{b-2} = \frac{4}{12}$$
 14

14.
$$\frac{12}{k} = \frac{24}{k}$$
 no solution

89

3 3

13. $\frac{a-8}{12}$ =

9

6 17

ı

 $\frac{2+w}{6}$

15.

15. 100:75, 44:33

14. 18 to 24, 50 to 75

13. 5:5, 30:20

2

2

yes

 $\frac{72}{64}$, $\frac{9}{8}$

12

11.5 to 9, 25 to 45

10. 2:3, 20:30

yes

yes

 $\frac{0.45}{0.9}$

18

 $\frac{0.1}{0.2}$,

17. $\frac{1.5}{2}$, $\frac{6}{8}$ yes

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Answers

Exercises

Use cross products to determine whether each pair of ratios forms a proportion.

10

1. $\frac{1}{2}$, $\frac{16}{32}$

π |∞ **5**

25 49

10 20,

 $\frac{1}{20}$

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g-g uossəŋ Use cross products to determine whether each pair of ratios forms a proportion. Write yes or no.

1.
$$\frac{4}{5}$$
, $\frac{20}{25}$ yes
3. $\frac{6}{7}$, $\frac{24}{28}$ yes

4.
$$\frac{8}{9}$$
, $\frac{72}{81}$ yes

2

7 1

9 5

$$\frac{9}{9}, \frac{13}{81}$$
 yes

$$\frac{8}{9}, \frac{72}{81}$$
 yes

6.
$$\frac{13}{19}$$
, $\frac{26}{38}$ yes

2

 $\frac{7}{16}, \frac{42}{90}$

2

50

 $\frac{12}{17}$,

 $\frac{21}{98}$

 $7.\frac{3}{14}$

$$\frac{1}{x} = \frac{2}{14}$$
 7

10.
$$\frac{5}{b} = \frac{3}{9}$$
 15

12.
$$\frac{3}{a} = \frac{1}{6}$$
 18

14.
$$\frac{5}{e} = \frac{35}{21}$$
 3
16. $\frac{6}{23} = \frac{y}{69}$ 18

7

36

7

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14.

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9 | 2

13.

18.
$$\frac{7}{b} = \frac{1}{9}$$
 63

$$18. rac{7}{b} = rac{1}{9} \; 63$$

20.
$$\frac{11}{15} = \frac{n}{60}$$
 44

42

30

 $\frac{10}{14}$

19.

 ∞

9

 \parallel

 $\frac{42}{56}$

17.

22.
$$\frac{5}{12}$$
 =

5

 $\frac{27}{39}$

6 | 0

48

20 8

24.
$$\frac{22}{x} = \frac{11}{30}$$
 60

16

 $\frac{4}{21}$

69

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Use cross products to determine whether each pair of ratios forms a proportion. Write yes or no.

2.
$$\frac{3}{11}$$
,

2

1. $\frac{7}{6}$, $\frac{52}{48}$

2

 $\frac{15}{66}$

$$\mathbf{5.} \frac{8}{9}, \frac{72}{81} \text{ yes}$$

 $\frac{108}{99}$ yes

4. $\frac{12}{11}$,

6. $\frac{1.5}{9}$, $\frac{1}{6}$ yes

 $\frac{18}{24}$, $\frac{36}{48}$

9. $\frac{7.6}{1.8}$, $\frac{3.9}{0.9}$

2

 $\frac{1.7}{1.2}$, $\frac{2.9}{2.4}$

7. $\frac{3.4}{5.2}$, $\frac{7.14}{10.92}$ yes

Solve each proportion. If necessary, round to the nearest hundredth. 10.
$$\frac{5}{a} = \frac{30}{54}$$
 9 11. $\frac{v}{46} = \frac{34}{23}$ 68 12. $\frac{40}{56} = \frac{k}{7}$ 5

12.
$$\frac{40}{56} = \frac{k}{7}$$
 5

34

11. $\frac{v}{46}$

30

| a | 57

15.
$$\frac{y}{3} = \frac{48}{9}$$
 16. 18. $\frac{3}{51} = \frac{z}{17}$ 1

8

 $\frac{27}{162}$

14.

4 | 3

13. $\frac{28}{49}$

1

35

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 $\frac{5}{11}$

17.

12

10

 $16. \frac{2}{y} = \dot{\hat{z}}$

18.
$$\frac{3}{51} = \frac{2}{17}$$
 121. $\frac{14}{49} = \frac{2}{a}$ 7

24

9 | 4

 $\frac{8}{16}$

20.

 $\frac{12}{h}$ 122

19. $\frac{6}{61}$

24.
$$\frac{m}{6} = \frac{5}{8} \frac{3\frac{3}{4}}{4}$$

3 = 7

33

 $\frac{8}{c}$ 10 $\frac{2}{7}$

= 6

27.
$$\frac{6}{n} = \frac{3}{0.51}$$
 1.02

 $a = \frac{12}{b}$ 2.88

26. $\frac{3}{0.72}$

7

25. $\frac{v}{0.23}$

29. $\frac{3}{12}$

 $=\frac{14}{6}$

30.
$$\frac{m-1}{8} = \frac{2}{4}$$
 5

33.
$$\frac{3}{7} = \frac{x-2}{6}$$

32. $\frac{r+2}{7} = \frac{5}{7}$

- 34. PAINTING Ysidra paints a room that has 400 square feet of wall space in $2\frac{1}{2}$ hours. At this rate, how long will it take her to paint a room that has 720 square feet of wall
- 35. VACATION PLANS Walker is planning a summer vacation. He wants to visit Petrified National Forest and Meteor Crater, Arizona, the 50,000-year-old impact site of a large meteor. On a map with a scale where 2 inches equals 75 miles, the two areas are about $1\frac{1}{2}$ inches apart. What is the distance between Petrified National Forest and Meteor

Crater? about 56.25 mi

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15

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11.

Answers

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Pre-Activity How are ratios used in recipes? Ratios and Proportions

Reading to Learn Mathematics

Read the introduction to Lesson 3-6 at the top of page 155 in your textbook.

- How many servings of honey frozen yogurt are made by this recipe?
- How many recipes would be needed to make enough honey frozen yogurt for all the students in your class? See students' work.

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Angles of a Triangle

Enrichment

3-6

NAME

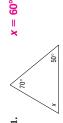
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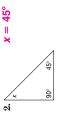
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In geometry, many statements about physical space are proven to be true. Such statements are called theorems. Here are two examples of geometric theorems.

- a. The sum of the measures of the angles of a triangle is 180°.
- b. If two sides of a triangle have equal measure, then the two angles opposite those sides also have equal measure.

For each of the triangles, write an equation and then solve for κ . (A tick mark on two or more sides of a triangle indicates that the sides have equal measure.)







Express the ratios in simplest form to see if they are equal. Check to see whether the cross products are equal.

 $=\frac{8}{20}$ is a proportion.

2. Describe two ways to decide whether the sentence $\frac{2}{5}$

A ratio is a comparison of two numbers by

1. Complete the following sentence.

Reading the Lesson

division



 $x = 10^{\circ}$

6.

 $x = 22.5^{\circ}$

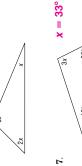
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3. For each proportion, tell what the extremes are and what the means are.

Extremes: Extremes:

15 12

14 9 | 8



4. A jet flying at a steady speed traveled 825 miles in 2 hours. If you solved the proportion

 $=\frac{x}{1.5}$, what would the answer tell you about the jet?

825

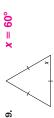
how far the jet traveled in 1.5 h

Helping You Remember

Means: Means:



 $x = 100^{\circ}$



Use cross products. Write an equation with the product of the extremes on the left side and the product of the means on the right side. Then 5. Write how you would explain solving a proportion to a friend who missed Lesson 3-6.

solve this second equation.



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11. Two angles of a triangle have the same these angles is one-half the measure of measure. The sum of the measures of the third angle. Find the measures of the angles of the triangle. 30°, 30°, 120°

twice the measure of a second angle. The measure of the third angle is 12 less than 12. The measure of one angle of a triangle is measures of the angles of the triangle. the sum of the other two. Find the

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Study Guide and Intervention

PERIOD

Percent of Change

Percent of Change When an increase or decrease in an amount is expressed as a percent, the percent is called the **percent of change**. If the new number is greater than the original number, the percent of change is a **percent of increase**. If the new number is less than the original number, the percent of change is the **percent of decrease**.

Solve Problems Discounted prices and prices including tax are applications of percent of change. Discount is the amount by which the regular price of an item is reduced. Thus, the discounted price is an example of percent of decrease. Sales tax is amount that is added to the cost of an item, so the price including tax is an example of percent of increase.

(continued)

Study Guide and Intervention

Percent of Change

A coat is on sale for 25% off the original price. If the original price

of the coat is \$75, what is the discounted price?

The discount is 25% of the original price.

25% of $$75 = 0.25 \times 75$

= 18.75

Example 1

Find the percent of increase original: 48 new: 60

original: 30 new: 22

> First, subtract to find the amount of increase. The amount of increase is 60 - 48 = 12.

Then find the percent of increase by using the original number, 48, as the base.

$$\frac{12}{48} = \frac{r}{100}$$
 Percent proportion $\frac{12}{2(100)} = 48(r)$ Cross products $\frac{1200 = 48r}{48}$ Simplify, $\frac{1200}{48} = \frac{48r}{48}$ Divide each side by 48.

The percent of increase is 25%.

Find the percent of decrease.

First, subtract to find the amount of decrease. The amount of decrease is 30-22=8.

Then find the percent of decrease by using the original number, 30, as the base.

Percent proportion	Cross products	Simplify.	Divide each side by 30.	Simplify.
$\frac{8}{30} = \frac{r}{100}$	8(100) = 30(r)	Ш	$\frac{800}{30} = \frac{30r}{30}$	$26\frac{2}{3} = r$

The percent of decrease is $26\frac{2}{3}\%$, or about 27%.

State whether each percent of change is a percent of increase or a percent of decrease. Then find each percent of change. Round to the nearest whole percent.

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The discounted price of the coat is \$56.25

Subtract \$18.75 from the original price.

\$75 - \$18.75 = \$56.25

Find the final price of each item. When a discount and a sales tax are listed, compute the discount price before computing the tax.

3. Airline ticket: \$248.00 Superair discount: 33% \$166.16	6. Celebrity calendar: \$10.95 Sales tax: 7.5% \$11.77	9. Video recorder: \$110.95 Discount: 20% Sales tax: 5% \$93.20
2. Two concert tickets: \$28 Student discount: 28% \$20.16	5. CD player: \$142.00 Sales tax: 5.5% \$149.81	8. Software: \$44.00 Discount: 21% Sales tax: 6% \$36.85
1. Compact disc: \$16 Discount: 15% \$13.60	4. Shirt: \$24.00 Sales tax: 4% \$24.96	7. Class ring: \$89.00 Group discount: 17% Sales tax: 5% \$77.56

10. VIDEOS The original selling price of a new sports video was \$65.00. Due to the demand the price was increased to \$87.75. What was the percent of increase over the original

decrease; 33%

increase: 7%

decrease; 20%

4. original: 77.5

new: 62

5. original: 140

new: 150

6. original: 135

new: 90

decrease; 9%

increase: 200%

increase; 50%

7. original: 120

8. original: 90

9. original: 27.5

decrease; 56%

increase: 11%

increase; 60%

1. original: 50

Exercises

2. original: 90

3. original: 45

11. SCHOOL A high school paper increased its sales by 75% when it ran an issue featuring a contest to win a class party. Before the contest issue, 10% of the school's 800 students bought the paper. How many students bought the contest issue? 140 students 12. BASEBALL Baseball tickets cost \$15 for general admission or \$20 for box seats. The sales tax on each ticket is 8%, and the municipal tax on each ticket is an additional 10% of the base price. What is the final cost of each type of ticket? \$17.70; \$23.60

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increase; 100%

decrease: 20%

increase; 17%

10. original: 84

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12. original: 250

11. original: 12.5

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26. HEATING COSTS Customers of a utility company received notices in their monthly bills that heating costs for the average customer had increased 125% over last year because of an unusually severe winter. In January of last year, the Garcia's paid \$120 for heating. What should they expect to pay this January if their bill increased by 125%? \$270 Glencoe Algebra 1 25. INVESTMENTS The price per share of an internet-related stock decreased from \$90 per decrease. Then find each percent of change. Round to the nearest whole percent. **21.** pair of shorts: \$24.99 State whether each percent of change is a percent of increase or a percent of PERIOD 18. luggage: \$185.00 increase; 12% increase; 60% share to \$36 per share early in 2001. By what percent did the price of the stock decrease? 60% decrease; 6% 24. printer: \$255.00 12. jacket: \$125.00 9. original: 58.8 discount: 45% discount: 30% 3. original: 200 6. original: 128 15. kite: \$18.90 \$131.88 tax: 5.5% tax: 5.5% \$188.32 \$19.85 \$13.74 tax: 5% DATE 20. prescription glasses: \$149 17. computer game: \$49.99 discount: 25% 23. DVD player: \$269.00 decrease; 21% decrease; 35% increase; 14% 14. blanket: \$24.99 8. original: 98.6 new: 64 discount: 20% discount: 20% 176 2. original: 140 11. crib: \$240.00 5. original: 76 new: 160 tax: 6.5% \$255.60 \$119.20 \$230.26 Find the discounted price of each item. new: 60 \$26.74 tax: 7% tax: 7% Practice (Average) Percent of Change Find the total price of each item. Find the final price of each item. 10. concrete blocks: \$95.00 **16.** dry cleaning: \$25.00 discount: 15% 13. class ring: \$325.00 22. television: \$375.00 increase; 150% increase; 137% 19. stationery: \$12.95 decrease; 44% Glencoe/McGraw-Hill discount: 10% discount: 25% 4. original: 10 7. original: 15 1. original: 18 NAME \$100.70 \$298.13 \$344.50 new: 25 tax: 6% \$11.66 tax: 6% ر-و uossə٦ Glencoe Algebra 1 decrease. Then find each percent of change. Round to the nearest whole percent. State whether each percent of change is a percent of increase or a percent of **16.** concert tickets: \$48.00 tax: 7.5% 22. coffee maker: \$102.00 decrease; 25% DATE 18. monitor: \$150.00 increase; 12% 12. groceries: \$47.52 increase; 50% increase; 6% 10. binder: \$14.50 discount: 50% discount: 40% discount: 45% 14. shoes: \$65.00 20. shirt: \$25.50 **6.** original: 90 2. original: 50 4. original: 25 8. original: 60 \$75.00 new: 28 tax: 7% \$15.52 \$48.95 \$67.60 \$51.60 \$15.30 \$56.10 tax: 4% 175 Find the discounted price of each item. **Skills Practice** Percent of Change Find the total price of each item. 11. hardcover book: \$28.95 **21.** sleeping bag: \$125 13. filler paper: \$6.00 basketball: \$17.00 decrease; 60% decrease; 40% 17. backpack: \$56.25 increase; 25% decrease; 9% Glencoe/McGraw-Hill discount: 20% discount: 20% 9. dress: \$69.00 discount: 25% **5.** original: 50 3. original: 55 7. original: 48 1. original: 25 19. CD: \$15.99 new: 30 tax: 6.5% new: 50 \$45.00 \$93.75 \$72.45 \$30.69 \$12.79 tax: 5% tax: 6% \$18.02

3-7

Reading to Learn Mathematics

Percent of Change

Pre-Activity How can percents describe growth over time?

Read the introduction to Lesson 3-7 at the top of page 160 in your textbook.

- How many area codes were in use in 1947? 84 area codes
- How many more area codes were in use in 1999? 201 area codes

Reading the Lesson

- 1. If you use (original amount) (new amount) to find the change for a percent of change problem, then the problem involves a percent of (increase/decrease).
- 2. If you use (new amount) (original amount) to find the change for a percent of change problem, then the problem involves a percent of (increase/decrease).

Complete the chart.

	Original Amount	New Amount	Percent Proportion	Percent Increase or Percent Decrease?
ကံ	10	13	$\frac{\text{change}}{\rightarrow} \frac{3}{\rightarrow} \frac{r}{-r}$	increase
4	10	7	$\frac{change}{\longrightarrow} \to \frac{3}{\longrightarrow} = \frac{r}{\longrightarrow}$	decrease
10	50	42	$\frac{change}{\longrightarrow} \to \frac{8}{\longrightarrow} = \frac{r}{\longrightarrow}$	decrease
6.	50	58	$\frac{change}{\longrightarrow} \to \frac{8}{\longrightarrow} = \frac{r}{-r}$	increase

7. When you find a discount price, do you add to or subtract from the original price?

Helping You Remember

8. If you remember only two things about the ratio used for finding percent of change, what should they be? Subtract the prices, then divide by the original number.

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Enrichment

Using Percent

Use what you have learned about percent to solve each problem.

- A TV movie had a "rating" of 15 and a 25 "share." The rating is the percentage of the nation's total TV households that were tuned in to this show. The share is the percentage of homes with TVs turned on that were tuned to the movie. How many TV households had their TVs turned off at this time?
 - To find out, let T =the number of TV households
- and x = the number of TV households with the TV off. Then T x = the number of TV households with the TV on.
- Since 0.15T and 0.25(T-x) both represent the number of households tuned to the movie,
 - $\begin{array}{l} 0.15T = 0.25(T-x) \\ 0.15T = 0.25T 0.25x. \\ 0.25x = 0.10T \end{array}$

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- $\frac{1}{0.25} = 0.40T$ 0.10T| x Solve for x.
- Forty percent of the TV households had their TVs off when the movie was aired

Answer each question.

During that same week, a sports broadcast had a rating of 22.1 and a 43 share. Show that the percent of TV households with their TVs off was about 48.6%.

0.221T = 0.43T - 0.43x

- 2. Find the percent of TV households with their TVs turned off during a show with a rating of 18.9 and a 29 share. **34.8**%
- 3. Show that if T is the number of TV households, r is the rating, and s is the share, then the number of TV households with the TV off is
- **L** If the fraction of TV households with no TV on is $\frac{s-r}{r}$ then show that the fraction of TV households with TVs on is $\frac{r}{s}$. $1 - \frac{s-r}{s} =$
- 5. Find the percent of TV households with TVs on during the most watched serial program in history: the last episode of $M^*A^*S^*H$, which had a 60.3 rating and a 77 share.
- revenue per month. The station is thinking of going commercial free for the three months of summer to gain more listeners. What would its new share have to be for the last 4 months of the year to make more money for the year than it would have made had it not gone commercial free? greater than 3.5 5. A local station now has a 2 share. Each share is worth \$50,000 in advertising

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Study Guide and Intervention

Solving Equations and Formulas

Solve for Variables Sometimes you may want to solve an equation such as $V = \ell w h$ for one of its variables. For example, if you know the values of V, w, and h, then the equation $\ell = \frac{V}{wh}$ is more useful for finding the value of ℓ . If an equation that contains more than one variable is to be solved for a specific variable, use the properties of equality to isolate the specified variable on one side of the equation.

Example 1 Solve 2x - 4y = 8 for y. 2x - 4y = 8

$$2x - 4y - 2x = 8 - 2x$$

$$-4y = 8 - 2x$$

3m

 $y = \frac{8 - 2x}{-4}$ or $\frac{2x - 8}{4}$ The value of y is $\frac{2x-8}{4}$.

Example 2 Solve 3m - n = km - 8 for m.

$$3m - n = km - 8$$

 $3m - n - km = km - 8 - km$
 $3m - n - km = - 8$
 $n - n - km + n = - 8 + n$
 $3m - km + n = - 8 + n$
 $m(3 - k) = - 8 + n$

$$m(3-k) = -8 + n$$

$$m(3-k) = -8 + n$$

$$3 - k = -8 + n$$

$$m = -8 + n$$

$$m = -8 + n$$

$$m = -8 + n$$

The value of m is $\frac{n-8}{3-k}$. Since division by 0 is undefined, $3 - k \neq 0$, or $k \neq 3$.

8-£ uossə7

Solve each equation or formula for the variable specified.

2. 15x + 1 = y for x

1.
$$ax - b = c \text{ for } x$$

$$x = \frac{c+b}{a}, a \neq 0$$
4. $xy + z = 9 \text{ for } y$

3.
$$(x + f) + 2 = j \text{ for } x$$

 $x = j - 2 - f$

5.
$$x(4-k) = p$$
 for k
 $k = 4 - \frac{p}{x}, x \neq k$

 $y = \frac{9-z}{\sqrt{}}, x \neq$

0

8. 2x + b = c for x

7. 4(c + 3) = t for c

 $c=\frac{t}{4}-3$

 $\chi = \frac{c-b}{c-b}$

6.
$$7x + 3y = m \text{ for } y$$

$$\mathbf{y} = \frac{m - 7x}{3}$$

$$9.x(1+y) = z \text{ for } x$$

$$x = \frac{z}{1+y}, y \neq -1$$

12.
$$A = \frac{h(a+b)}{2}$$
 for h
 $h = \frac{2A}{a+b}, a \neq -b$

$$h = \frac{2A}{a+b}, \epsilon$$

 $r=\frac{d}{t},\,t\neq0$

11. d = rt for r

10. 16z + 4x = y for x

 $\chi = \frac{y - 16z}{x}$

14.
$$P = 2\ell + 2w$$
 for w

$$W = \frac{P - 2\ell}{2}$$

13. $C = \frac{5}{9}(F - 32)$ for F

 $F = \frac{9}{5}C + 32$

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15.
$$A = \ell w \text{ for } \ell$$

$$\ell = \frac{A}{w}, w \neq 0$$

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3-8

Study Guide and Intervention

Solving Equations and Formulas

(continued)

Use Formulas Many real-world problems require the use of formulas. Sometimes solving a formula for a specified variable will help solve the problem.

(Example) The formula $C = \pi d$ represents the circumference of a circle, or the distance around the circle, where d is the diameter. If an airplane could fly around Earth at the equator without stopping, it would have traveled about 24,900 miles. Find the diameter of Earth.

$$C=\pi d$$
 Given formula $d=\frac{C}{\pi}$ Solve for d $d=\frac{24,900}{0.14}$ Use $\pi=3.14$.

The diameter of Earth is about 7930 miles.

 $d \approx 7930$

- **GEOMETRY** The volume of a cylinder V is given by the formula $V = \pi r^2 h$, where r is the radius and h is the height
- **a.** Solve the formula for h. $h = \frac{V}{\pi r^2}$
- **b.** Find the height of a cylinder with volume 2500π feet and radius 10 feet. 25 ft
- **2. WATER PRESSURE** The water pressure on a submerged object is given by P=64d, where P is the pressure in pounds per square foot, and d is the depth of the object in feet.
 - **a.** Solve the formula for d. $d = \frac{P}{64}$
- b. Find the depth of a submerged object if the pressure is 672 pounds per square foot.
- **3. GRAPHS** The equation of a line containing the points (a,0) and (0,b) is given by the formula $\frac{x}{a} + \frac{y}{b} = 1$.
 - **a.** Solve the equation for y. $y = b\left(1 \frac{x}{a}\right)$
- **b.** Suppose the line contains the points (4, 0), and (0, -2). If x = 3, find y.
- **4. GEOMETRY** The surface area of a rectangular solid is given by the formula $S=2\ell w+2\ell h+2wh$, where $\ell=\mathrm{length}, w=\mathrm{width},$ and $h=\mathrm{height}.$
- **a.** Solve the formula for h. $h = \frac{S 2\ell w}{2\ell + 2w}$
- b. The surface area of a rectangular solid with length 6 centimeters and width 3 centimeters is 72 square centimeters. Find the height. 2 cm

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Solving Equations and Formulas **Skills Practice**

DATE

Solve each equation or formula for the variable specified.

1.
$$7t = x$$
, for $t = \frac{x}{7}$

2.
$$e = wp$$
, for $p = \frac{e}{w}$

1.
$$7t = x$$
, for $t = \frac{x}{7}$
3. $q - r = r$, for $r = \frac{q}{2}$

$$m - n = m, \text{ for } m = \frac{n}{3}$$

5. ab + 3c = 2d, for $b = \frac{2d - 3c}{2d - 3c}$

7. $\frac{2}{3}m + a = a + c$, for $m = \frac{3}{2}c$

3. mx + 4y = 3c, for $x = \frac{3c - 4y}{2c - 4y}$

1. d = rt, for $r = \frac{d}{t}$

4.
$$4m - n = m$$
, for m

3.
$$q - r = r$$
, for $r = \frac{q}{2}$ 4. $4m - n$
5. $7a - b = 15a$, for $a = -\frac{b}{2}$ 6. $-5c + d$

6.
$$-5c + d = 2c$$
, for c $\mathbf{c} = \frac{d}{7}$
8. $m + 3n = 1$, for $n = \frac{1 - m}{3}$

7. x - 2y = 1, for $y y = \frac{x - 1}{2}$

9. 7f + g = 5, for $f = \frac{5 - g}{7}$

$$=\frac{1-m}{3}$$

4.
$$9s - 5g = -4u$$
, for $s = \frac{-4u + 5g}{9}$
6. $2p = kx - q$, for $x = \frac{2p + q}{k}$
8. $\frac{2}{5}h + g = d$, for $h = \frac{5}{2}(d - g)$
10. $\frac{3}{4}a - q = k$, for $a = \frac{4}{3}(k + q)$
12. $\frac{3b - 4}{2} = c$, for $b = \frac{2c + 4}{3}$

2. 6w - y = 2z, for w = -1

Solve each equation or formula for the variable specified.

Solving Equations and Formulas

Practice (Average)

8-6

DATE

9.
$$\frac{2}{3}y + v = s$$
, for y $y = \frac{3}{2}(s - v)$ 10. $\frac{3}{4}a - v$
11. $\frac{rx + 9}{5} = h$, for $x = \frac{5h - 9}{r}$ 12. $\frac{3b - 4}{2}$
13. $2w - y = 7w - 2$, for $w = \frac{2 - y}{5}$ 14. $3k + y$

14.
$$3\ell + y = 5 + 5\ell$$
, for $\ell = \frac{y - 5}{2}$

Write an equation and solve for the variable specified.

15. Three times a number s plus 4 times a number y is 1 more than 6 times the number s.

3s + 4y = 6s + 1; $s = \frac{4y - 1}{2}$

16. Five times a number k minus 9 is two thirds of a number j. Solve for j.

 $5k - 9 = \frac{2}{3}j; j = \frac{3}{2}(5k - 9)$

The formula for Ohm's Law is E=IR, where E represents voltage measured in volts, I represents current measured in amperes, and R represents resistance measured in ohms. ELECTRICITY For Exercises 17 and 18, use the following information.

18. $\frac{b-4z}{7} = a$, for b **b** = 7a + 4z

17. $\frac{p+9}{5} = q$, for p = 5q - 9

16. $\frac{x-c}{2} = d$, for c = x - 2d

17. Solve the formula for $R = \vec{E}$

18. Suppose a current of 0.25 ampere flows through a resistor connected to a 12-volt battery. What is the resistance in the circuit? 48 ohms

MOTION For Exercises 19 and 20, use the following information.

20. One fourth of a number q is three more than three times a number w. Solve for q.

 $\frac{1}{4}q = 3w + 3$; q = 12w + 12

19. Five more than a number g is six less than twice a number h. Solve for g.

g + 5 = 2h - 6; g = 2h - 11

Write an equation and solve for the variable specified.

21. Eight less than a number s is three more than four times a number t. Solve for s.

s-8=4t+3; s=4t+11

In uniform circular motion, the speed v of a point on the edge of a spinning disk is $v = \frac{2\pi}{\tau}r$. where r is the radius of the disk and T is the time it takes the point to travel once around

19. Solve the formula for r. $r = \frac{Tv}{2\pi}$

20. Suppose a merry-go-round is spinning once every 3 seconds. If a point on the outside edge has a speed of 12.56 feet per second, what is the radius of the merry-go-round? (Use 3.14 for π .) **6 ft**

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2k-3g

12. bc + 3g = 2k, for c = 0

2n + y

11. rt - 2n = y, for t = t

10. ax - c = b, for $x = \frac{b + c}{c}$

R-E nossal

 $\frac{5p-6j}{8}$

14. 8c + 6j = 5p, for c = c = c

13. kn + 4f = 9v, for $n = \frac{9v - 4f}{k}$

15. $\frac{x-c}{2} = d$, for x = c + 2d

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Solving Equations and Formulas

Reading to Learn Mathematics

Pre-Activity How are equations used to design roller coasters?

Read the introduction to Lesson 3-8 at the top of page 166 in your textbook. number values do you know for these variables in this situation? The equation $g(195-h)=rac{1}{2}v^2$ contains several variables. What

32 for g and 49 for v

Reading the Lesson

1. Suppose you have an equation with several variables. You want to solve for a particular one variable? How does the solution compare with the solution for an equation with one variable. How does the procedure compare with that for solving an equation with just variable? Sample answer: The procedure is basically the same. You use properties of operations and equality to isolate the variable in which you are interested. The solution will probably contain variables instead of just a

Describe what dimensional analysis involves.

Sample answer: You use the units along with number values as you do calculations. You treat the units pretty much the same way you would variables. For example, you can divide them and use exponents with

What do you have to be careful about when you use variables in denominators of

You have to be sure that you do not use values that would make the denominator 0.

Helping You Remember

4. When you give the dimensions of a rectangle, you have to tell how many units long it is and how many units wide it is. How can this help you remember what dimensional analysis involves.

dimensional analysis, you include units for dimensions in calculations. Sample answer: Keep the words dimension and unit in mind. In

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3-8

Enrichment

PERIOD

DATE

Even though researchers have been studying the disease diabetes mellitus for hundreds of years, scientists have only recently discovered the cause of the disease and developed methods for reducing its the pioneers of this more modern research. He studied the relationship between diabetes and the pituitary gland, and in 1947 became the first. Latin American to win the Nobel Prize in Medicine and Physiology. severity. Dr. Bernardo Houssay, an Argentine physiologist, was one of Dr. Bernardo Houssay

Though there is no cure for diabetes, specific diets and exercise can help people control the disease. The American Diabetes Association (ADA) has helped establish flexible dietary guidelines for consumers to follow. These guidelines include some of the following general nutrition rules.

- Fat intake should be equal to or less than 30% of daily calories.
- Saturated fat intake should be equal to or less than 10% of daily
- Protein should be limited to 10% to 20% of daily calories. Persons showing the initial signs of diabetes-induced kidney disease should limit protein to 10% of daily calories.
 - Cholesterol intake should be 300 milligrams or less daily

Fesson 3-8

Refer to the information above for Exercises 1-4.

- 1. Robert consumed 2100 calories on Tuesday. His fat intake totaled 70 grams, and of that 70 grams, 14 were saturated
- a. What percentage of his calorie consumption was fat, and what percentage of that fat was saturated? (To find the percentage of calories from fat, multiply the number of fat grams by 9 before dividing by the number of calories.) 30%; 20
- Did Robert stay within the recommended allowance of fats? yes
- 2. Anna's cholesterol intake was 330 milligrams on Sunday. By what percentage does she need to reduce her cholesterol consumption to remain within the guidelines? 10%
- 3. What number of fat grams is 30% of 240 calories? 8
- 4. Sharon follows a diet that provides about 50 grams of protein each day. Sharon's doctor has just told her to reduce her daily protein intake by 30%. About how much protein will be in her reduced protein diet? **35 grams**

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3-9

Study Guide and Intervention

Weighted Averages

Mixture Problems

Weighted A

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Mixture Problems are problems where two or more parts are combined into a whole. They involve weighted averages. In a mixture problem, the weight is usually a price or a percent of something.

example Delectable Cookie Company sells chocolate chip cookies for \$6.95 per pound and white chocolate cookies for \$5.95 per pound. How many pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies to obtain a mixture that sells for \$6.75 per pound.

Let w = the number of pounds of chocolate chip cookies

	A contract of the second	F **** C ** C *************************	Total Duise
	Number of Pounds Price per Pound	Frice per Found	lotal Price
Chocolate Chip	W	96.9	6.95w
White Chocolate	4	26.3	4(5.95)
Mixture	W + 4	92'9	6.75(w + 4)

Equation: 6.95w + 4(5.95) = 6.75(w + 4)

Solve the equation.

$$\begin{array}{lll} 6.95w+4(5.95)=6.75(w+4) & \text{Original equation} \\ 6.95w+23.80=6.75w+27 & \text{Simplity} \\ 6.95w+23.80-6.75w=6.75w+27-6.75w & \text{subtract} 6.78w \text{ from each side,} \\ 0.2w+23.80=27-23.80 & 27-23.80 & \text{subtract} 23.80 \text{ contract} 23.80 & \text{subtract} 23.80 \text{ subtract} 23.80 & \text{subtract} 23.80 & \text{sub$$

pounds of chocolate chip cookies should be mixed with 4 pounds of white chocolate cookies.

Exercises

- 1. SOLUTIONS How many grams of sugar must be added to 60 grams of a solution that 32% sugar to obtain a solution that is 50% sugar? 21.6 g
- walnuts sell for \$1.95 per pound. How many pounds of walnuts must be added to 15 pounds of pecans to make a mixture that sells for \$1.75 per pound? 15 lb NUTS The Quik Mart has two kinds of nuts. Pecans sell for \$1.55 per pound and
- 3. INVESTMENTS Alice Gleason invested a portion of \$32,000 at 9% interest and the balance at 11% interest. How much did she invest at each rate if her total income from both investments was \$3,200. \$16,000 at 9% and \$16,000 at 11%
- **MILK** Whole milk is 4% butterfat. How much skim milk with 0% butterfat should be added to 32 ounces of whole milk to obtain a mixture that is 2.5% butterfat? 19.2 oz 4. MILK

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PERIOD

(continued) Study Guide and Intervention Weighted Averages 3-9

Uniform Motion Problems Motion problems are another application of weighted averages. **Uniform motion problems** are problems where an object moves at a certain speed, or rate. Use the formula d = rt to solve these problems, where d is the distance, r is the rate, and t is the time.

expressway for 2 hours. He then drove at a speed of 65 miles per hour on an expressway for 2 hours. He then drove for 1.5 hours at a speed of 45 miles per hour on a state highway. What was his average speed? Example

$$M=rac{65\cdot 2+45\cdot 1.5}{2+1.5}$$
 Definition of weighted average ~ 56.4

Bill drove at an average speed of about 56.4 miles per hour.

Exercises

- **I. TRAVEL** Mr. Anders and Ms. Rich each drove home from a business meeting. Mr. Anders traveled east at 100 kilometers per hour and Ms. Rich traveled west at 80 kilometers per hours. In how many hours were they 100 kilometers apart. $\frac{5}{2}$ h
- **2.** AIRPLANES An airplane flies 750 miles due west in $1\frac{1}{2}$ hours and 750 miles due south in 2 hours. What is the average speed of the airplane? about 429 mph
- later and runs 100 meters in 14 seconds. If each of them runs at a constant rate, who is 3. TRACK Sprinter A runs 100 meters in 15 seconds, while sprinter B starts 1.5 seconds further in 10 seconds after the start of the race? Explain.

6-E uossa7

Subtract 23.80 from each side.

Simplify.

 $\frac{100}{15}$ m/s. In 10 seconds, sprinter A will have run $\frac{100}{15}$ (10) = 66.7 m. Sprinter B's rate is $\frac{100}{14}$. In 10 seconds, with the delayed start, sprinter B Sprinter A; since sprinter A runs 100 m in 15 s, this sprinter runs at a has run $\frac{100}{14}$ (10 – 1.5) = 60.7 m. rate of -

- TRAINS An express train travels 90 kilometers per hour from Smallville to Megatown. A local train takes 2.5 hours longer to travel the same distance at 50 kilometers per hour. How far apart are Smallville and Megatown? 281.25 km
- **CYCLING** Two cyclists begin traveling in the same direction on the same bike path. One travels at 15 miles per hour, and the other travels at 12 miles per hour. When will the cyclists be 10 miles apart? $3\frac{1}{2}h$
- **TRAINS** Two trains leave Chicago, one traveling east at 30 miles per hour and one traveling west at 40 miles per hour. When will the trains be 210 miles apart? $\frac{3}{1}$

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Weighted Averages

Skills Practice

DATE

SEASONING For Exercises 1-4, use the following information.

A health food store sells seasoning blends in bulk. One blend contains 20% basil. Sheila wants to add pure basil to some 20% blend to make 16 ounces of her own 30% blend. Let b represent the amount of basil Sheila should add to the 20% blend.

1. Complete the table representing the problem.

	Onnces	Amount of Basil
20% Basil Blend	16 – <i>b</i>	0.20(16-b)
100% Basil	q	1.00 <i>b</i>
30% Basil Blend	16	0.30(16)

- 2. Write an equation to represent the problem. 0.20(16 b) + 1.00b = 0.30(16)
- 3. How many ounces of basil should Sheila use to make the 30% blend? 2 oz
- 4. How many ounces of the 20% blend should she use? 14 oz

HIKING For Exercises 5-7, use the following information.

At 7.00 A.M., two groups of hikers begin 21 miles apart and head toward each other. The first group, hiking at an average rate of 1.5 miles per hour, carries tents, sleeping bags, and cooking equipment. The second group, hiking at an average rate of 2 miles per hour, carries food and water. Let t represent the hiking time.

5. Copy and complete the table representing the problem.

		1	a = r
First group of hikers	1.5	t	1.5
Second group of hikers	2	t	21

- **6.** Write an equation using t that describes the distances traveled. 1.5t + 2t = 21
- 7. How long will it be until the two groups of hikers meet? 6 h

SALES For Exercises 8 and 9, use the following information.

make the mixture, he uses Virginia peanuts that cost \$3.50 per pound and Spanish peanuts Sergio sells a mixture of Virginia peanuts and Spanish peanuts for \$3.40 per pound. To hat cost \$3.00 per pound. He mixes 10 pounds at a time.

- 8. How many pounds of Virginia peanuts does Sergio use? 8 lb
- 9. How many pounds of Spanish peanuts does Sergio use? 2 lb

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NAME

PERIOD

DATE

Practice (Average)

Weighted Averages

A nursery sells Kentucky Blue Grass seed for \$5.75 per pound and Tall Fescue seed for \$4.50 per pound. The nursery sells a mixture of the two kinds of seed for \$5.25 per pound. Let k represent the amount of Kentucky Blue Grass seed the nursery uses in 5 pounds of

GRASS SEED For Exercises 1-4, use the following information.

1. Complete the table representing the problem.

	Number of Pounds	Price per Pound	Cost
Kentucky Blue Grass	K	\$5.75	2.75k
Tall Fescue	5 – k	\$4.50	4.50(5-k)
Mixture	5	\$5.25	5.25(5)

- 2. Write an equation to represent the problem. 5.75k + 4.50(5 k) = 5.25(5)
- 3. How much Kentucky Blue Grass does the nursery use in 5 pounds of the mixture? 3 lb
- 4. How much Tall Fescue does the nursery use in 5 pounds of the mixture? 2 lb

TRAVEL For Exercises 5-7, use the following information.

Two commuter trains carry passengers between two cities, one traveling east, and the other west, on different tracks. Their respective stations are 150 miles apart. Both trains leave at the same time, one traveling at an average speed of 55 miles per hour and the other at an average speed of 65 miles per hour. Let t represent the time until the trains pass each other.

5. Copy and complete the table representing the problem.

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	r	t	d = rt
First Train	22	t	551
Second Train	9	t	199

- Write an equation using t that describes the distances traveled. 55t + 65t = 150
- 7. How long after departing will the trains pass each other? 1.25 h
- 8. TRAVEL Two trains leave Raleigh at the same time, one traveling north, and the other south. The first train travels at 50 miles per hour and the second at 60 miles per hour. In how many hours will the trains be 275 miles apart? 2.5 h
- 9. JUICE A pineapple drink contains 15% pineapple juice. How much pure pineapple juice should be added to 8 quarts of the drink to obtain a mixture containing 50% pineapple

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b. Why must y be an even number? If y is odd, then x won't be an integer.

a. First solve the equation for x. x = 16

1. 2x + 5y = 32

c. Find at least one solution. Any of these: (11, 2), (6, 4), (1, 6)

a. First solve the equation for x. $\mathbf{x} = -$

2. 5x + 2y = 42

Solve each diophantine equation by finding at least one pair of positive integers that makes the equation true. Some hints are given to help you.

When the coefficients of an indeterminate equation are integers and you are asked to find solutions that must be integers, the equation is called *diophantine*. Such equations can be quite difficult to solve, often involving trial and error—and some luck!

The first great algebraist, Diophantus of Alexandria (about A.D. 300), devoted much of his work to the solving of indeterminate equations. An indeterminate equation has more than one variable and an

Diophantine Equations

Enrichment

3-9

unlimited number of solutions. An example is x + 2y

Reading to Learn Mathematics

Weighted Averages

Pre-Activity How are scores calculated in a figure skating competition?

Read the introduction to Lesson 3-9 at the top of page 171 in your textbook. Why is the sum of Ilia Kulik's scores divided by 3?

Her first score is counted once and her second score

Reading the Lesson

1. Read the definition of weighted average on page 171 of your textbook. What is meant by the weight of a number in a set of data?

the number of times the number occurs in the set of data

- **2.** Linda's quiz scores in science are 90, 85, 85, 75, 85, and 90. What is the weight of the score 85? 3
- 3. Suppose Clint drives at 50 miles per hour for 2 hours. Then he drives at 60 miles per hour for 3 hours
- a. Write his speed for each hour of the trip.

 Speed	20	20	09	09	09
Hour	-	2	8	4	വ

b. What is the weight of each of the two speeds? 50 mph: 2; 60 mph: 3

Helping You Remember

4. Making a table can be helpful in solving mixture problems. In your own words, explain how you use a table to solve mixture problems.

Complete each row to write an expression in the last column for each part of the problem and for the combination, then write an equation using those expressions from the last column.

Any of these: (14, 4), (9, 11), (4, 18)

(11, 1) or (4, 3)

3. 2x + 7y = 29

4. 7x + 5y = 118

(19, 4), (32, 12) or any pair when y = 4n and n is a positive odd number **5.** 8x - 13y = 100

(6, 1) or (2, 4)

6. 3x + 4y =

(5, 1), (19, 6) or any pair when y = 5m - 4 and m is a positive number 7. 5x - 14y = 11

(4, 4) or (1, 11) **8.** 7x + 3y = 40

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c. Why must (2-2y) be a multiple of 5? Otherwise, x won't be an integer. **b.** Rewrite your answer in the form x = 8 + some expression. $x = 8 + \frac{2-2y}{2}$

d. Find at least one solution. Any of these: (8, 1), (6, 6), (4, 11), (2,

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Form 1 **Page 191**

1. _D_

Page 192

11. B

Form 2A **Page 193**

1. B

2. D

12. C

3. B

13. **A**

4. _D_

14. D

4. B

5. C

15. C

5. D

6. **A**

16. C

17. <u>B</u>

7. <u>B</u>

18. D

7. C

8. <u>B</u>

19. B

8. D

9. **A**

20. A

9. C

10. _D_

45 **B:** _

10. <u>B</u>

Form 2A (continued)

Page 194

11. B

12. A

13. C

14. B

15. C

16. B

17. <u>D</u>

18. **A**

19. B

20. C

3.6 L

1. **A**

5. A

6. D

7. <u>B</u>

Form 2B

Page 195

2. _C_

3. _C_

8. C

9. A

Page 196

11. B

12. D

13. C

14. A

15. B

16. D

17. <u>B</u>

18. A

19. A

20. C

21 B: ____

Form 2C Page 197

6.
$$14\frac{2}{5}$$

9.
$$36 - x = 3(4 + x)$$

Three times the sum of *x* and *y* equals two

10. times y minus x.

$$n-3.5=12.7;$$
11. _____16.2

$$12. \ \ \frac{5n+12=-3;-3}{}$$

Page 198

15.
$$\frac{1\frac{1}{3}}{3}$$

$$\begin{array}{ccc}
19. & & & & & \\
& & & & & \\
20. & & & & & \\
\end{array}$$

$$h = \frac{V}{\pi r^2}$$
; 10.5 in.

Form 2D

Page 199

2.
$$\frac{\frac{2}{3}}{3}$$

6.
$$7\frac{5}{7}$$

9.
$$18 + n = 7(n - 3)$$

Three divided by y minus five equals x times the

10. sum of *y* and 7.

$$_{11}$$
, $n-8.1=4.9$; 13

12.
$$6n + 15 = 9; -1$$

Page 200

15.
$$1\frac{4}{5}$$

$$20. r = s(4v - t)$$

25.
$$h = \frac{V}{\pi r^2}$$
; 18.67 in.

Form 3

Page 201

3.
$$-2\frac{2}{3}$$

5.
$$-1\frac{2}{13}$$

7.
$$\frac{8}{\frac{x-45}{12}+20=5(32-x)}$$

9.
$$\frac{3}{5}x = 1; \frac{5}{3}$$

10.
$$(x + 2)10 = 8x + 36; 8$$

Five times the sum of two times x and three times y equals the square of y minus two times the cube of x.

Page 202

$$-\frac{7}{9}$$

$$x = \frac{r+n}{a}$$

$$20. \qquad x = \frac{rs - t}{4}$$

Page 203, Open-Ended Assessment Scoring Rubric

Score	General Description	Specific Criteria
4	Superior A correct solution that is supported by well-developed, accurate explanations	 Shows thorough understanding of the concepts of translating between verbal sentences and equations, solving equations, percents of increase and decrease, uniform motion problems, and proportions. Uses appropriate strategies to solve problems. Computations are correct. Written explanations are exemplary. Goes beyond requirements of some or all problems.
3	Satisfactory A generally correct solution, but may contain minor flaws in reasoning or computation	 Shows an understanding of the concepts of translating between verbal sentences and equations, solving equations, percents of increase and decrease, uniform motion problems, and proportions. Uses appropriate strategies to solve problems. Computations are mostly correct. Written explanations are effective. Satisfies all requirements of problems.
2	Nearly Satisfactory A partially correct interpretation and/or solution to the problem	 Shows an understanding of most of the concepts of translating between verbal sentences and equations, solving equations, percents of increase and decrease, uniform motion problems, and proportions. May not use appropriate strategies to solve problems. Computations are mostly correct. Written explanations are satisfactory. Satisfies the requirements of most of the problems.
1	Nearly Unsatisfactory A correct solution with no supporting evidence or explanation	 Final computation is correct. No written explanations or work is shown to substantiate the final computation. Satisfies minimal requirements of some of the problems.
0	Unsatisfactory An incorrect solution indicating no mathematical understanding of the concept or task, or no solution is given	 Shows little or no understanding of most of the concepts of translating between verbal sentences and equations, solving equations, percents of increase and decrease, uniform motion problems, and proportions. Does not use appropriate strategies to solve problems. Computations are incorrect. Written explanations are unsatisfactory. Does not satisfy requirements of problems. No answer may be given.

Page 203, Open-Ended Assessment Sample Answers

In addition to the scoring rubric found on page A34, the following sample answers may be used as guidance in evaluating open-ended assessment items.

- 1a. The student should explain that the first phrase is a product of *x* and *y* and then the addition of z, while the second phrase is a product of *x* and the quantity y + z.
- **1b.** Check that the student's values for x, y, and z satisfy both xy + z and x(y+z). One example is x=1, y=2, and z = 3. Another example is x = 2, y = 3, and z = 0.
- $2a. \quad \frac{ry+s}{m}-t=x$ (Original equation) $\frac{ry+s}{m}-t+t=x+t$ (Add t to each side.) $\frac{ry+s}{m} = x+t$ (Simplify.)

$$m\left(\frac{ry+s}{m}\right) = m(x+t)$$
fultiply each side by m

(Multiply each side by m.)

$$ry + s = mx + mt$$
 (Simplify.)

ry + s - s = mx + mt - s(Subtract *s* from each side.)

$$ry = mx + mt - s$$
 (Simplify.)

$$\frac{ry}{r} = \frac{mx + mt - s}{r}$$
 (Divide each side by r .)

$$y = \frac{mx + mt - s}{r}$$

(Simplify.)

The value of *y* is $\frac{mx + mt - s}{r}$.

2b. Division by 0 is undefined, so in the original equation $m \neq 0$, and in the final equation $r \neq 0$.

- **3a.** The student should conclude that a 10% decrease followed by a 10% increase results in a net decrease of 1%. Thus, the final cost would be 99% of the original price.
- **3b.** Since multiplication is commutative, multiplying by 1.1 and then 0.9 would yield the same result as multiplying by 0.9 and then 1.1. The student should conclude that a 10% increase followed by a 10% decrease yields the same result as a 10% decrease followed by a 10% increase.
- **4a.** Since the two people walked for the same amount of time and time can be calculated as distance divided by rate, the proportion

 $\underline{\text{Tony's distance}} = \underline{\text{Ivia's distance}}$ Tony's rate Ivia's rate can be used to solve this problem.

- **4b.** The length of Tony's walk can be calculated directly from his rate of 3 miles per hour and his distance of 6 miles. Ivia walked 1 mile per hour faster, so her rate is 4 miles per hour. The length of Ivia's walk can be calculated directly from her rate of 4 miles per hour and distance of 6 miles. Thus, a proportion would not be used to solve this problem.
- **5a.** Sample answer: x + 2 = 10, x 2 = 6, $2x = 16, \frac{x}{2} = 4$
- **5b.** Sample answer: 2x + 1 = x + 9
- **5c.** These two equations are equivalent. The solution to both equations is 5. The student should recognize that the solution to all equations in parts a and **b** is 8. Therefore neither of these two equations could be equivalent to any of the equations created for parts a and **b**.

Vocabulary Test/Review | Page 204

- 1. false; added to
- 2. true
- 3. true
- 4. false; more
- 5. false; true
- 6. false; division
- 7. true
- 8. true
- 9. false; percent of decrease
- 10. false; percent of increase
- 11. an equation stating that two ratios are equal
- 12. an equation that states a rule for the relationship between certain quantities

Quiz (Lessons 3-1 through 3-3) Page 205

- 1. 2n = 3(n + 9)
- $y^2 12 = 5x$

Two times *b* minus 3. 10 equals 4.

- The sum of y and the product 4. of three and the square of x is five times x.
- 5. ____14
- 6. ______
- 8. -9
- 9. _____40
- 10. ______

8. _increase; 25%

7 decrease; 28%

Quiz (Lessons 3-6 and 3-7)

no

no

15

27

99

1. ____ yes

Page 206

2. _____

3. _____

4.

5. _____

6. _____

- 9 \$19.08
- 10. \$75.60

Quiz (Lessons 3-4 and 3-5) Page 205

- 1. _____7
- 2. _____84
- $-5\frac{3}{5}$
- ₄ -5
- 5. no solution
- 6. _____
- 7. _____7
- 8. _____C
- 9. _____2
- 10. _____135

Quiz (Lessons 3-8 and 3-9) **Page 206**

1.
$$x = \frac{p+m}{n}$$

$$2. \quad b = x - ac$$

- 3. 4 g
- 4. 2.4 mph

$$_{5} \ell = \frac{P-2w}{2}$$
; 14 m

Mid-Chapter Test Page 207

Part I

- 1. _B_
- 2. _D_
- 3. **A**
- 4. C
- 5. B
- 6. _C_

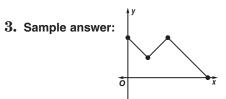
Part II

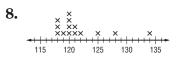
- 7. ____0
- 8. all numbers
- 10. ____\$116.15

Four times *n* equals *m* times the difference of 11. five and *n*.

Three times the sum of y and 5 equals the 12. product of y and 7.

$$5u + 9v$$





10.
$$85 - 9y = 7(4 + y)$$

15.
$$m = n(q - p)$$

Standardized Test Practice

Page 209

Page 210

1. (A) (B) (C) (D)

10				
10.	3	/	2	
		0	9	
	<u>. </u>)()	0	9
	9	Θ	1	9
	3	3	3	(
	4	4	4	4
	5	5)(6	5	5)(6
	7	9	7	9
	8	8	8	8
	9	(9	9

11.

•	1		1	2
	0	00	00	0
		0	0	0
	1	1	1	1
	2	2	2	2
	3	3	3	3
	4	4	4	4
	(5)	(5)	5	(5)
	6	6	6	6
	7	7	7	7
	8	8	8	8
	9	9	9	9

2. (E) (F) (G) (H)

3. (A) (B) (C) (D)

4. E E G H

8 9

8 8 9 9

5. A B C D

6. (A) (B) (C) (D)

14. (A) (B) (C) (D)

7. A B C D

15. (A) (B) (C) (D)

8. E E G H

16. A B C D

9. A B C D

Unit 1 Test Page 211

1. _____5__n³

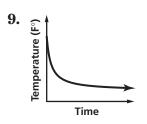
Multiplicative Inverse Property; $\frac{1}{6}$

$$5. 7t^2 + 3t$$

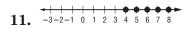
6.
$$7r + 9t$$

$$_{7}$$
 23a + 6b

8. H: a figure is a triangle;C: it is a polygon; If a figure is a triangle, then it is a polygon.



10. 40 people



13. _

16. _____**5** : **1**

Page 212



Median; most of the 18. data clusters near the median.

19. irrational, real

20.
$$\frac{-3.\overline{65}, -\frac{18}{5}, \frac{75}{21}, \sqrt{13}}{}$$

26. all real numbers

$$\frac{3^2}{7}$$

$$_{29.}$$
 $v = t - sr$